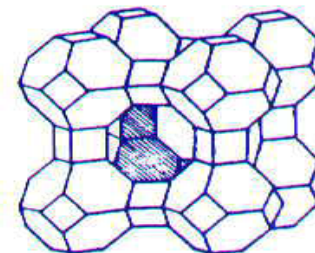
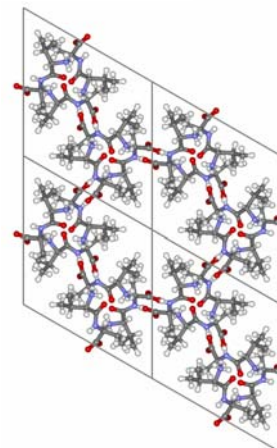
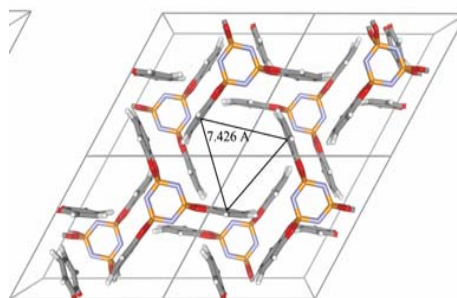
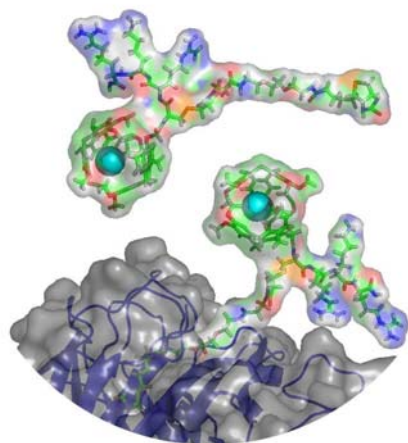
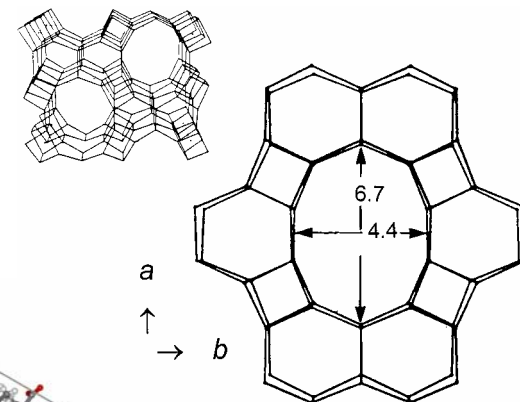
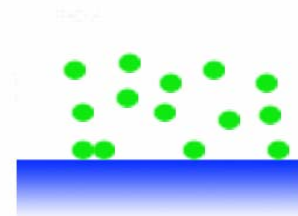


Xe chemical shifts: What do they tell us about the physical system?

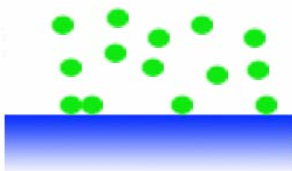
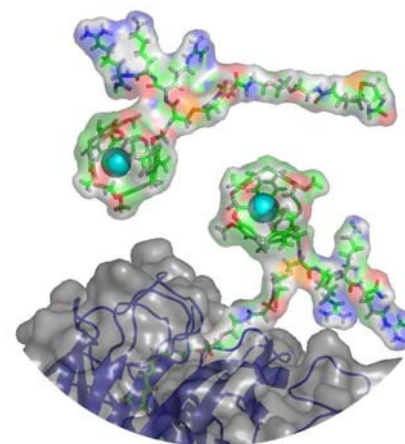
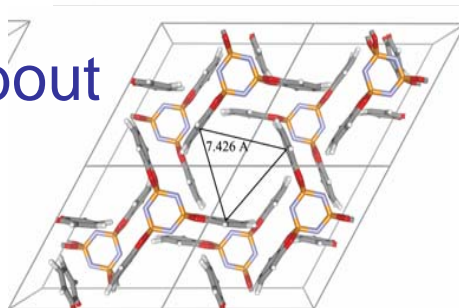
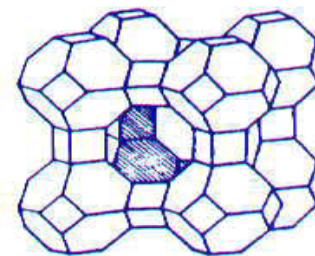
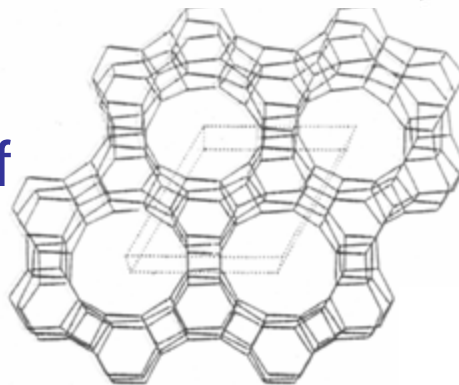
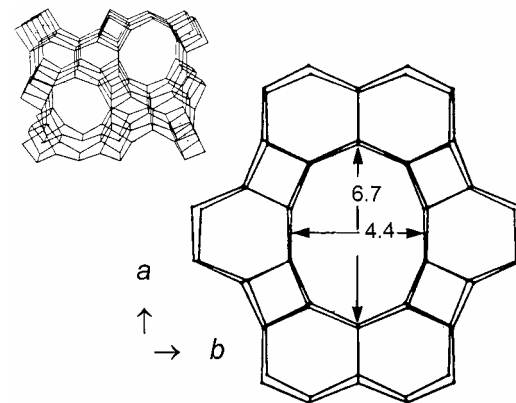
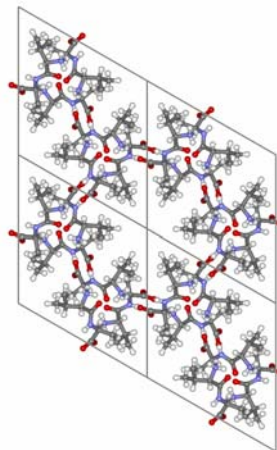
Cynthia J. Jameson

University of Illinois at Chicago



Xe intermolecular chemical shifts

- **exquisitely sensitive** to the environment of the Xe atom
- permits the Xe nucleus to **report attributes of the physical system** in which Xe atom finds itself
- needs **understanding at a fundamental level** so as to elicit the desired detailed information about the physical system



The general approach:

- Use Xe and small molecules to explore **internal surfaces** of nanometer dimensions in model materials (crystalline).
- Measure average **tensor** properties of Xe, where possible, or the average isotropic property, otherwise.
- We employ a property with a **steep dependence on intermolecular distances**, a local probe
- Combine **quantum mechanical calculations of the property as a function of intermolecular separations and configurations** with **Monte Carlo grand canonical averaging or molecular dynamics simulations** to understand/reproduce what is observed.

Simulations:

1. Assume a model of the real physical system
 - Model for shielding response calculation
 - Model for the material system
2. Quantum mechanics: Calculate Xe shielding response as a function of configuration
3. Adopt potential energy of intermolecular interactions between Xe and the environment atoms
4. Choose appropriate averaging process, assuming additivity:
 - Canonical Monte Carlo
 - Grand Canonical Monte Carlo
 - Molecular Dynamics
5. **Simulations produce:**
 - Xe one-body distributions: where does Xe spend time?**
 - Average isotropic Xe chemical shift**
 - Xe line shapes characterizing Xe chemical shift tensor**
 - Xe distribution among cages or phases, etc., etc.**

Information that is encoded in observed Xe spectra:

- structural as well as dynamic information
- the diameter of the channel
- the aspect ratio of the cross section of the channel
- the architecture of the channel
- average size of the cage
- average symmetry of the cage
- number of molecules per cage
- electronic structure of atoms constituting the cavity walls
- rate of cage-to-cage jumps within the crystal
- coverage on a single crystal surface
-
-

Quantum-mechanical molecular level interactions determine:

- (A) the sorption thermodynamics,
- (B) the Xe exchange dynamics,
- (C) the instantaneous shielding at a Xe nucleus arising from the electronic environment formed by all the rest of the atoms (including other Xe atoms).

The **average Xe chemical shift** is a weighted average of the Xe shielding function (C) with weighting factors determined by (A) and (B)

How is information encoded into the average Xe chemical shift?

The Xe chemical shift encodes any structural or dynamic information that depends on:

- **Electronic structure of the neighbors of the Xe atom**
- **Configurations of neighbor atoms, how many, at what distances**
- **The relative probabilities of the various configurations**

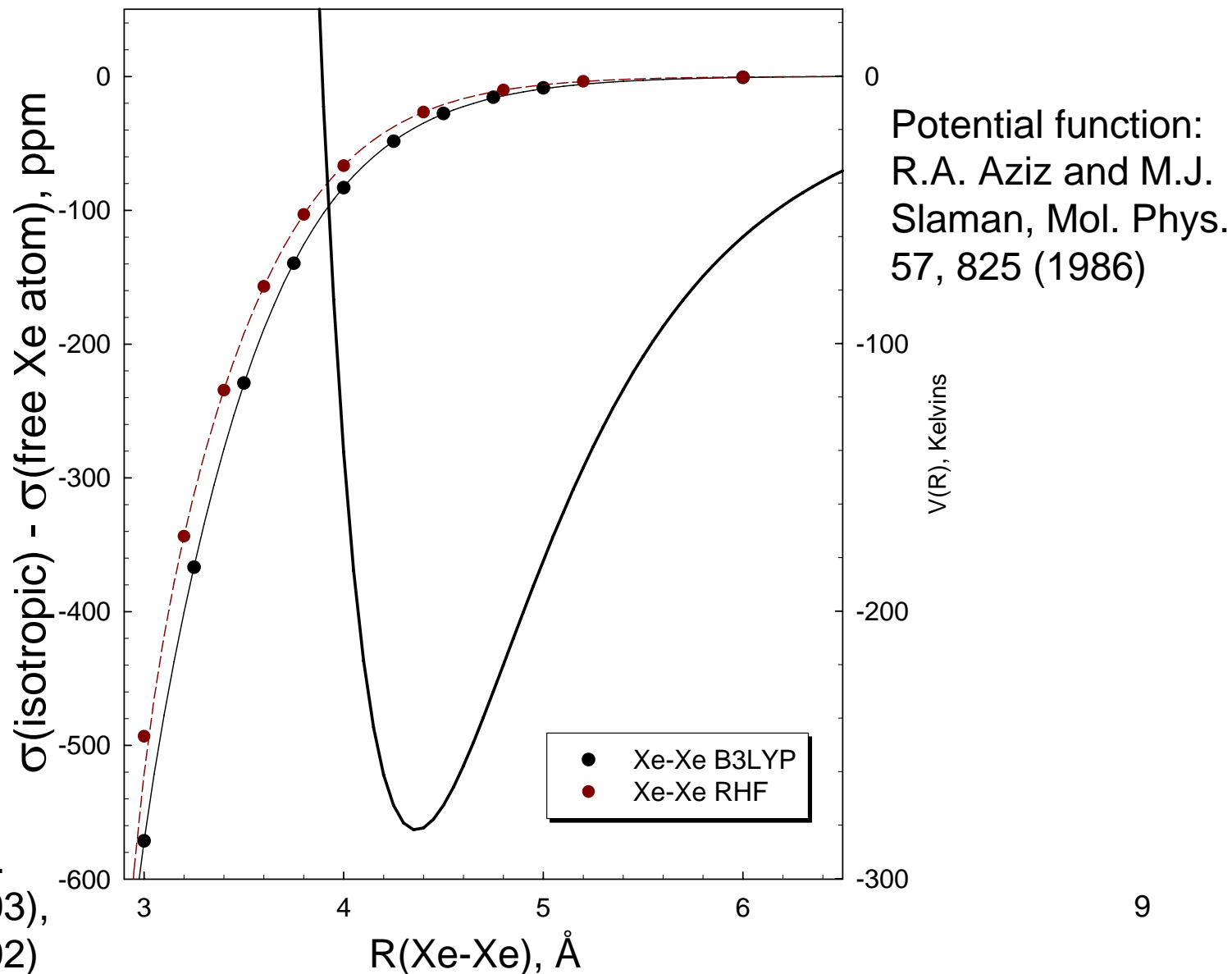
All these are ultimately **quantum mechanical** in origin.

For one neighbor

Ab initio calculations show that

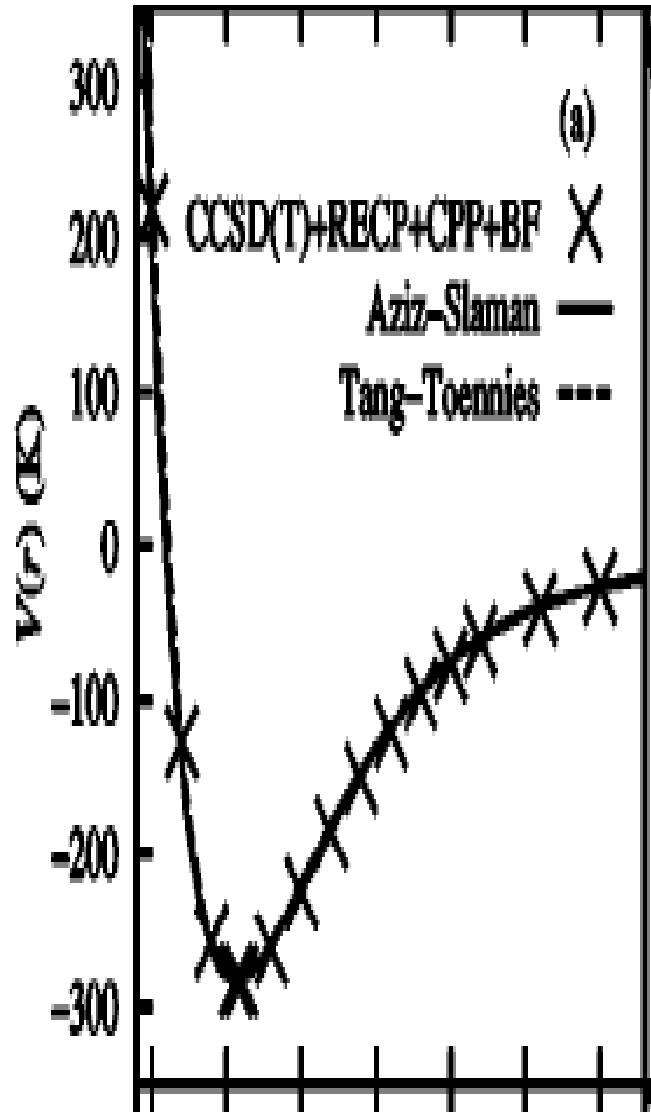
- (1) the Xe shielding response drops off very steeply with distance of the neighbor atom**
- (2) the magnitude of Xe shielding response depends on the electronic structure of the neighbor atoms or molecules**

Xe isotropic shielding function $\sigma(R)$ and potential function $V(R)$ for the Xe-Xe system



Jameson et al.
J. Chem. Phys.
118, 2575 (2003),
116, 3805 (2002)

X Best theoretical potential energy curve for Xe_2



Hanni, Lantto,
Nuneberg, Jokisaari,
Vaara, J.Chem. Phys.
121, 5908 (2004)

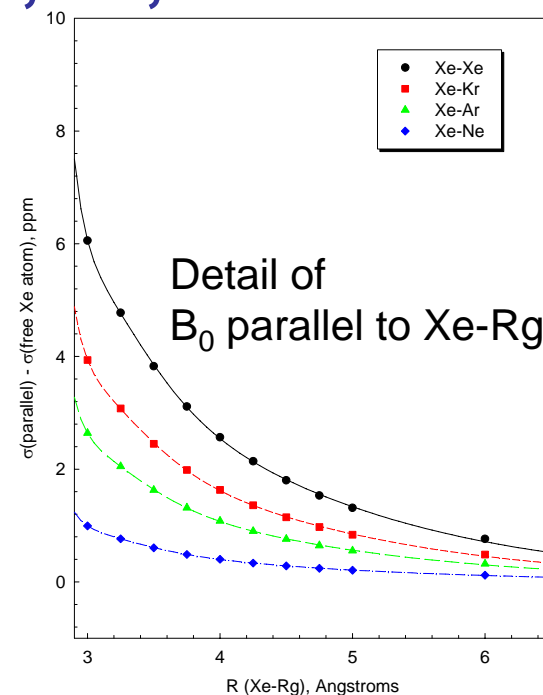
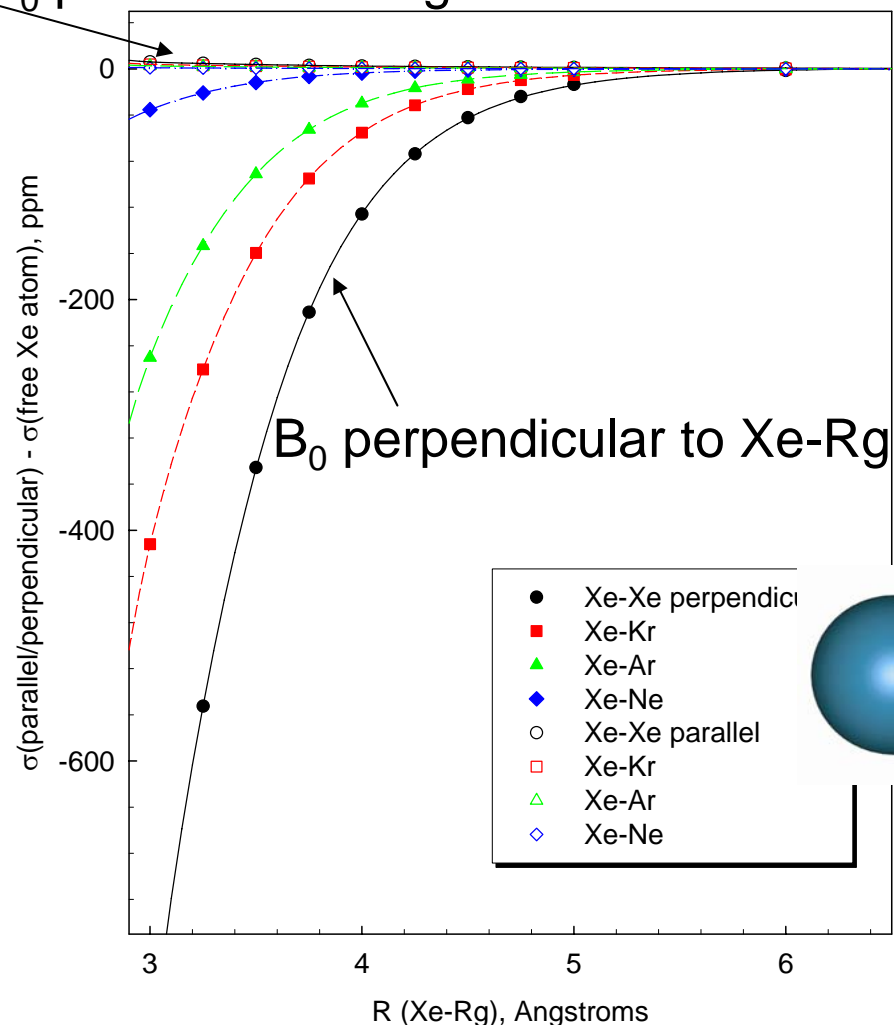
The Xe SHIELDING RESPONSE

changes with magnetic field direction

and depends on the
electronic structure
of the neighbor:

Xe, Kr, Ar, Ne

B_0 parallel to Xe-Rg



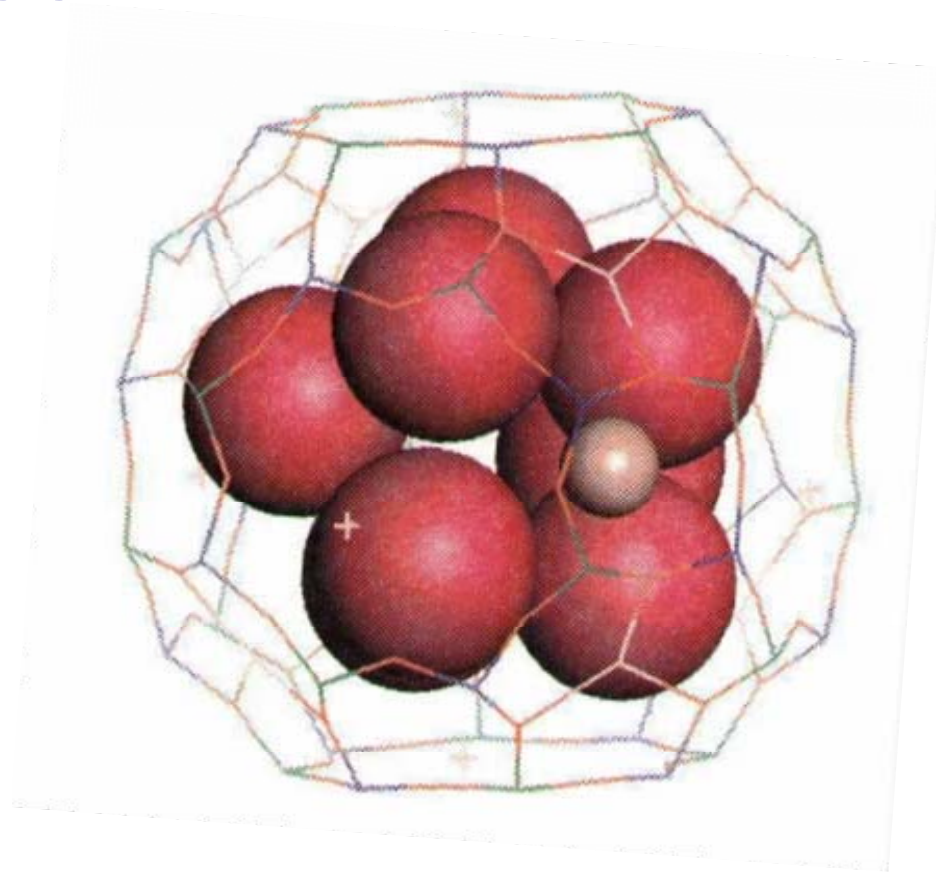
Xe shielding depends on how many neighbor atoms, at what distances

For a single instantaneous configuration, the Xe shielding response is **nearly additive**.

For example, the ab initio Xe shielding for Xe surrounded by some number of Ne atoms (in circles or helices) is found to be nearly the same as the **sum** of the ab initio Xe-Ne shieldings at those Xe-Ne distances

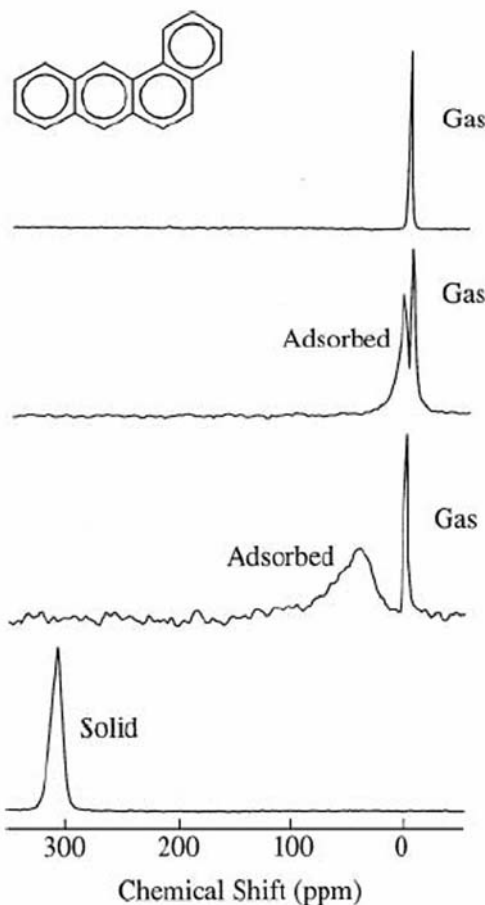
Shielding is a very local molecular property because of the r_N^{-3} part of the operator

How many neighbor atoms, at what distances?



How many neighbor atoms, at what distances?

Example:



dilute Xe gas
large $r_{\text{Xe-Xe}}$, $\sigma(\text{Xe atom})$

limiting case
one Xe on crystal
 $\sigma(r_{\text{Xe-C}})$, short $r_{\text{Xe-C}}$

occasional Xe-Xe neighbors
 $\sigma(r_{\text{Xe-C}})$, short $r_{\text{Xe-C}}$
+ $\sigma(r_{\text{Xe-Xe}})$, short $r_{\text{Xe-Xe}}$

many Xe-Xe neighbors
 $\sigma(r_{\text{Xe-C}})$, short $r_{\text{Xe-C}}$
+ $\sum \sigma(r_{\text{Xe-Xe}})$, short $r_{\text{Xe-Xe}}$

D. Raftery, H. Long,
T. Meersmann,
P.J. Grandinetti,
L. Reven, and A. Pines,
Phys. Rev. Lett. **66**, 584
(1991).

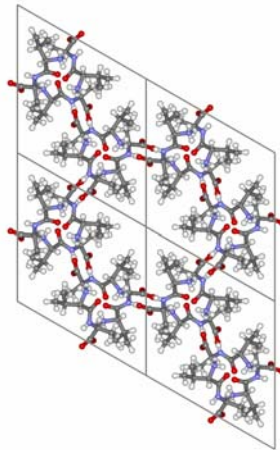
What fraction of the time a particular Xe-neighbor configuration is found

- Probability of finding Xe at a particular location depends on the intermolecular potential functions between Xe and the neighbor atoms. This too can be assumed to be additive and distance-dependent within a grand canonical Monte Carlo simulation.

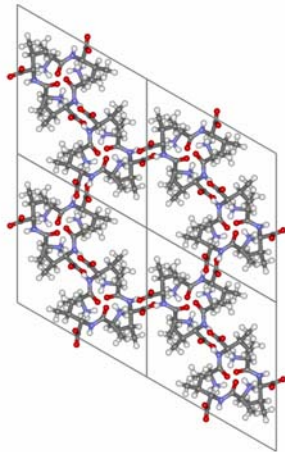
For a given solid material structure (i.e., equilibrium positions of atoms which constitute the solid), the **electronic structure of the atoms** which are accessible to Xe atoms determine the

- **adsorption isotherm for Xe in the material**
i.e., the total Xe occupancy (at a given temperature and overhead Xe pressure)

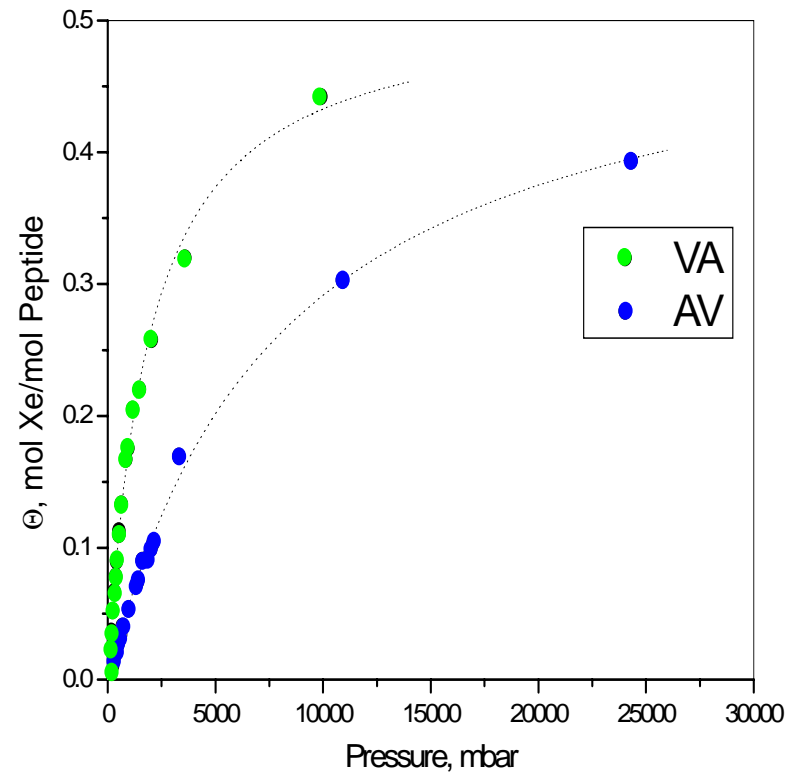
Channel structure & adsorption isotherm



L-Val-L-Ala



L-Ala-L-Val



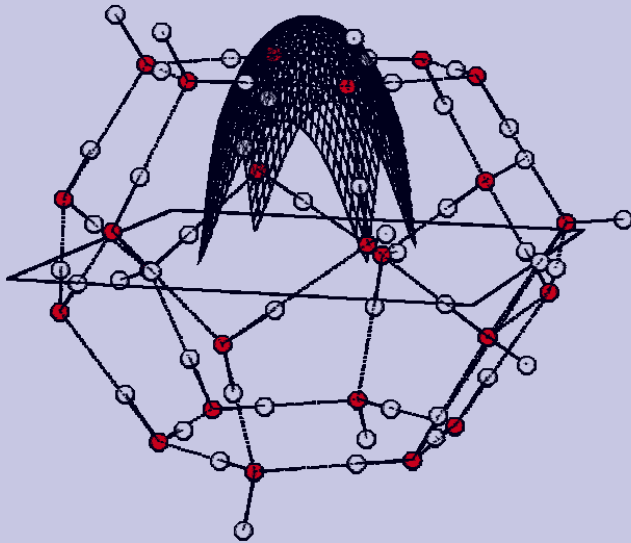
adsorption isotherm
can be reproduced
by simulations

Thus, we have an interesting intrinsic connection between the **Xe shielding function** for a particular configuration of atoms and the **probability of such a configuration occurring** at a particular temperature.

Intermolecular chemical shifts

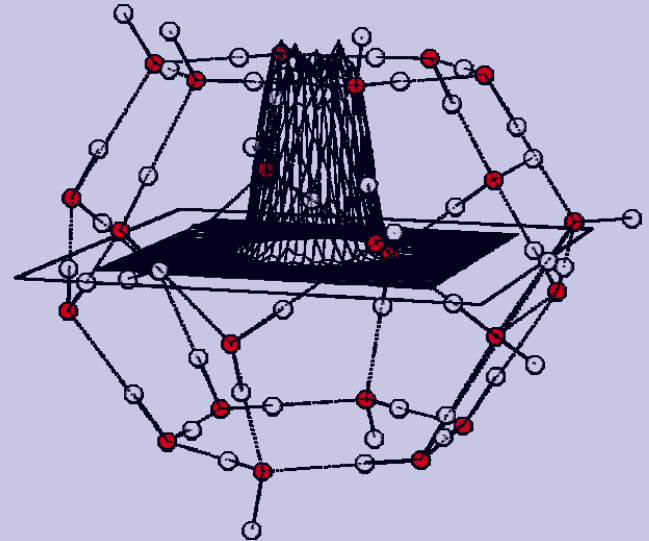
The Xe **SHIELDING SURFACE**:
the shielding as a function
of configuration (coordinates)
of the system

(a) isotropic shielding surface



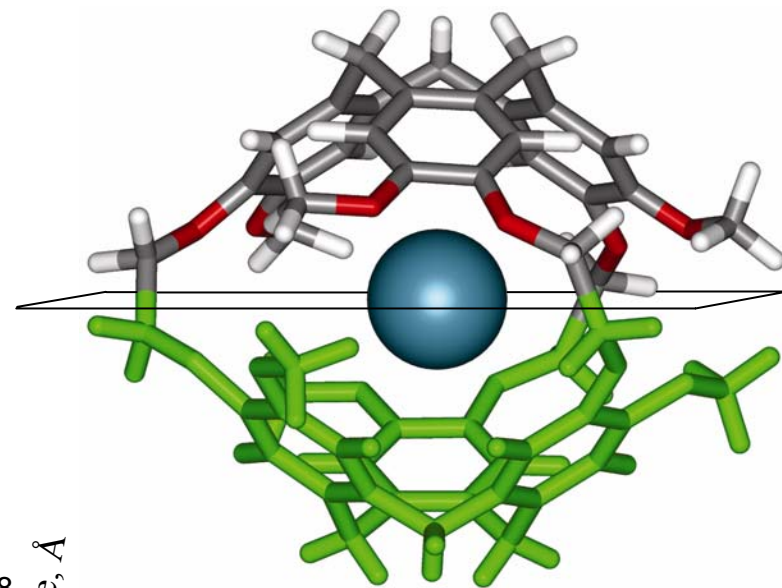
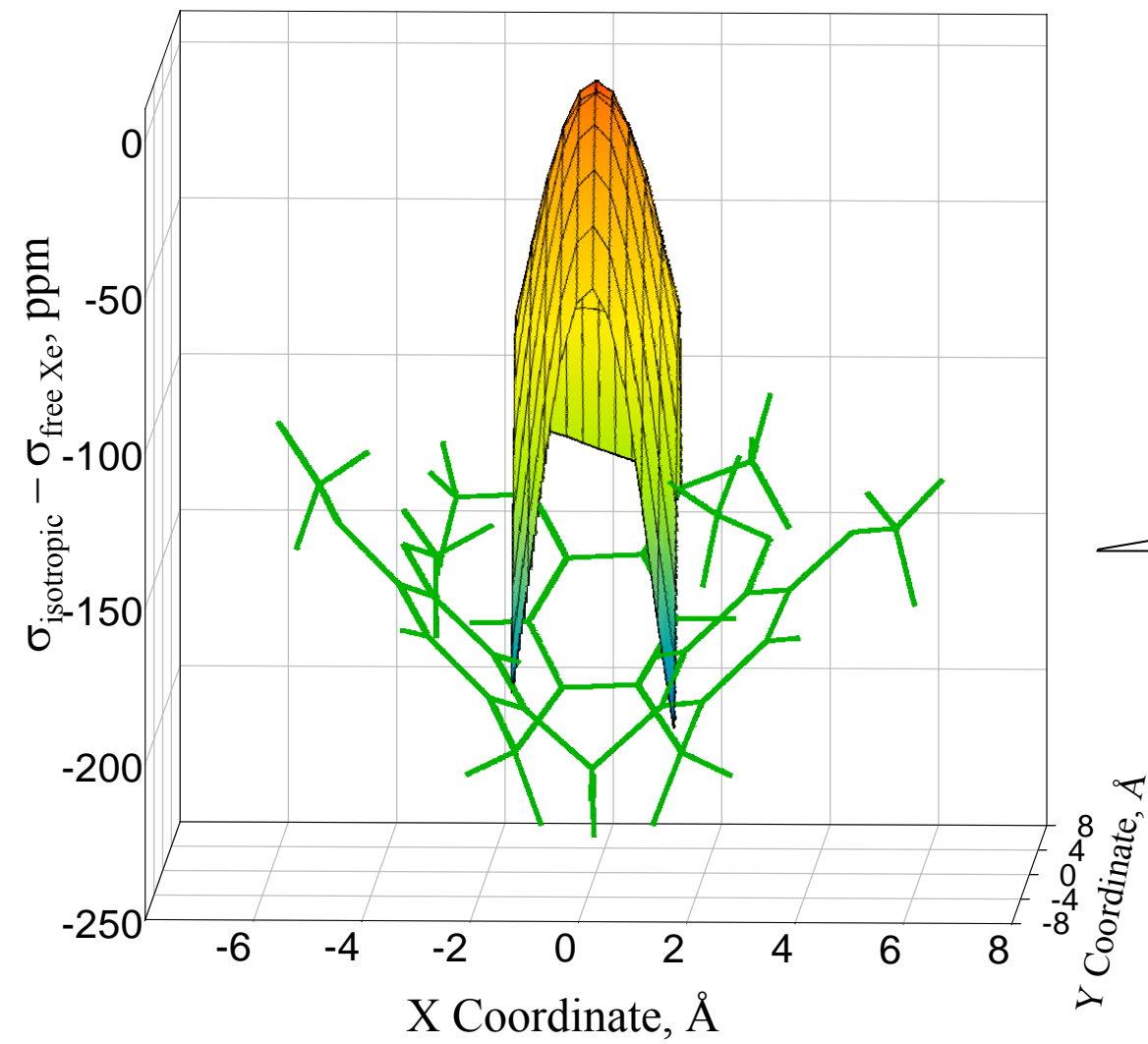
The Xe one-body distribution:
the **PROBABILITY** of finding
the system in a given
configuration

(b) one-body distribution surface

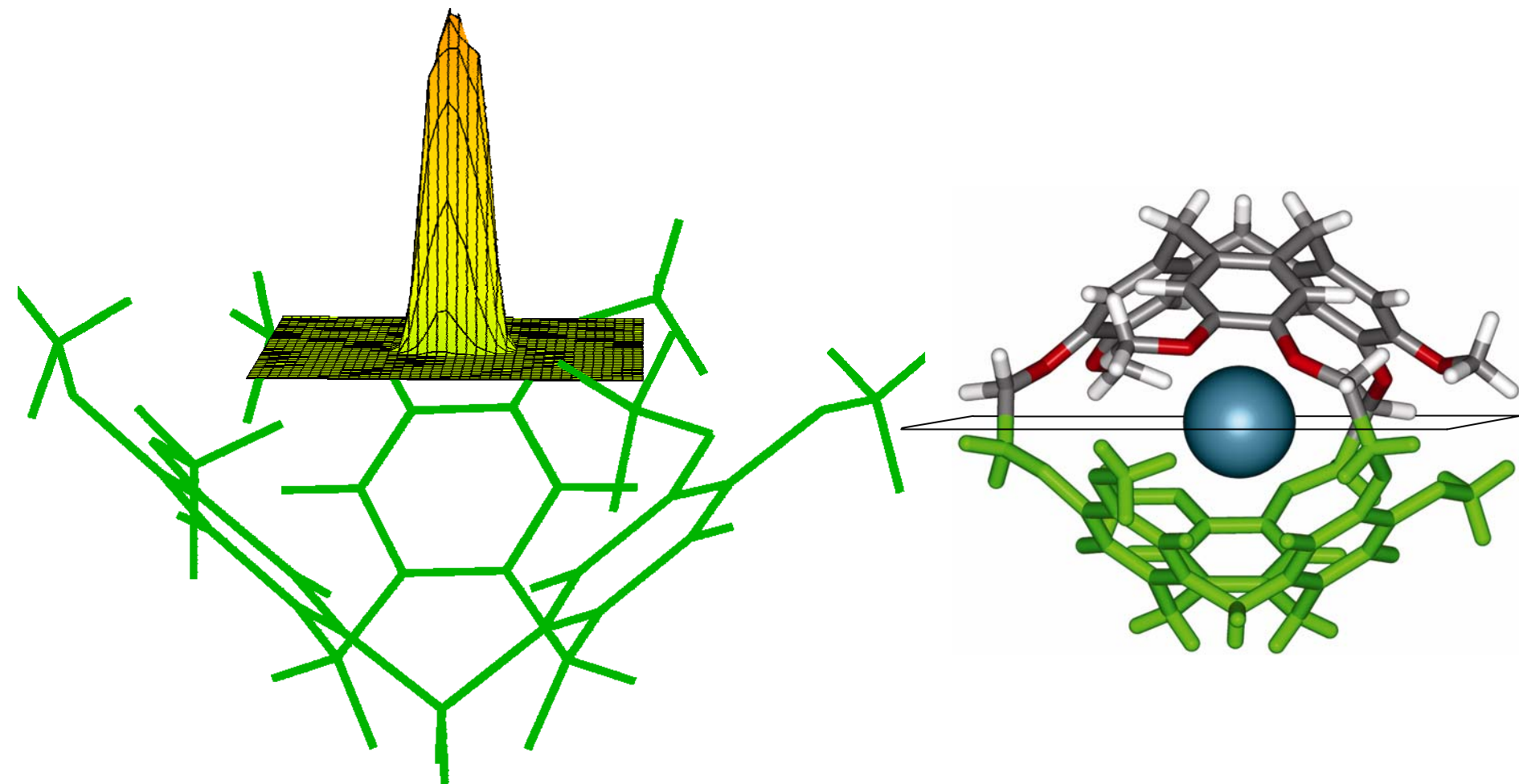


Xe in the $5^{12}6^2$ cage of clathrate hydrate Structure I

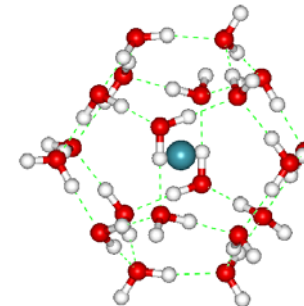
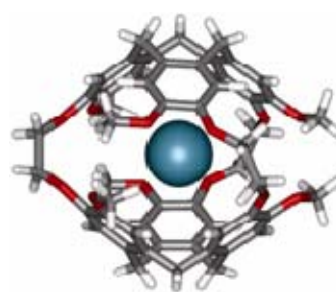
The Xe shielding surface for Xe@cryptoA



One-body distribution function for Xe@cryptoA from Monte Carlo simulations



Xe in cages



QUESTION:

What information is encoded into the Xe chemical shift of a Xe atom trapped in a cage?

- architecture of the cage: size, shape
- hydrogen-bonding network
- aromatic rings
- vibrational, other dynamics of the cage atoms
- electronic structure of the cage: availability of electrons that can elicit a shielding response

Xe in the cages of clathrate hydrates Structure I and II

interesting as a test:

- a hydrogen-bonded network
- disordered proton configurations, yet must obey ice rules
- try out an additive pair tensor model

The dimer tensor model for Xe shielding tensor in a cage

For example, the contribution to the shielding of Xe at point J due to i^{th} O atom located at (x_i, y_i, z_i) is given by the ab initio tensor components for the

XeO dimer, the functions $\sigma_{\perp}(r_{\text{XeO}})$, $\sigma_{||}(r_{\text{XeO}})$.

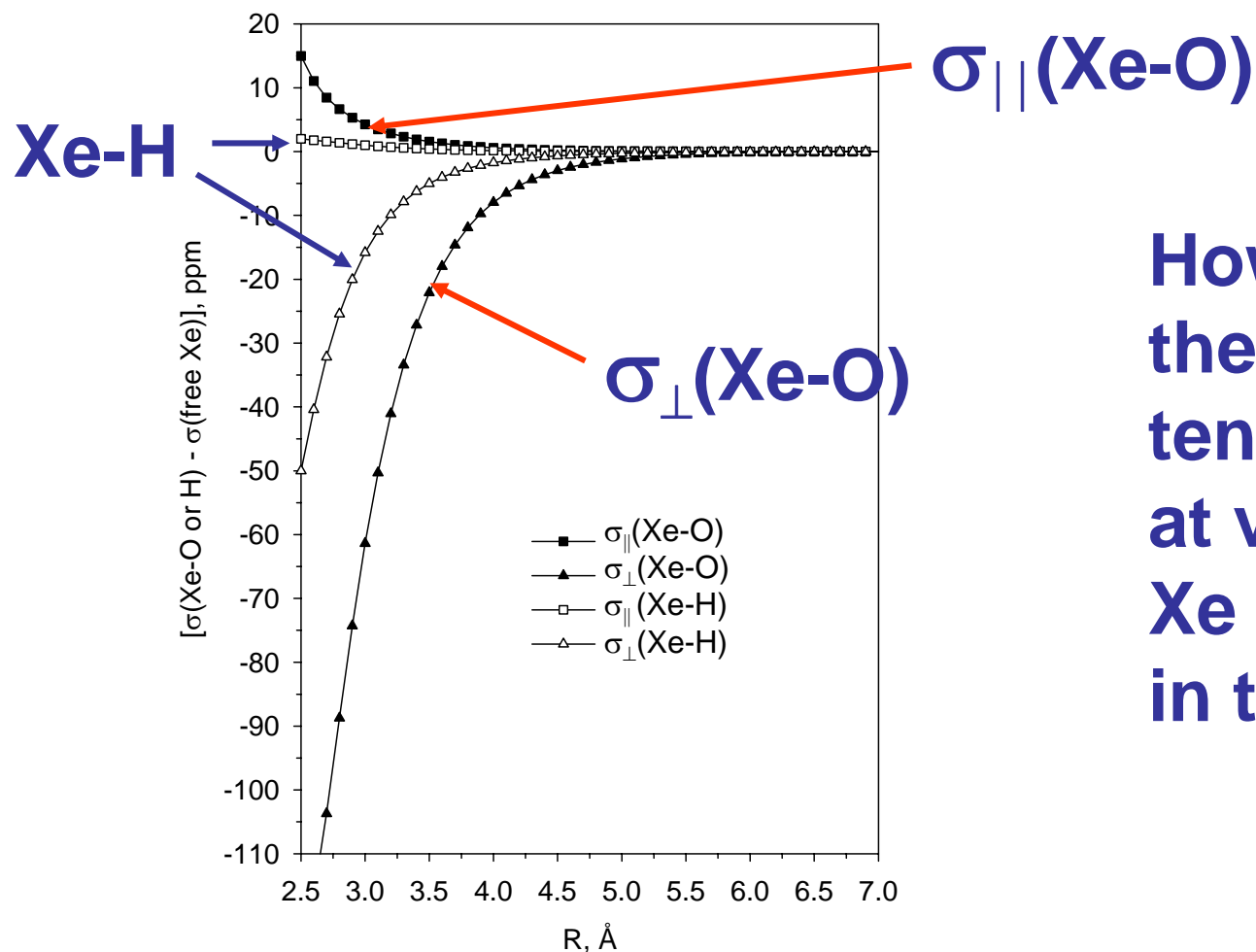
Tensor components in the laboratory frame
(frame of the simulation box):

$$\sigma_{XX} = [(x_i - x_J)/r_{iJ}]^2 \sigma_{||} + \{[(y_i - y_J)/r_{iJ}]^2 + [(z_i - z_J)/r_{iJ}]^2\} \sigma_{\perp}$$

$$\frac{1}{2}(\sigma_{XY} + \sigma_{YX}) = [(x_i - x_J)/r_{iJ}] \bullet [(y_i - y_J)/r_{iJ}] (\sigma_{||} - \sigma_{\perp})$$

Sum over all such contributions from every O, every H atom.

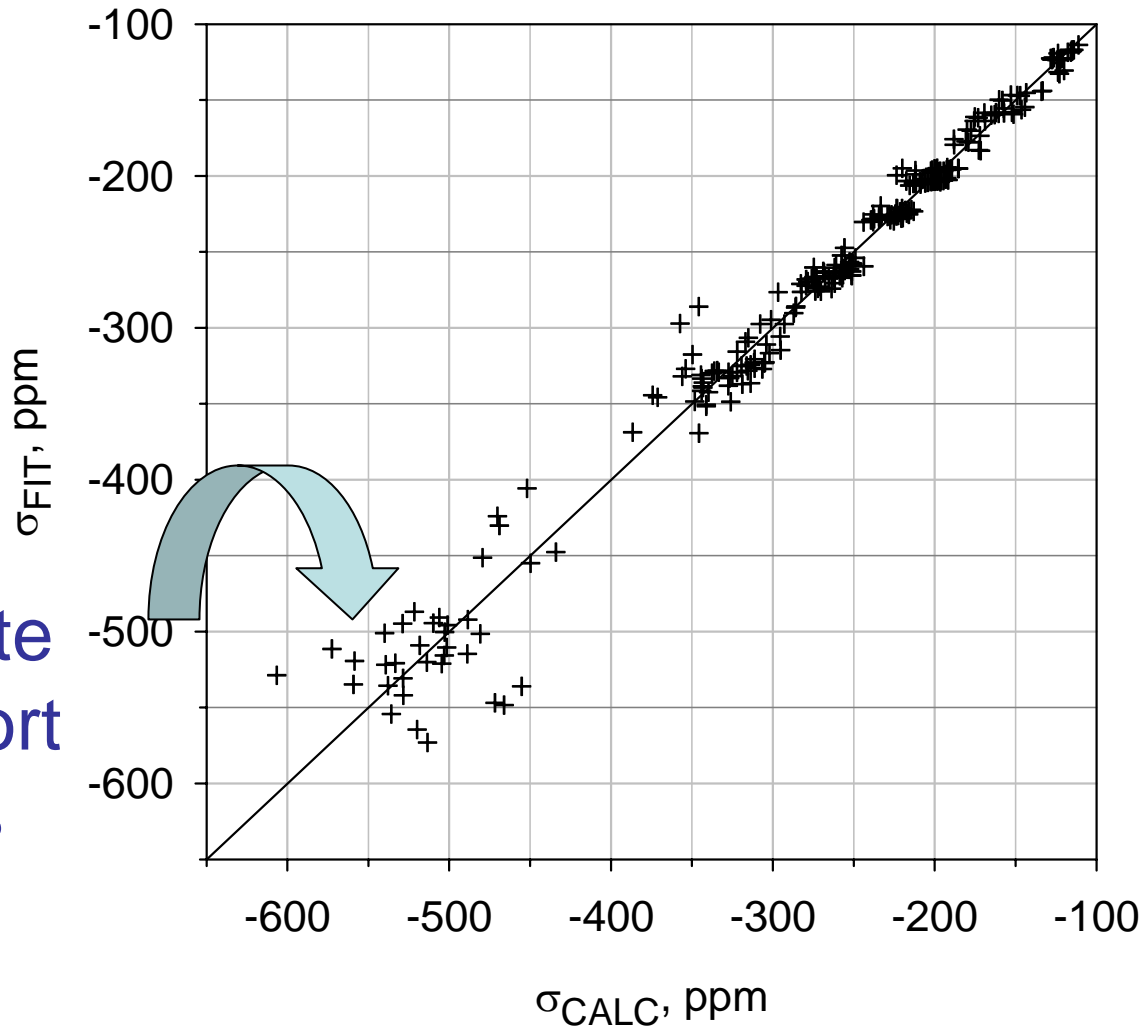
The Xe-O and Xe-H shielding tensors



How to describe
the ab initio
tensor values
at various
Xe positions
in the cage?

Sums over these **pair** shielding functions
reproduce the ab initio Xe shielding tensor
at each Xe position within the cage (in model XCAGE/PCA)

Sum over pair shielding tensors reproduce ab initio tensor components

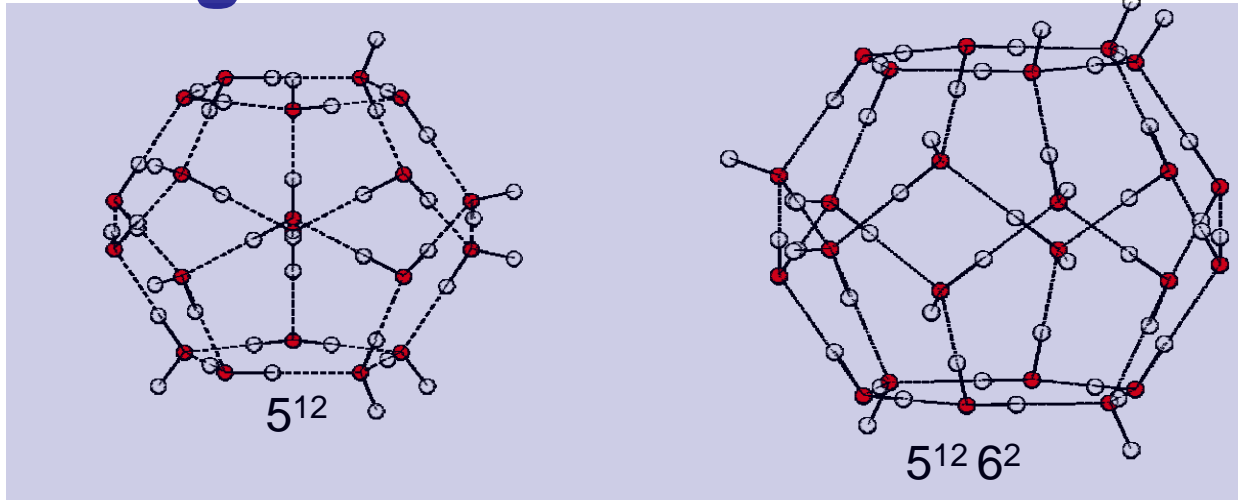


but deviate
at the short
distances

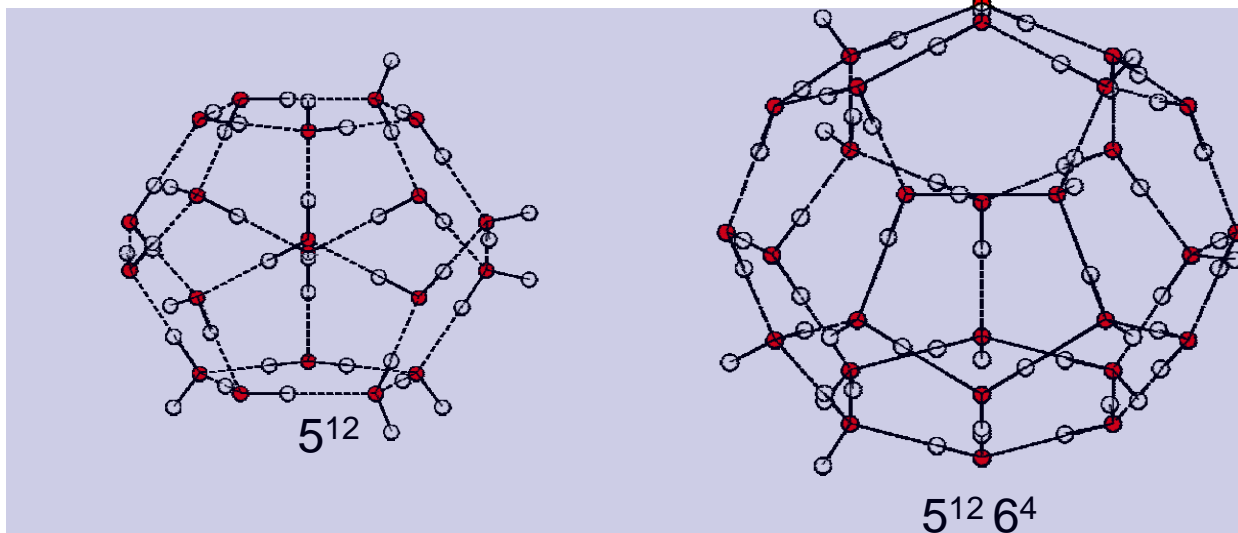
Clathrate hydrates

the cages

Structure I



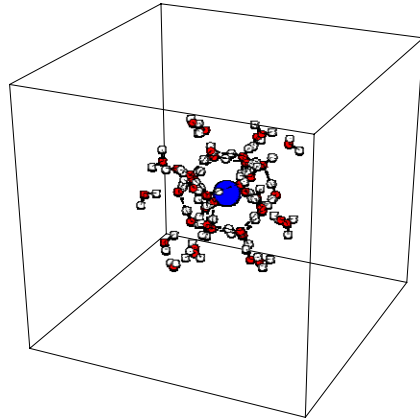
Structure II



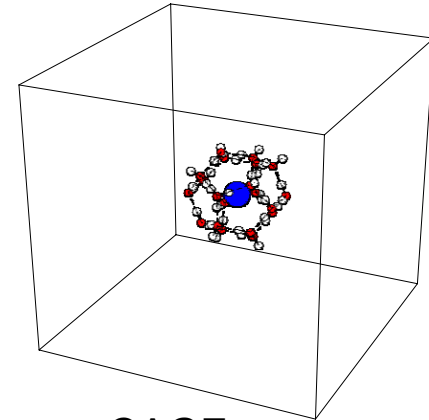
How to model a cage in a hydrogen bonded network?

Generate crystal fragment with a valid proton configuration:
47.93 Å on the side, 4x4x4 unit cells, 2944 water molecules

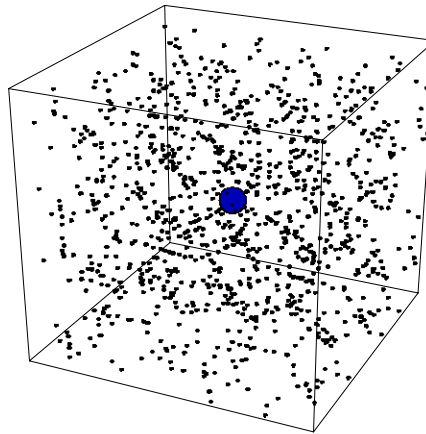
MODELS



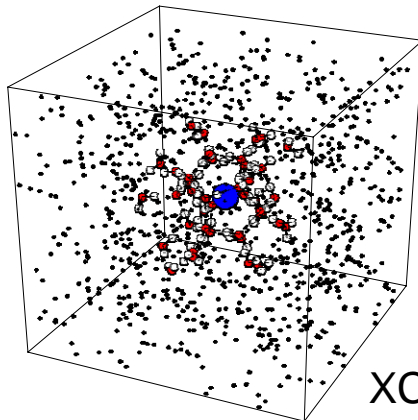
XCAGE



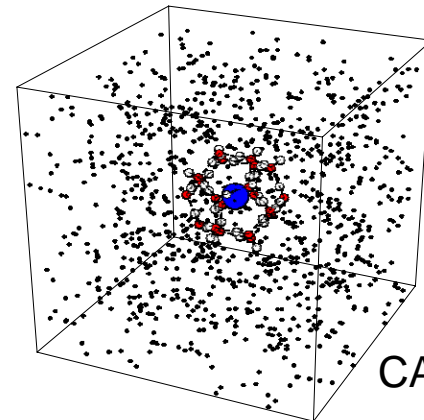
CAGE



PCA

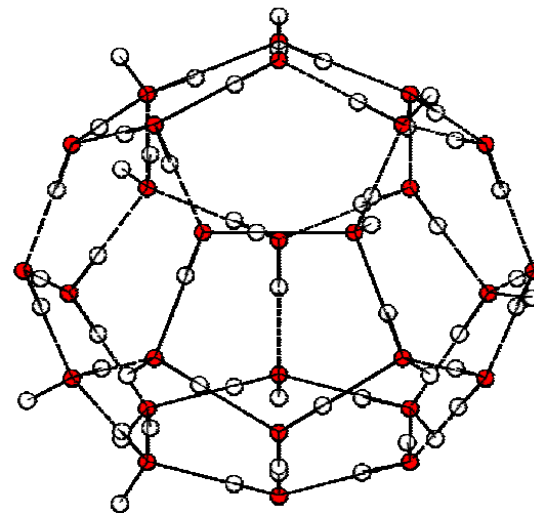
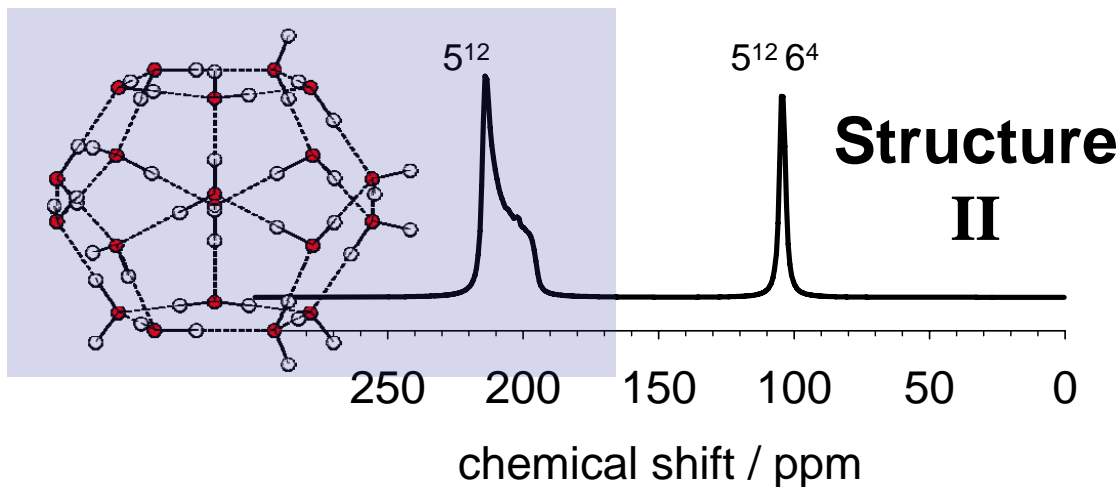
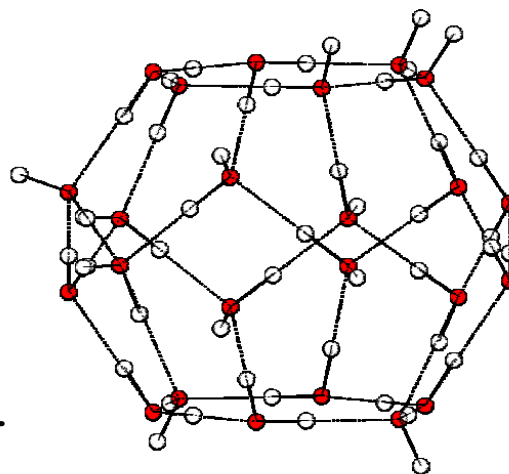
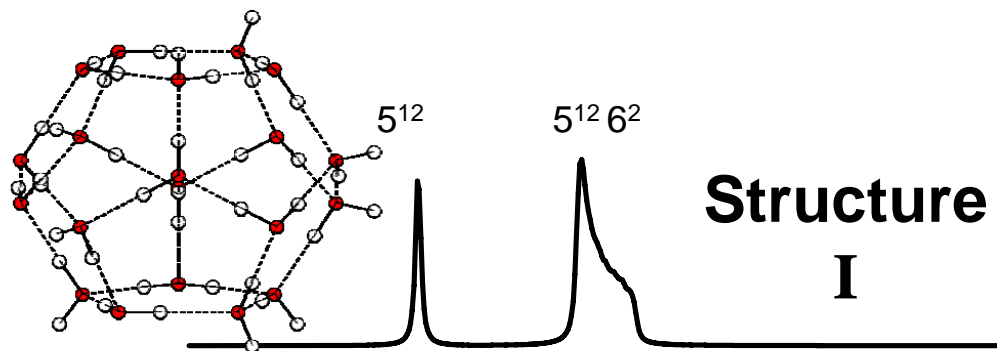


XCAGE/PCA



CAGE/PCA

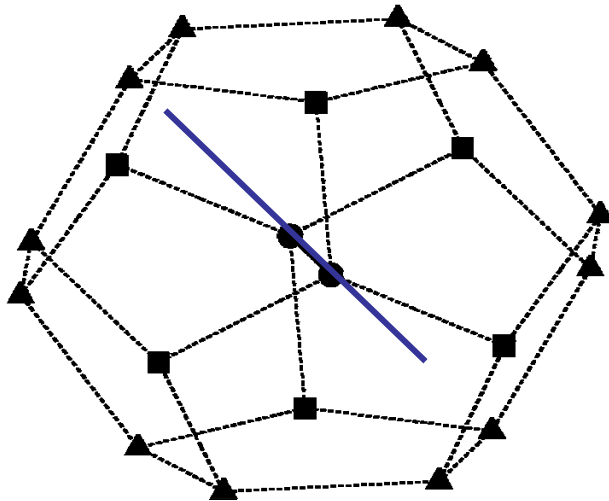
Calculated Xe NMR lineshapes from Monte Carlo simulations in single cages:



using
the same Xe-O and Xe-H shielding tensor functions,
the same Xe-O and Xe-H potential functions

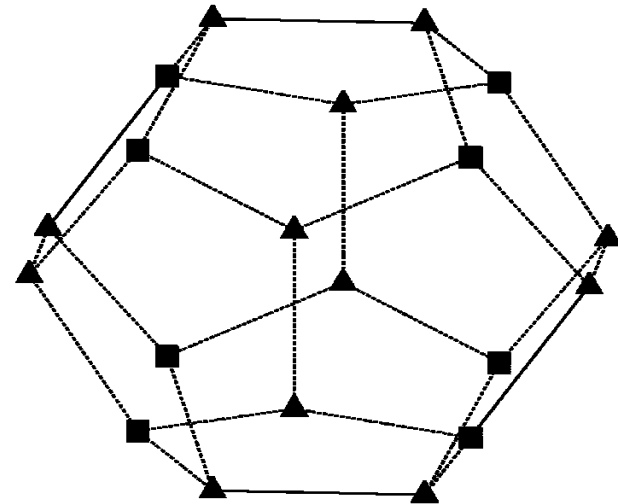
Why is the Xe lineshape in the 5^{12} cage in Structure II axially anisotropic while the Xe lineshape in the 5^{12} cage in Structure I is isotropic?

(a) 5^{12} cage
in structure II



vs.

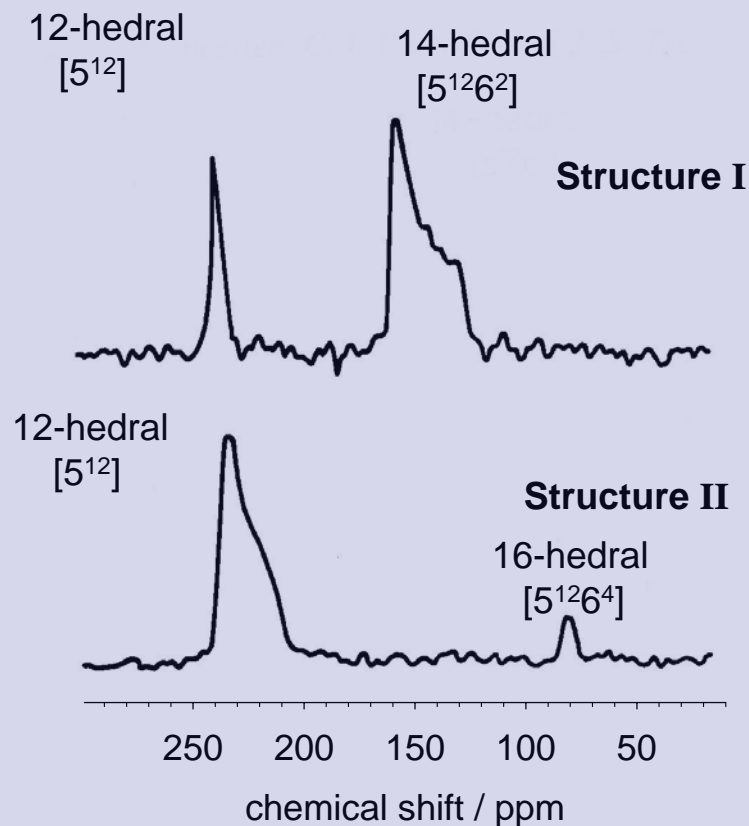
(b) 5^{12} cage
in structure I



There is a unique pair
of oxygen atoms in this cage,
defining a unique axis.
O-O distances differ from
Structure I cage by **$\sim 0.11 \text{ \AA}$**

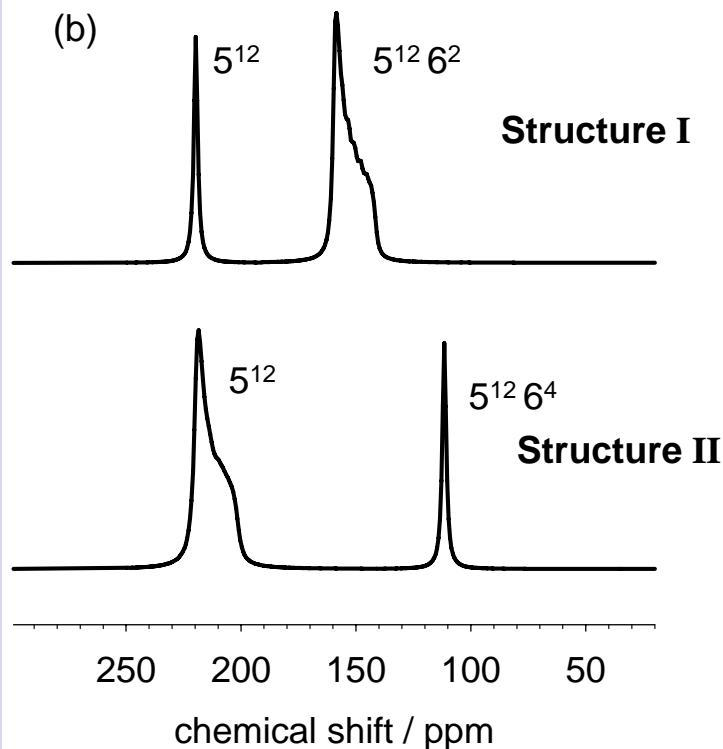
**Xe can sense and report
this difference!**

Xe in the cages of clathrate hydrates Structure I and II



EXPERIMENTS

J. A. Ripmeester, C. I. Ratcliffe and J. S. Tse,
Trans. Faraday Soc. 1, 84, 3731 (1988)

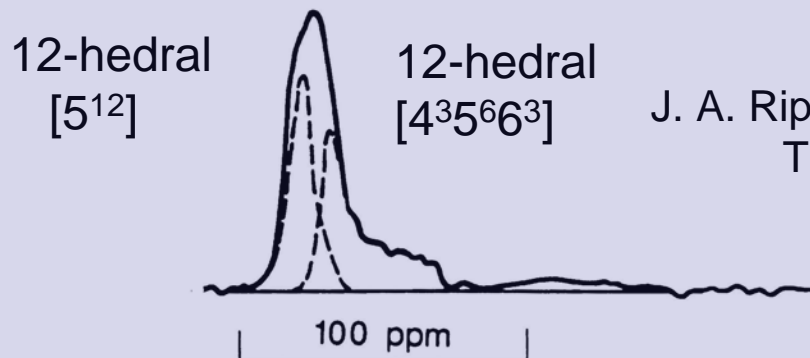


CALCULATIONS

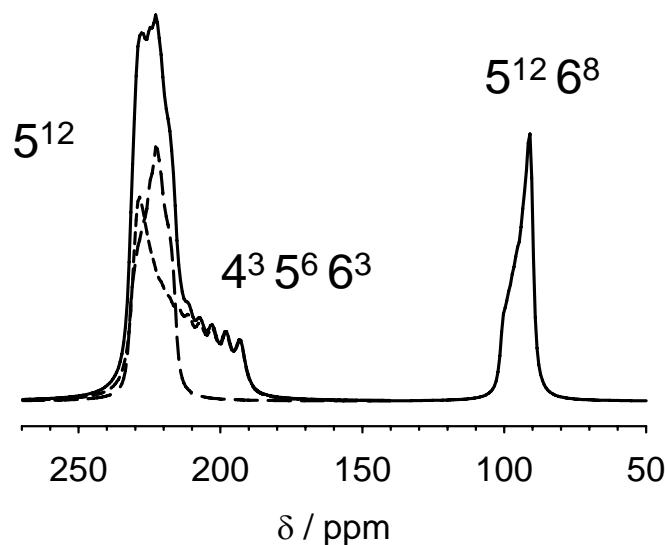
Monte Carlo simulations in a
4x4x4 supercell and 2x2x2 supercell
C. J. Jameson, D. Stueber, J Chem Phys 120,
10200 (2004)

Xe in clathrate hydrate Structure H

EXPERIMENT



J. A. Ripmeester, C. I. Ratcliffe and J. S. Tse,
Trans. Faraday Soc. 1, 84, 3731 (1988)

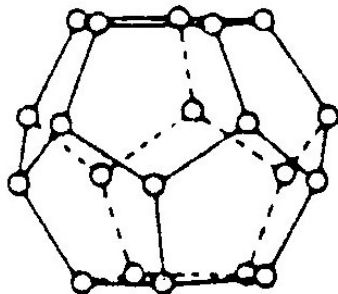


CALCULATIONS

Monte Carlo simulations
C. J. Jameson & D. Stueber, 2003

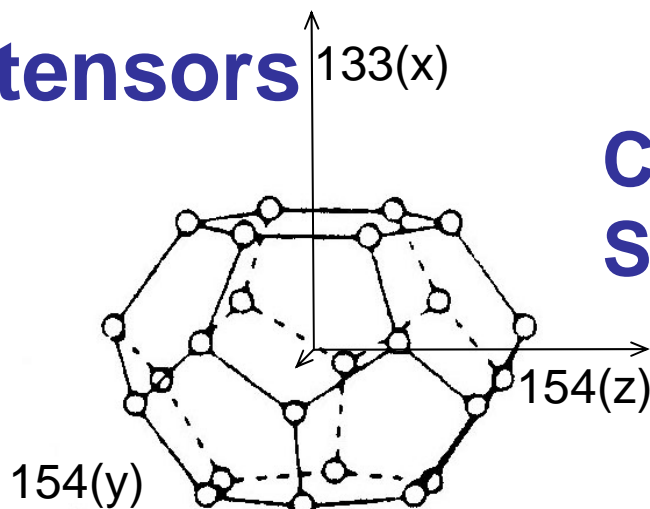
Xe chemical shift tensors

isotropic 214



5^{12}

symmetric

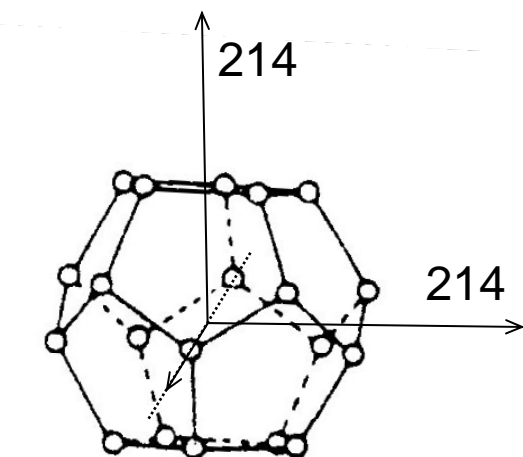


$5^{12}6^2$

axial, disk-like

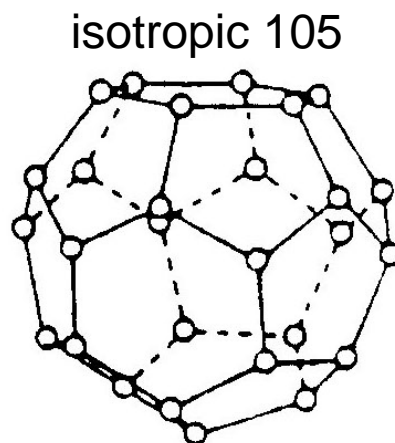
**Clathrate
Structure I**

from canonical
Monte Carlo
simulations



5^{12}

axial



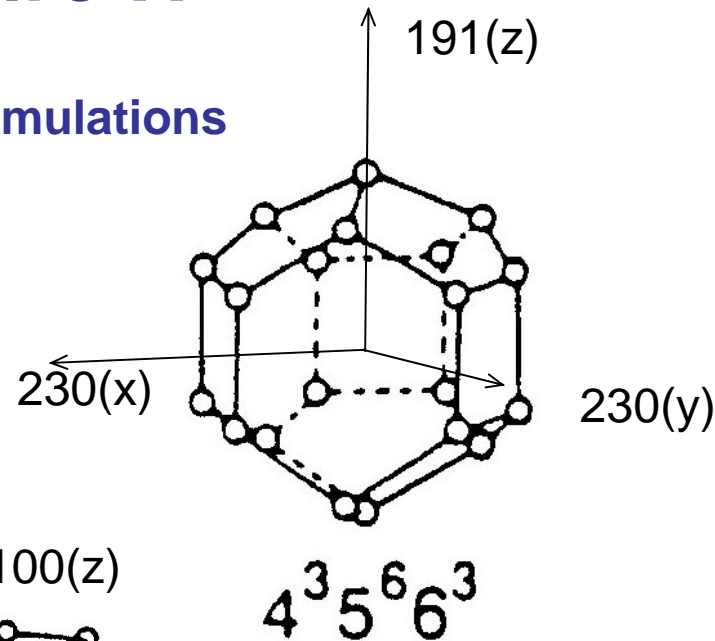
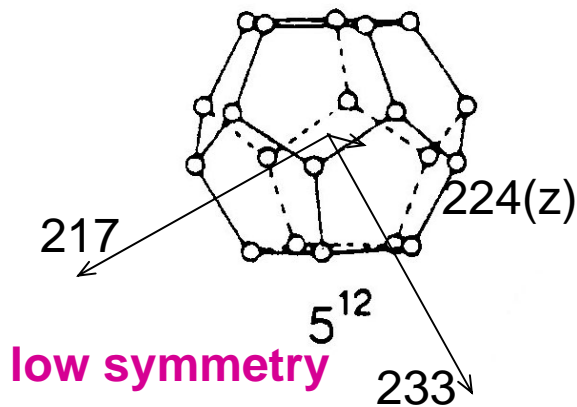
$5^{12}6^4$

symmetric

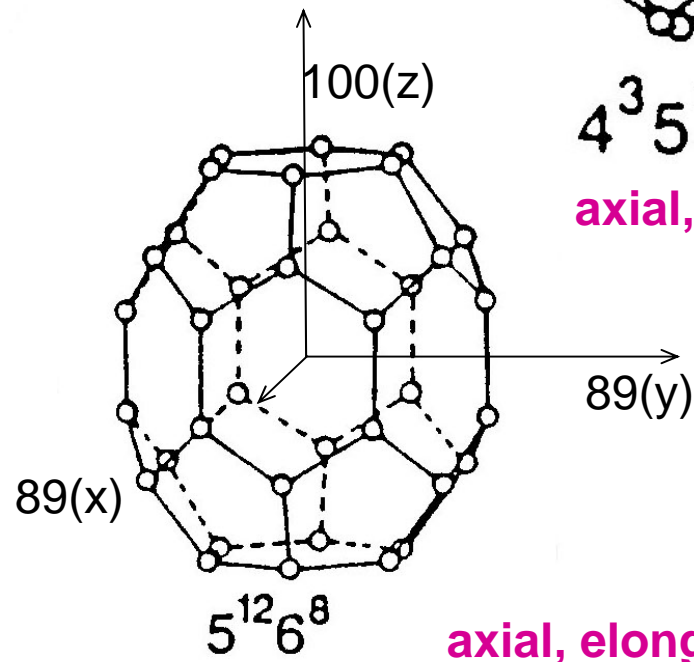
**Clathrate
Structure II**

Xe tensors in Clathrate Structure H

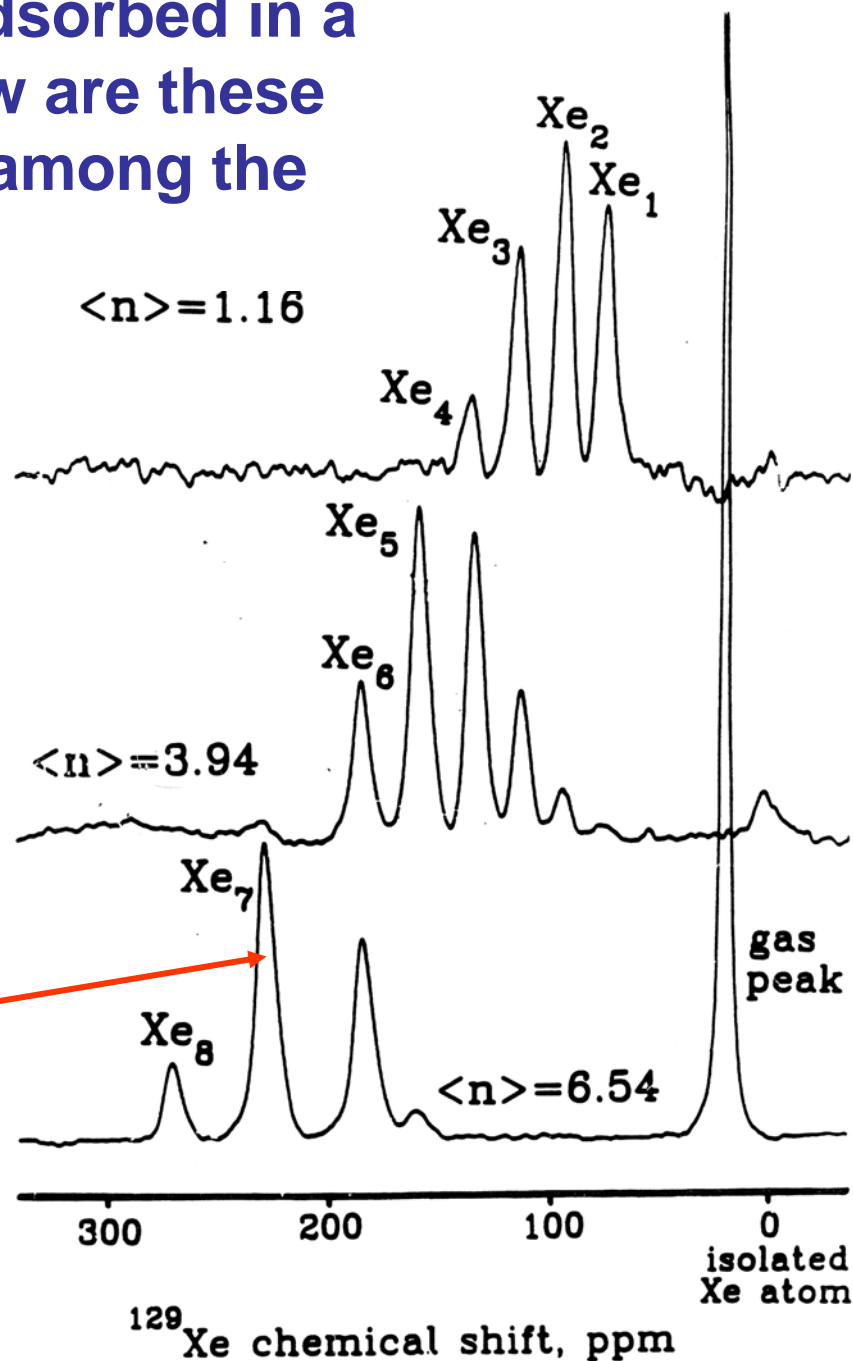
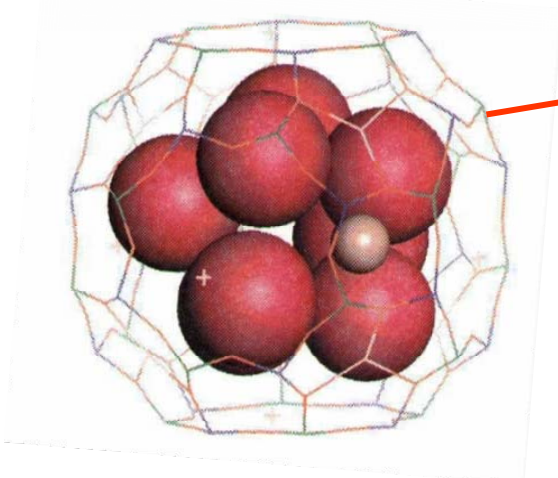
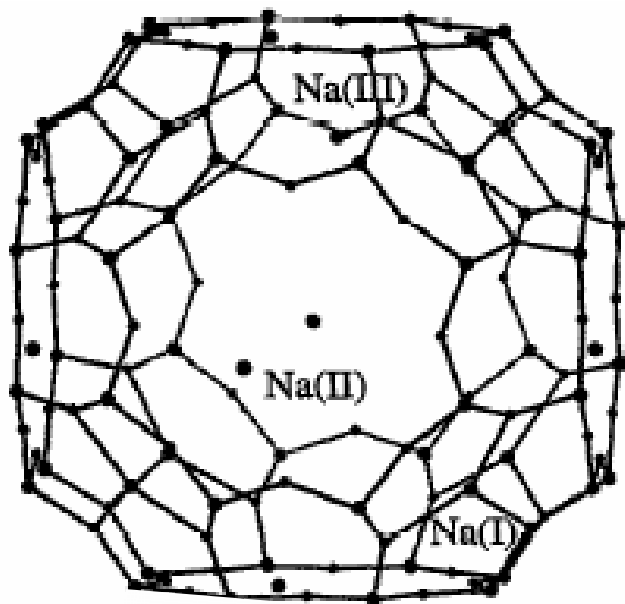
from canonical Monte Carlo simulations



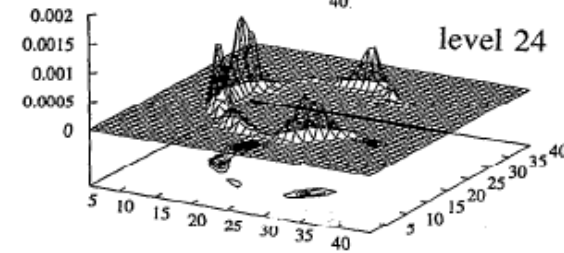
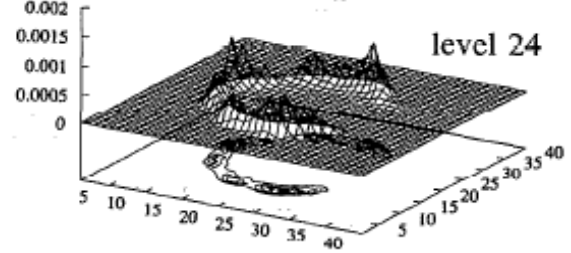
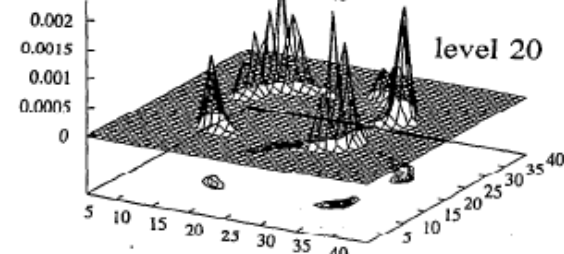
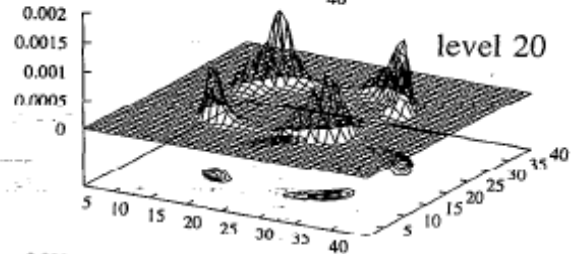
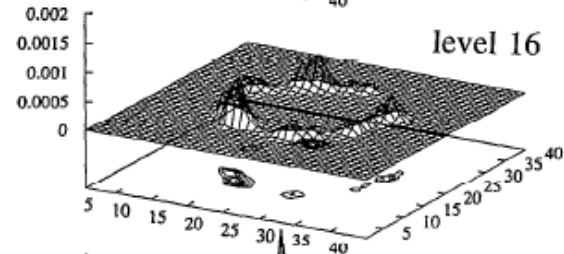
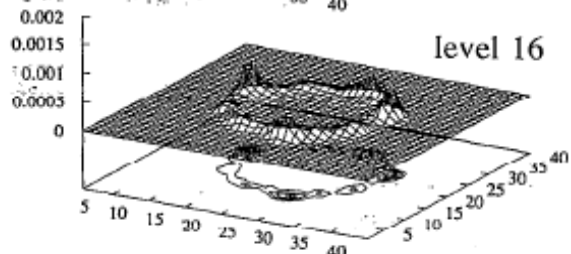
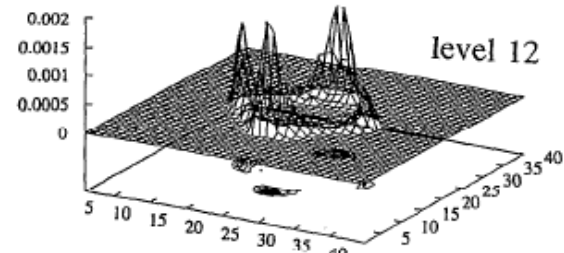
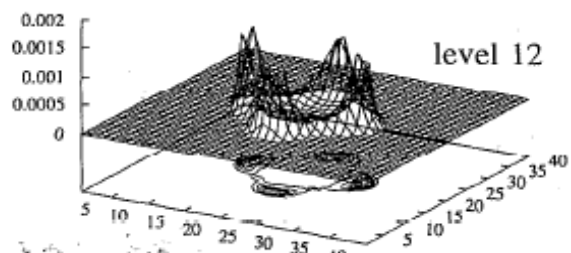
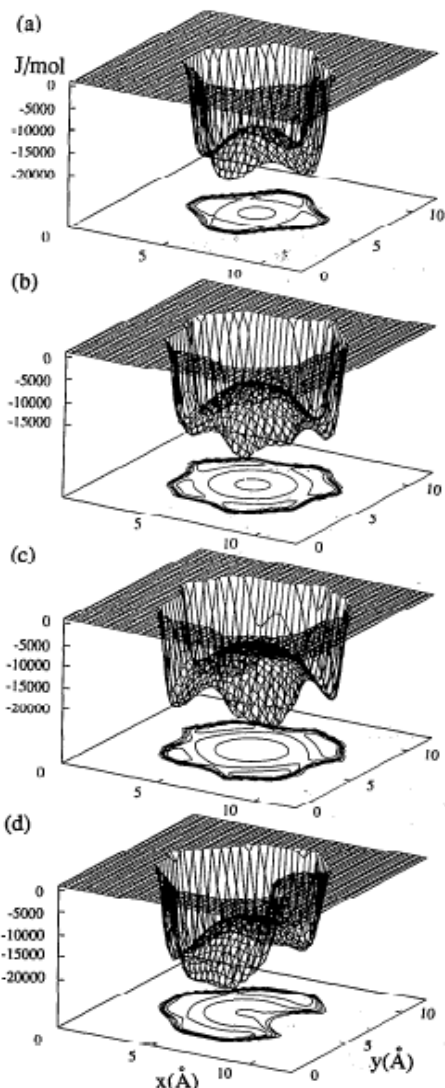
axial, squat



When molecules are adsorbed in a microporous solid, how are these molecules distributed among the cavities?



DISTRIBUTION of Xe ATOMS in a CAGE



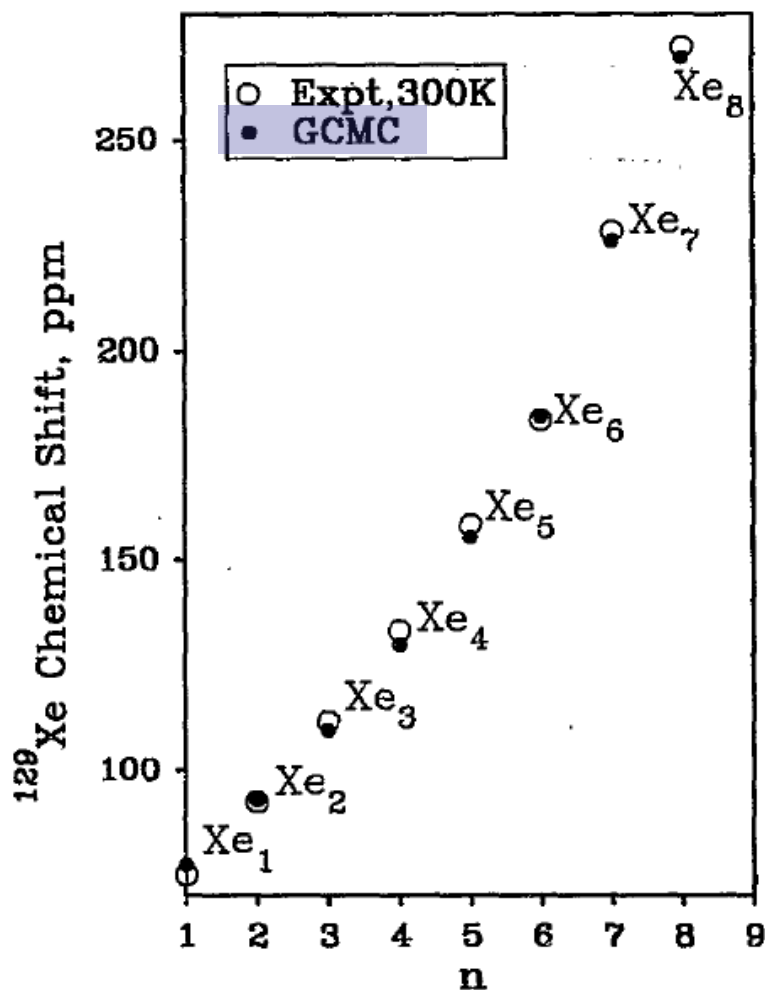
8 Xe in a cage

one Xe in a cage

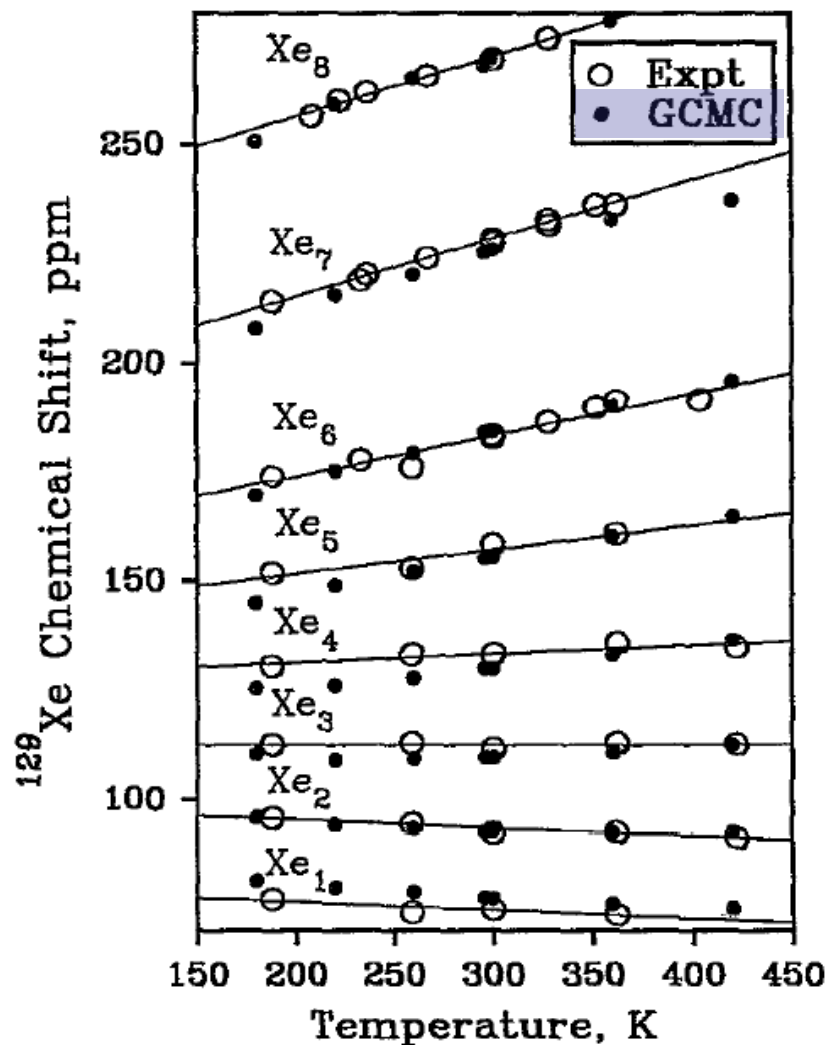
POTENTIAL
ENERGY

Probability of finding a Xe on a plane in a cage

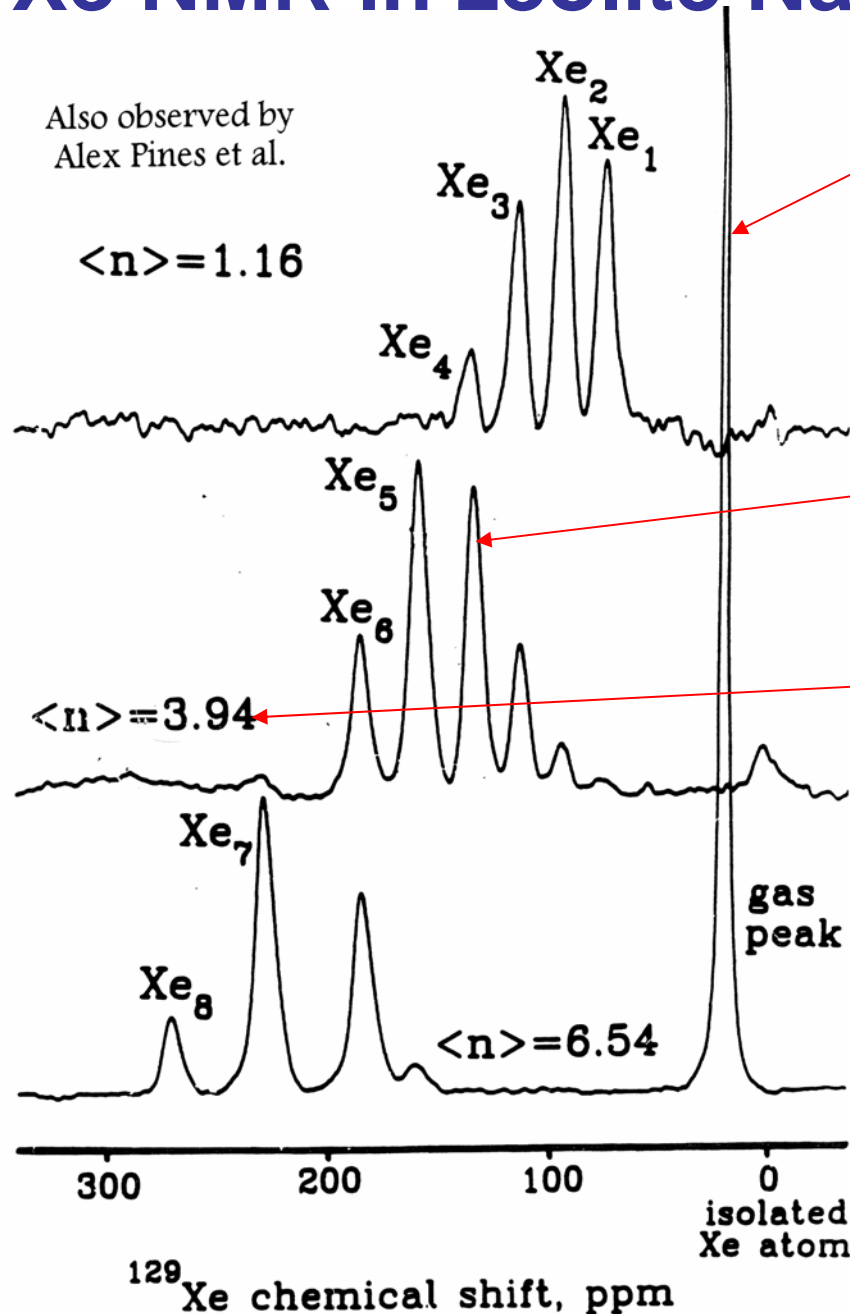
We reproduce the individual chemical shifts



and also the temperature dependence of each



Xe NMR in zeolite NaA

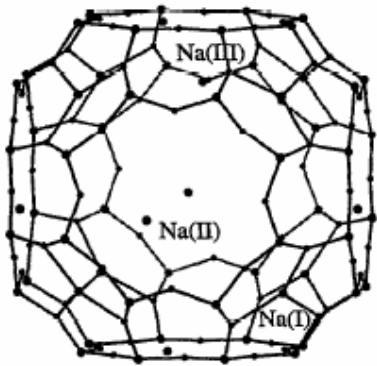


Xe chemical shift of gas peak provides ρ_{Xe} Xe density in the overhead bulk gas

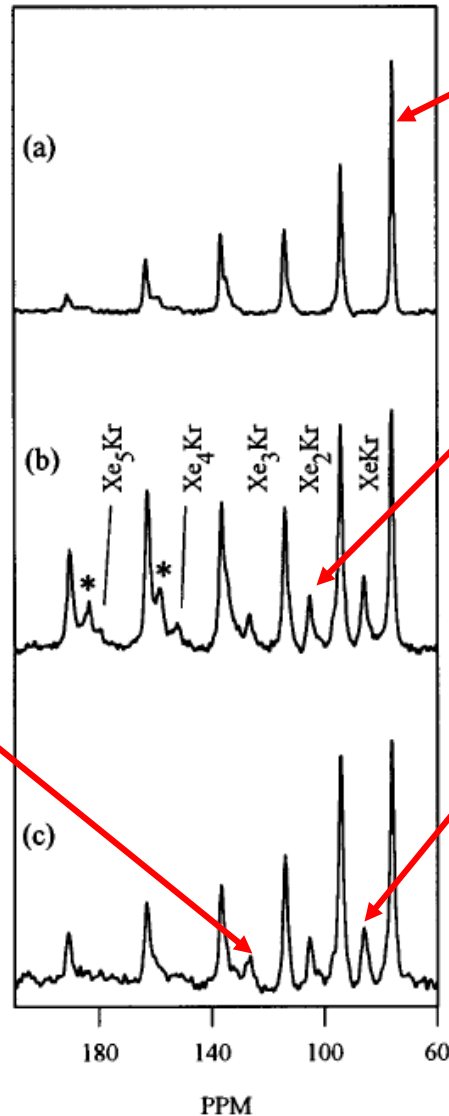
Relative areas under the peaks provides the fraction of cages containing a number n of Xe atoms and also the average $\langle n \rangle$. Adsorption isotherm by NMR!

Chemical shift of an individual peak can verify the GCMC *distribution of n Xe atoms within the cavity.*

Competitive Adsorption



three Xe+one Kr
in a cage



one Xe
in a cage

two Xe+one Kr
in a cage

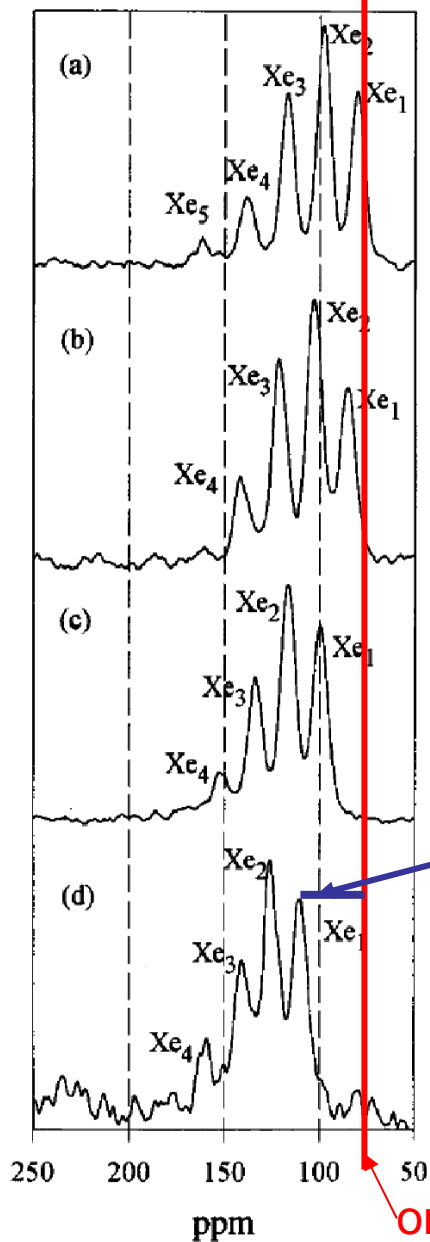
one Xe+ one Kr
in a cage

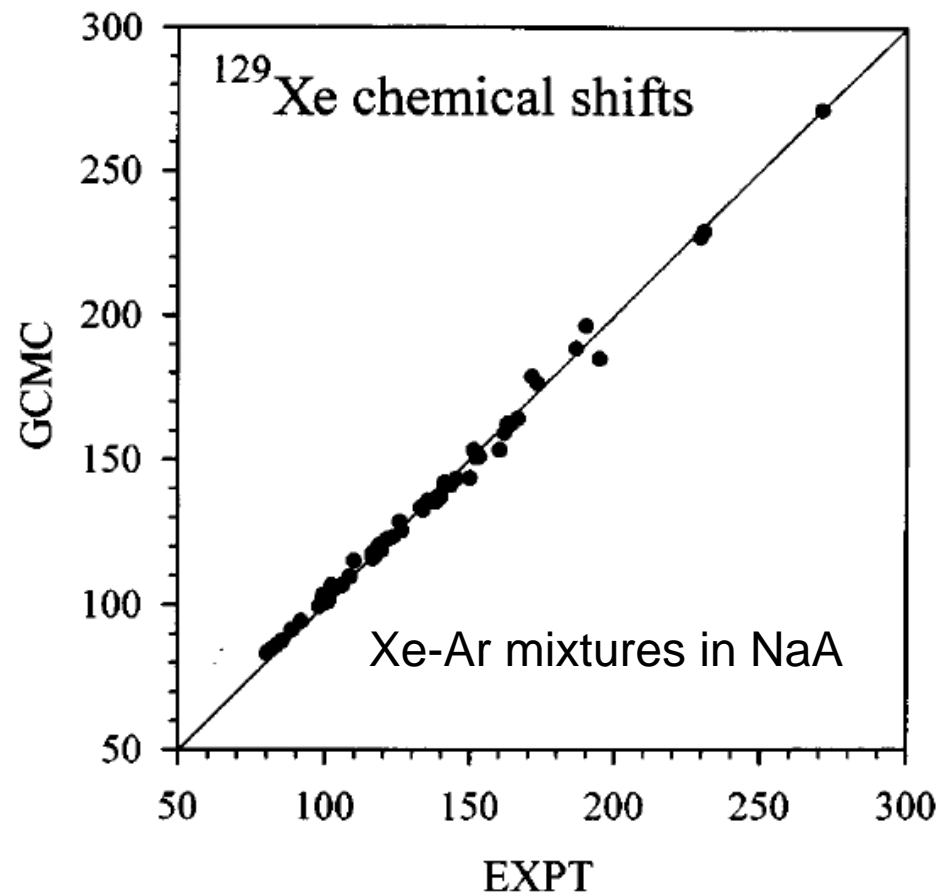
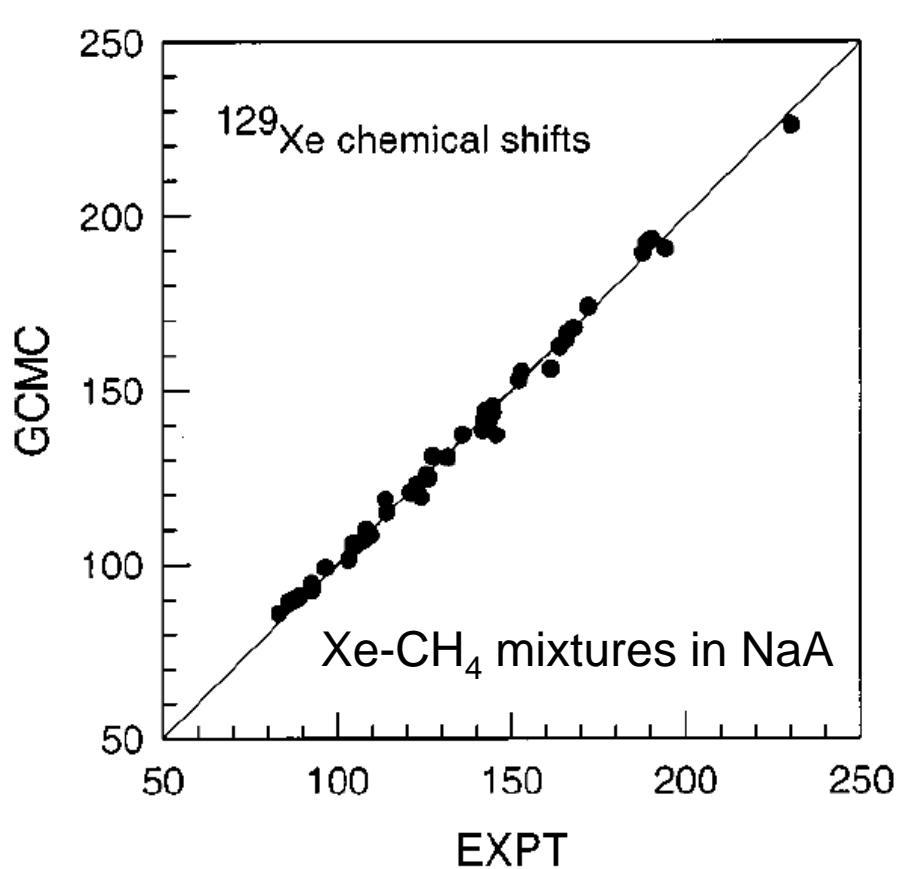
Xe NMR spectrum

The Xe chemical shift for Xe_n depends on the average number of Ar atoms in the same cage as n Xe atoms.

The INTENSITY of the Xe_n peak is a direct measure of the fraction of cages that have exactly n Xe atoms, as in pure Xe

Its shift from corresp peak in pure Xe/NaA gives the average number of Ar atoms in the same cage with it!



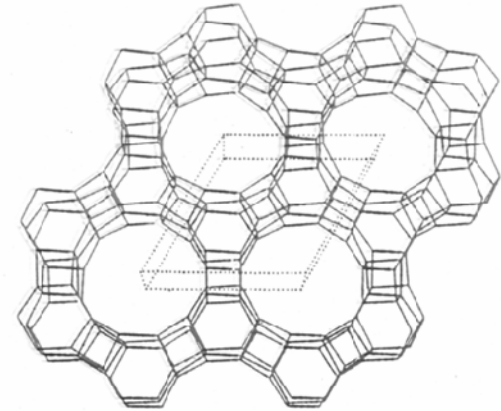


W can reproduce the Xe chemical shifts in all the samples of varying Xe- 'other' composition, thus, the average number of 'other' in the same cage as n Xe atoms is well represented by GCMC results.

Xe in nanochannels

QUESTION:

Is information about the architecture and constitution of the nanochannel encoded into the Xe NMR lineshape in polycrystalline samples?



- nature of geometric confinement, i. e., size and shape of the nanochannel or cavity
- electronic structure of the channel atoms

Xe shielding tensor in a channel in an external magnetic field (B_0) along direction (θ, ϕ) :

$$\sigma_{B0}(\theta, \phi) =$$

$$\sigma_{xx} \sin^2\theta \cos^2\phi + \sigma_{yy} \sin^2\theta \sin^2\phi + \sigma_{zz} \cos^2\theta + \\ \frac{1}{2}(\sigma_{xy} + \sigma_{yx}) \sin^2\theta \sin 2\phi + \frac{1}{2}(\sigma_{xz} + \sigma_{zx}) \sin 2\theta \cos\phi + \\ \frac{1}{2}(\sigma_{yz} + \sigma_{zy}) \sin 2\theta \sin\phi$$

one Xe tensor from interaction with ALL channel atoms

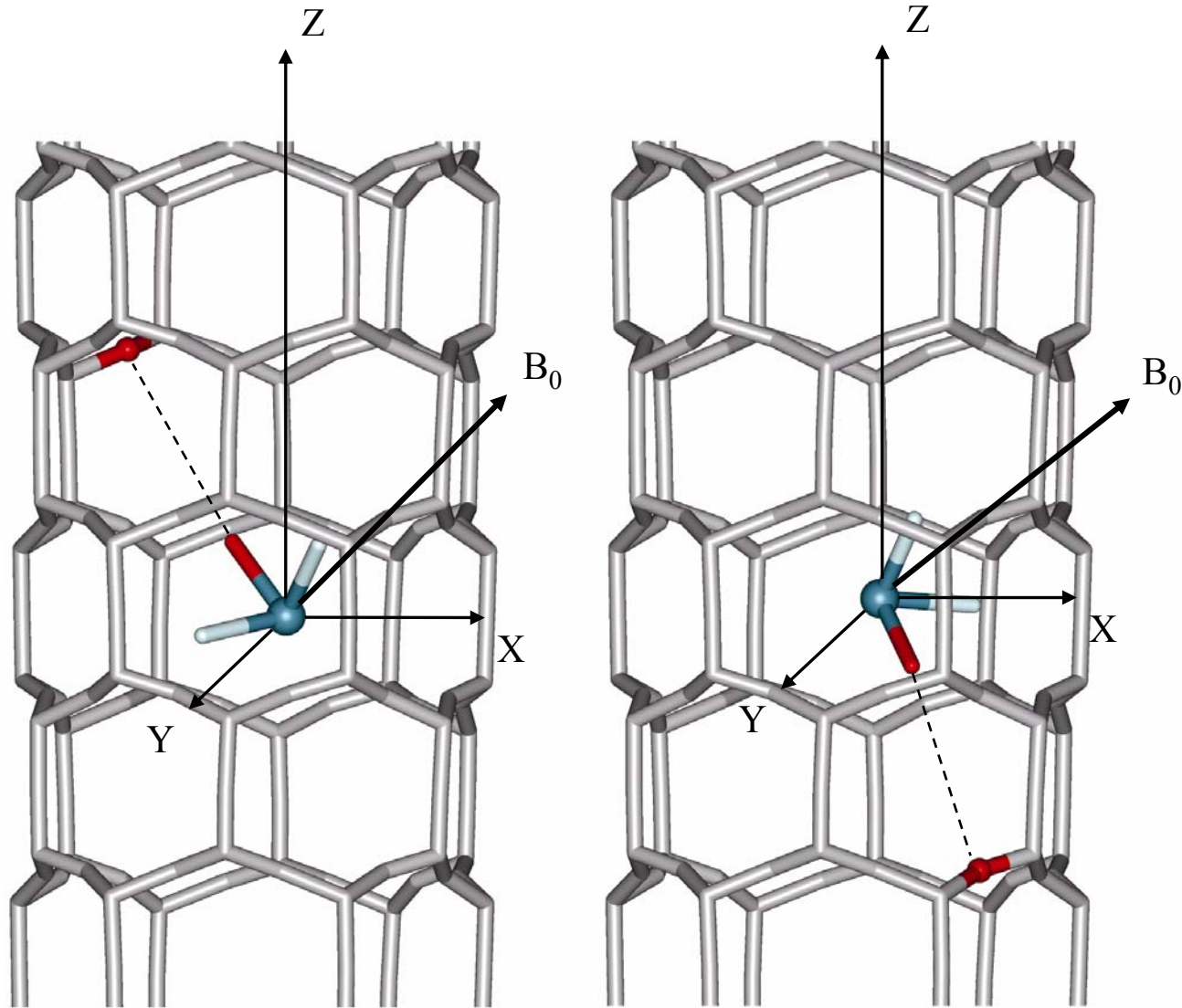
The dimer tensor model for Xe shielding tensor in the channel

The contribution to the shielding of Xe at point J due to i^{th} C or H atom of located at (x_i, y_i, z_i) is given by the tensor components for the Xe-C or Xe-H dimer, the functions $\sigma_{\perp}(r_{\text{XeC/H}})$, $\sigma_{||}(r_{\text{XeC/H}})$.

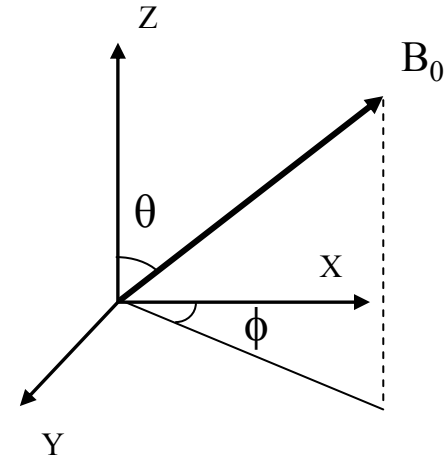
$$\sigma_{XX} = [(x_i - x_J)/r_{iJ}]^2 \sigma_{||} + \{[(y_i - y_J)/r_{iJ}]^2 + [(z_i - z_J)/r_{iJ}]^2\} \sigma_{\perp}$$

$$\frac{1}{2}(\sigma_{XY} + \sigma_{YX}) = [(x_i - x_J)/r_{iJ}] \cdot [(y_i - y_J)/r_{iJ}] (\sigma_{||} - \sigma_{\perp})$$

Lineshapes by grand canonical Monte Carlo



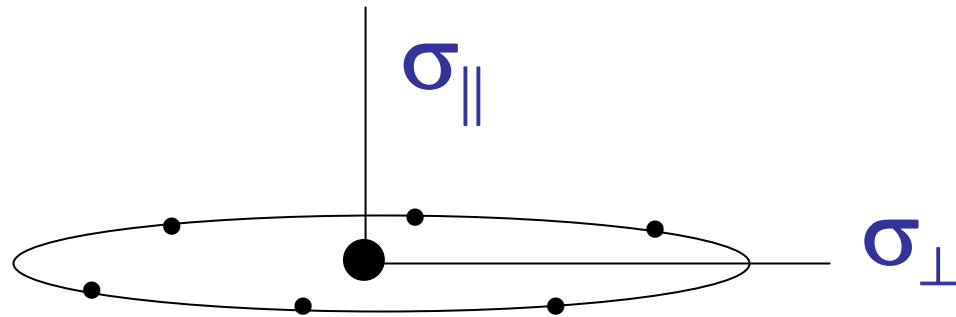
Consider one Xe-O at a time
(and one Xe-Xe at a time)



Random orientation of
crystallites:
Probability that B_0 lies
in any infinitesimal
solid angle is
 $d\zeta d\phi / 4\pi$, where
 $\zeta = (-\cos\theta)$
Equal areas in $\zeta\phi$
plane correspond to
equal probabilities

Are Xe shielding tensor components pairwise additive?

Example:



Xe in the center of a ring of Ne atoms

The dimer tensor model for Xe shielding tensor in a Ne channel

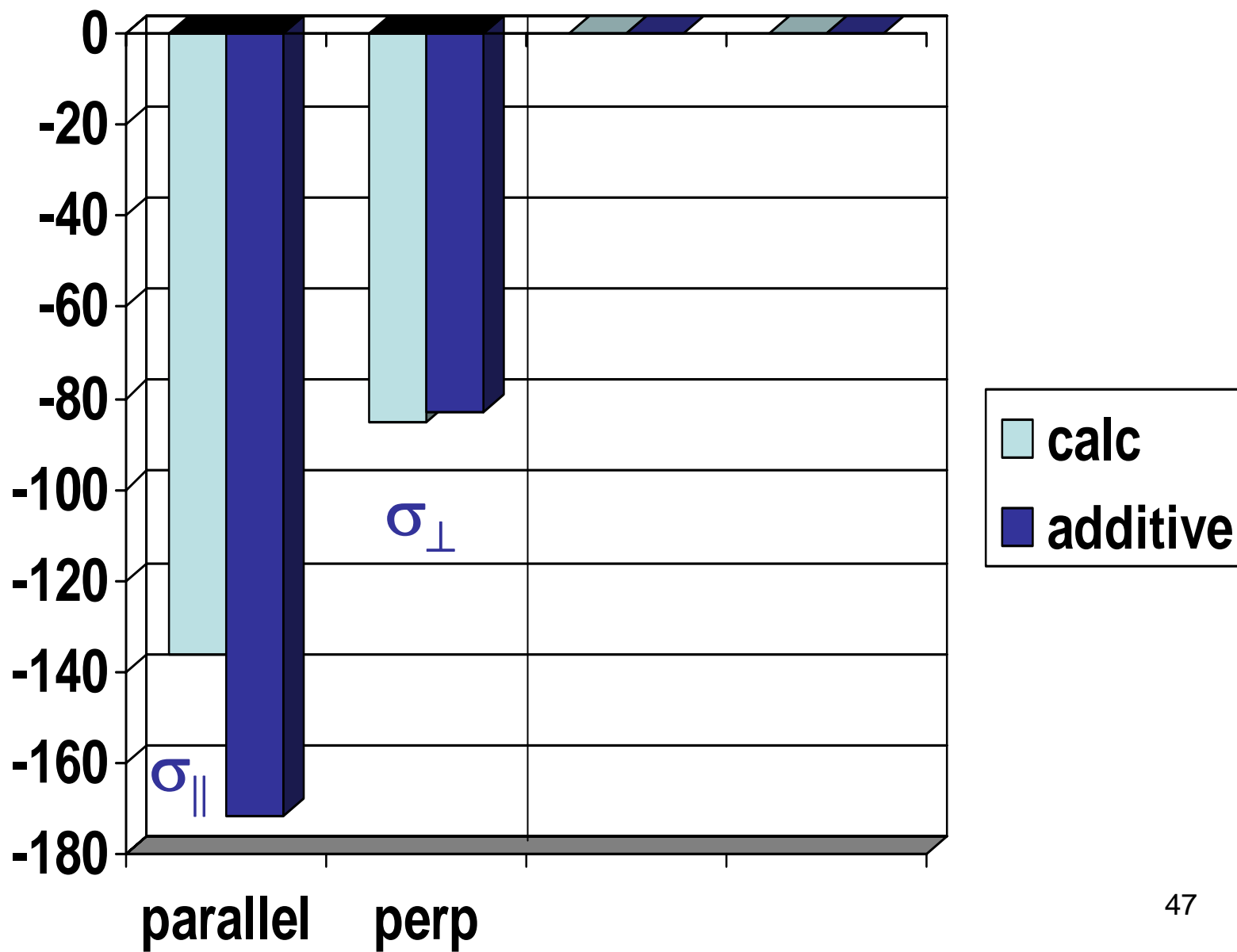
The contribution to the shielding of Xe at point J due to i_{th} Ne atom located at (x_i, y_i, z_i) is given by the ab initio tensor components for the XeNe dimer, the functions $\sigma_{\perp}(r_{XeNe})$, $\sigma_{||}(r_{XeNe})$.

$$\sigma_{XX} = [(x_i - x_J)/r_{iJ}]^2 \sigma_{||} + \{[(y_i - y_J)/r_{iJ}]^2 + [(z_i - z_J)/r_{iJ}]^2\} \sigma_{\perp}$$

$$\frac{1}{2}(\sigma_{XY} + \sigma_{YX}) = [(x_i - x_J)/r_{iJ}] \cdot [(y_i - y_J)/r_{iJ}] (\sigma_{||} - \sigma_{\perp})$$

The contribution to the shielding of Xe at point J due to the K_{th} Xe atom located at (x_K, y_K, z_K) is given by the ab initio tensor components for the XeXe dimer, the functions $\sigma_{\perp}(r_{XeXe})$, $\sigma_{||}(r_{XeXe})$.

Xe@Ne₆ small ring
 $r = 3 \text{ \AA}$

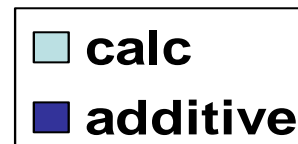
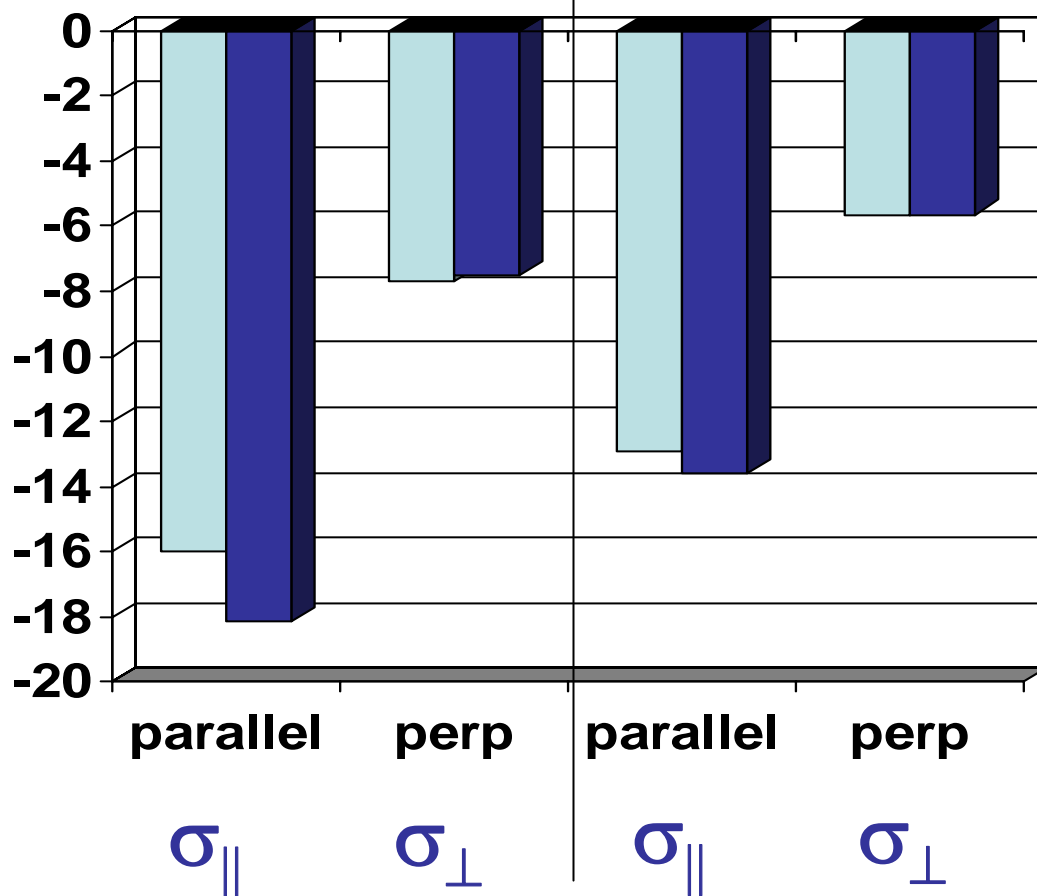


larger ring

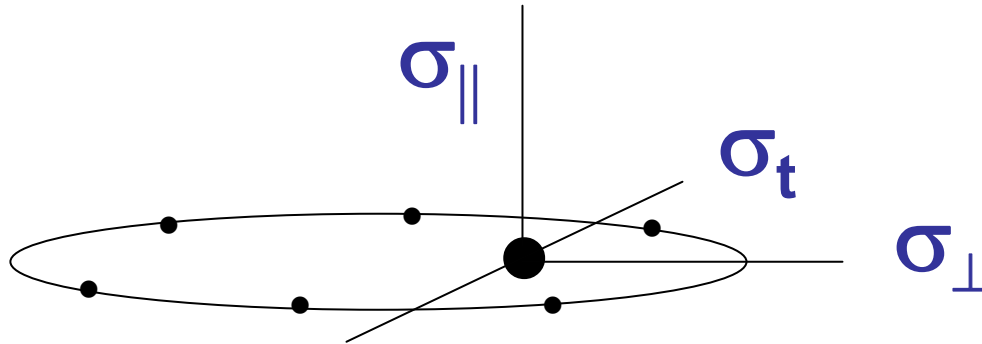
Xe@Ne_8
 $r = 4 \text{ \AA}$

Xe@Ne_6
 $r = 4 \text{ \AA}$

ppm
relative
to
isolated
Xe
atom



Xe off-center in the larger ring of Ne atoms

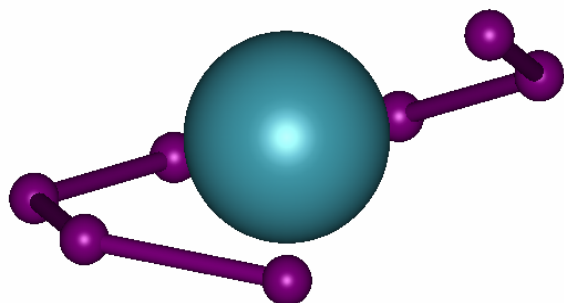


Model	r_{ring} Å	R_{Xe} Å	σ_{\parallel}	σ_{\perp}	σ_t
Xe@Ne ₆	4.0	1.0	-40.04	-11.13	-28.86
$\sum_i^6 \text{XeNe}_i$	4.0	1.0	-43.18	-11.45	-29.00
Xe@Ne ₈	4.0	1.0	-47.67	-18.39	-35.48
$\sum_i^8 \text{XeNe}_i$	4.0	1.0	-57.20	-18.69	-34.83

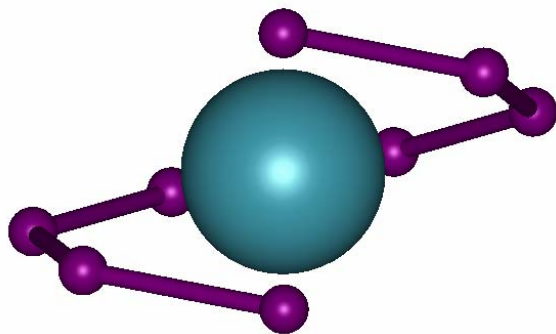
↑
large deviation

The shielding tensor of Xe interacting with Ne helices

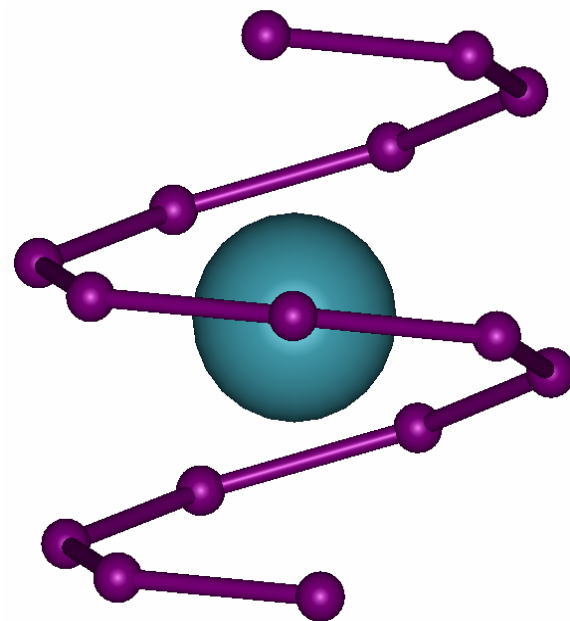
Xe in a left handed helix



Xe@Ne_7



Xe@Ne_8



Xe@Ne_{15}

Are Xe shielding tensor components pairwise additive?

Xe@Ne ₇ (L)	ab initio	dimer tensor model	diff
σ_{XX}	-55.4526	-55.3409	-0.11
σ_{YY}	-52.2268	-52.1340	-0.09
σ_{ZZ}	-86.6174	-98.1004	11.48
$\frac{1}{2}(\sigma_{XY} + \sigma_{YX})$	-0.0948	0.0000	-0.09
$\frac{1}{2}(\sigma_{XZ} + \sigma_{ZX})$	-2.8110	-3.2641	0.45
$\frac{1}{2}(\sigma_{YZ} + \sigma_{ZY})$	12.7147	15.4706	-2.76
σ_{iso}	-64.7656	-68.5253	3.76

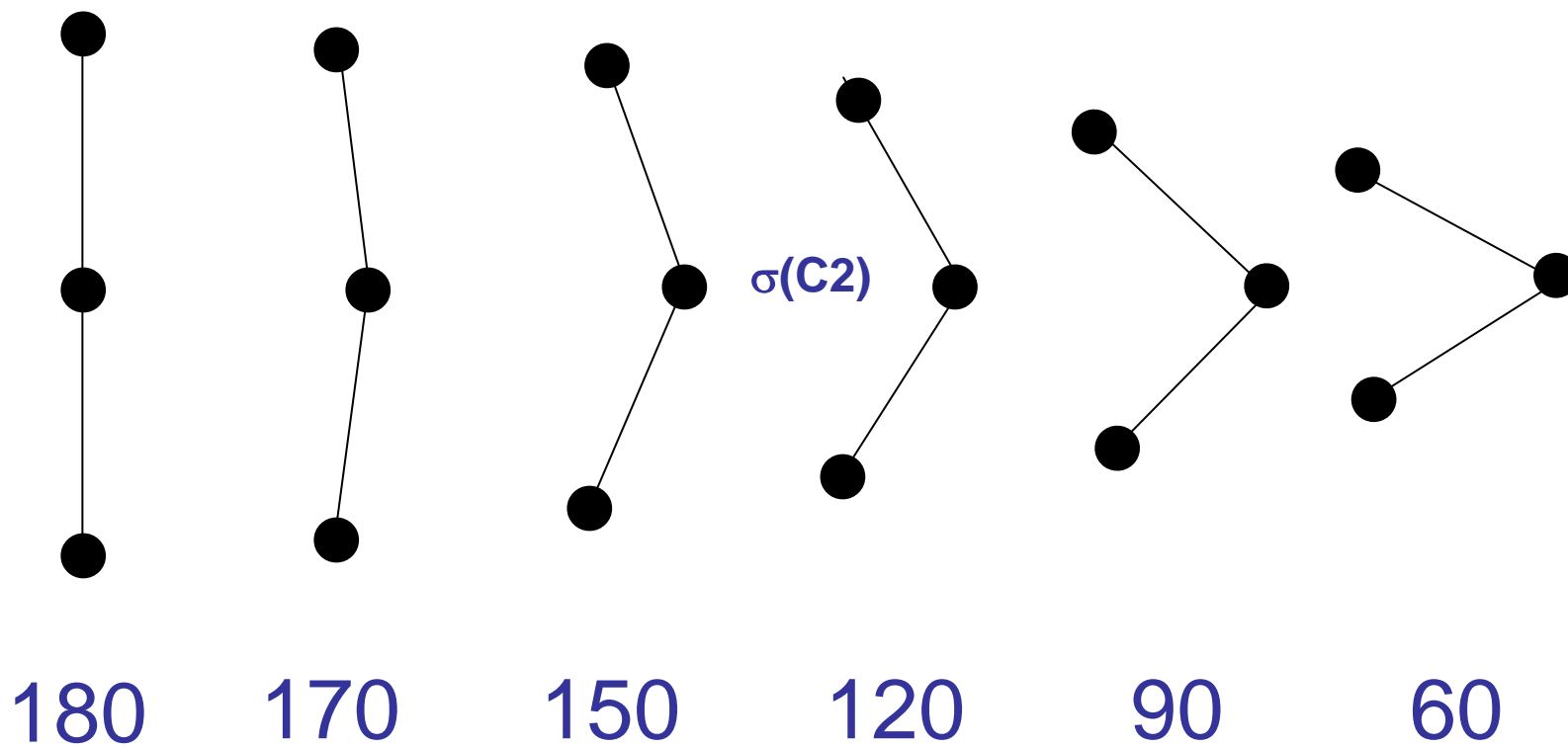
Are Xe shielding tensor components pairwise additive?

$\text{Xe@Ne}_8(\text{L})$	ab initio	dimer tensor model	diff
σ_{XX}	-56.4270	-56.5864	0.16
σ_{YY}	-59.0700	-59.4600	0.39
σ_{ZZ}	-91.2691	-103.6742	12.41
$\frac{1}{2}(\sigma_{\text{XY}} + \sigma_{\text{YX}})$	0.0000	0.0000	0.00
$\frac{1}{2}(\sigma_{\text{XZ}} + \sigma_{\text{ZX}})$	0.0000	0.0000	0.00
$\frac{1}{2}(\sigma_{\text{YZ}} + \sigma_{\text{ZY}})$	12.5036	15.4706	-2.97
σ_{iso}	-68.9221	-73.2404	4.32

Are Xe shielding tensor components pairwise additive?

$\text{Xe@Ne}_{15}(\text{L})$	ab initio	dimer tensor model	diff
σ_{XX}	-64.8244	-66.4863	1.66
σ_{YY}	-65.1560	-66.6497	1.49
σ_{ZZ}	-97.4705	-111.0832	13.61
$\frac{1}{2}(\sigma_{\text{XY}} + \sigma_{\text{YX}})$	-0.1955	-0.1000	-0.10
$\frac{1}{2}(\sigma_{\text{XZ}} + \sigma_{\text{ZX}})$	3.3079	4.2987	-0.99
$\frac{1}{2}(\sigma_{\text{YZ}} + \sigma_{\text{ZY}})$	6.7964	8.9260	-2.13
σ_{iso}	-75.8170	-81.4067	5.59

three Xe atoms



central Xe in Xe₃ $r_{\text{Xe-Xe}} = 4.0 \text{ \AA}$ (shorter)

	σ_{\perp}	$\sigma_{(\text{C2})}$	$\sigma_{(\perp \text{ to C2})}$
$\alpha = 180^\circ$	-204.72	-204.72	+5.17
<i>if additive</i>	-202.38	-202.38	+5.06
<i>dev</i>	-2.3	-2.3	-0.1
$\alpha = 170^\circ$	-204.79	-203.04	+3.62
<i>if additive</i>	-202.38	-200.80	+3.48
<i>dev</i>	-2.3	+2.2	-0.1
$\alpha = 150^\circ$	-205.23	-190.17	-8.52
<i>if additive</i>	-202.38	-188.50	-8.84
<i>dev</i>	+2.8	+2.0	-0.3
$\alpha = 120^\circ$	-204.32	-151.04	-46.32
<i>if additive</i>	-202.38	-150.52	-46.80
<i>dev</i>	+1.9	+0.5	-0.5

central Xe in Xe₃ $r_{\text{Xe-Xe}} = 4.4 \text{ \AA}$ (longer)

	σ_{\perp}	$\sigma_{(\text{C}2)}$	$\sigma_{(\perp \text{ to C}2)}$
$\alpha = 180^\circ$	-81.89	-81.89	+3.88
<i>if additive</i>	-81.58	-81.58	+3.88
<i>dev</i>	+0.3	+0.3	0.0
$\alpha = 170^\circ$	-81.91	-81.21	+3.23
<i>if additive</i>	-81.58	-80.93	+3.23
<i>dev</i>	+0.3	+0.3	0.0
$\alpha = 150^\circ$	-82.00	-76.04	-1.84
<i>if additive</i>	-81.58	-75.86	-1.84
<i>dev</i>	+0.4	+0.2	0.0
$\alpha = 120^\circ$	-81.81	-60.29	-17.44
<i>if additive</i>	-81.58	-60.22	-17.48
<i>dev</i>	+0.2	+0.1	0.0

central Xe in Xe₃ $r_{\text{Xe-Xe}} = 4.4 \text{ \AA}$

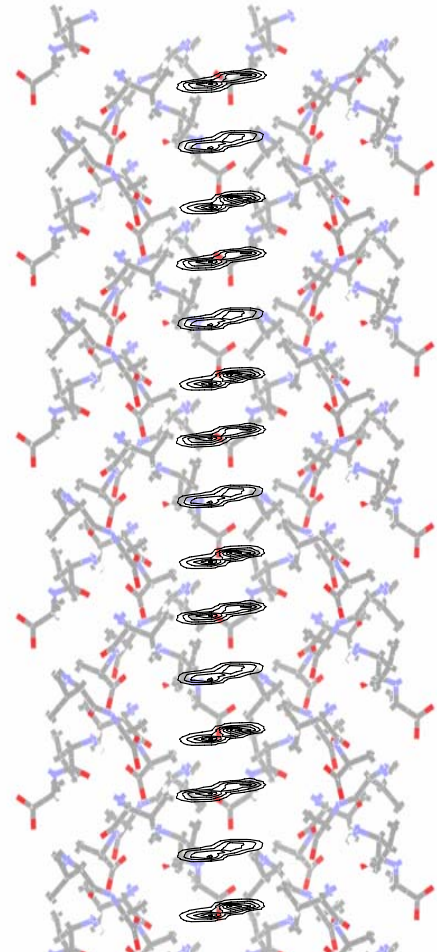
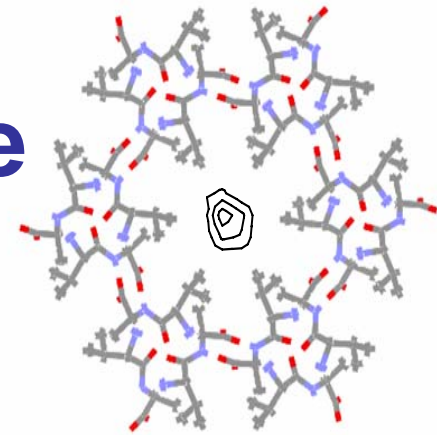
	σ_{\perp}	$\sigma_{(\text{C}2)}$	$\sigma_{(\perp \text{ to C}2)}$
$\alpha = 90^\circ$	-79.89	-38.87	-38.87
<i>if additive</i>	-81.58	-38.85	-38.85
<i>dev</i>	-1.7	0.0	0.0
$\alpha = 60^\circ$	-70.05	-17.89	-58.51
<i>if additive</i>	-81.58	-17.48	-60.22
<i>dev</i>	-11.5	0.4	-1.7

↑
in the molecular plane, the
electrons of terminal Xe atoms
interacting substantially for 60°

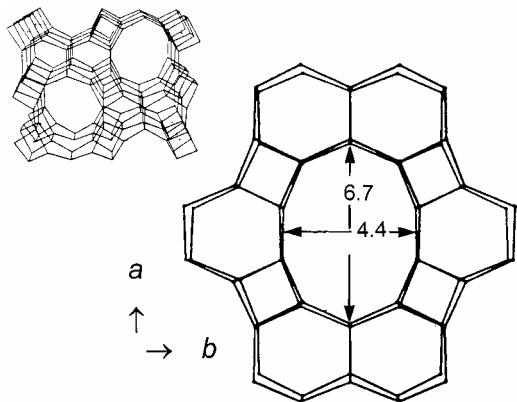
Xe distribution in the material, i.e., where does Xe spend time?

The one-body distribution function shows the probability of finding a Xe atom as a function of position within the channel

Xe in VA
from GCMC
simulations



Architecture of the channel determines the Xe lineshape

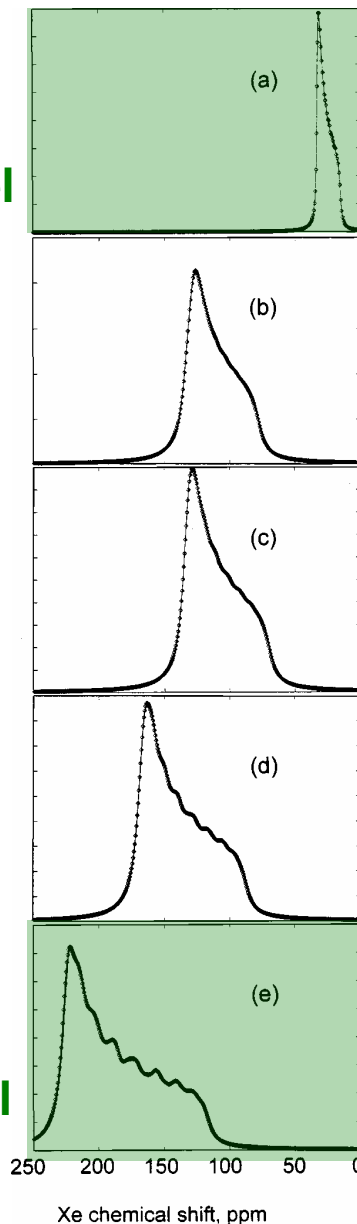


ALPO₄-11
architecture

One Xe atom
in a **neon channel**

Electronic structure
of the channel
atoms
determines the
isotropic chemical
shift
and width at zero-
loading

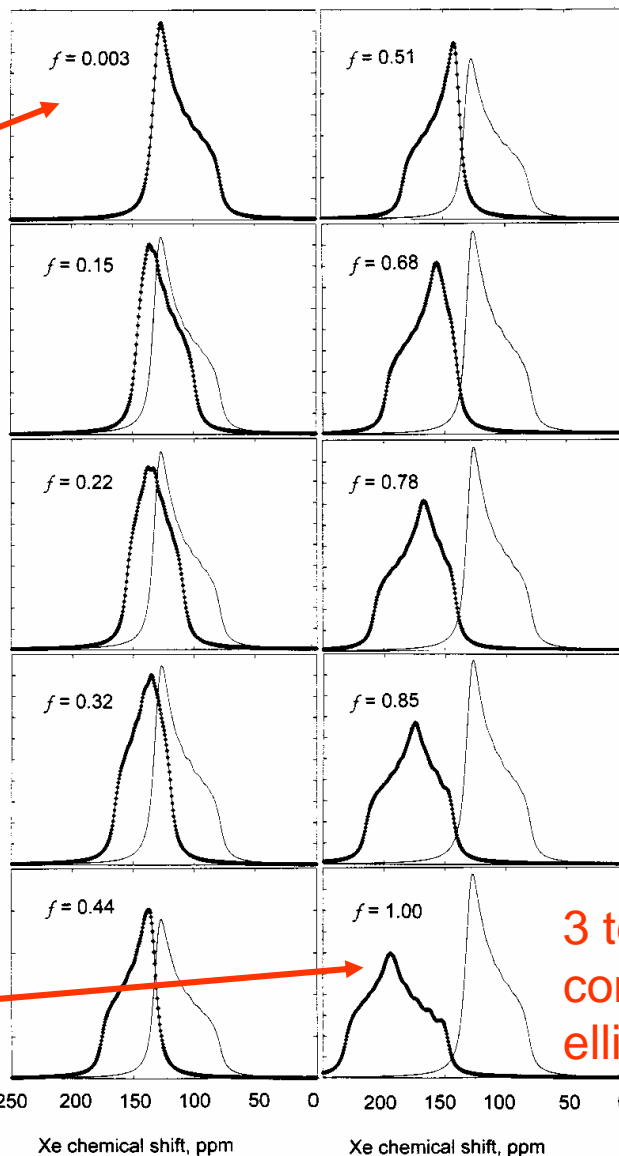
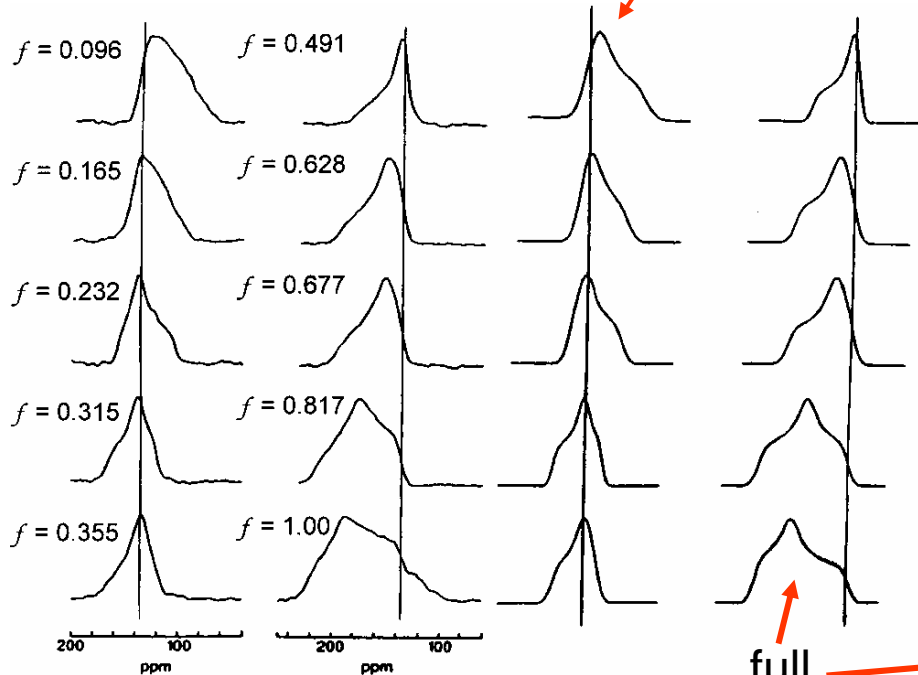
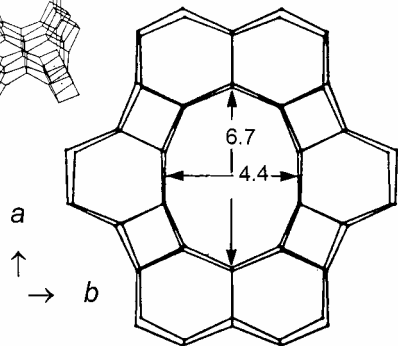
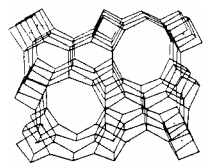
One Xe atom
in an **argon channel**



Jameson,
JCP 116,
8912 (2002)

Xe in the channels of ALPO₄-11

Grand Canonical Monte Carlo **SIMULATIONS**



Jameson
J Chem
Phys 116,
8912
(2002)

3 tensor
components
ellipticity

EXPERIMENTS

J.A. Ripmeester and C.I. Ratcliffe,
J. Phys. Chem. 99, 619 (1995)

dipeptides

L-Val-L-Ala

VA

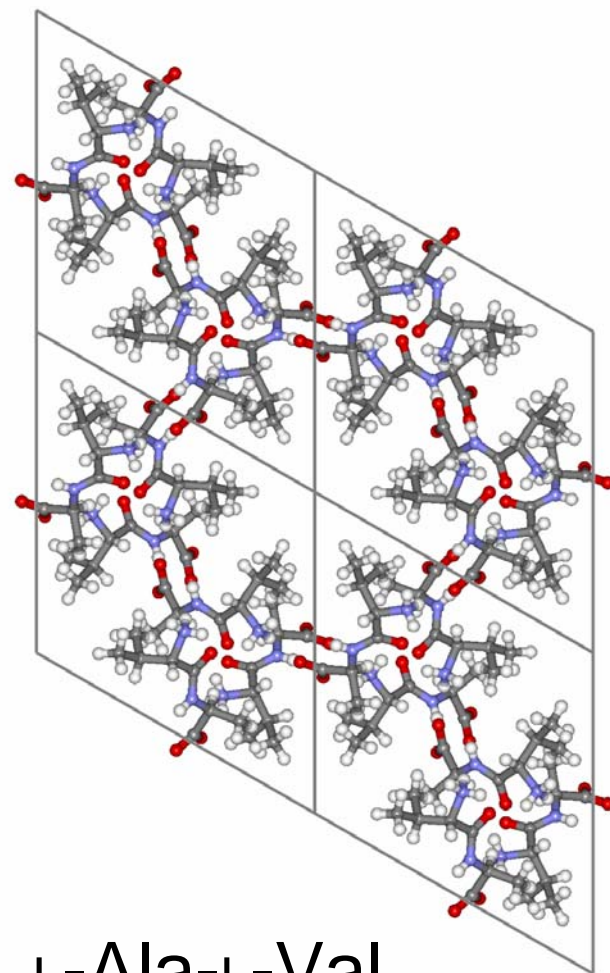
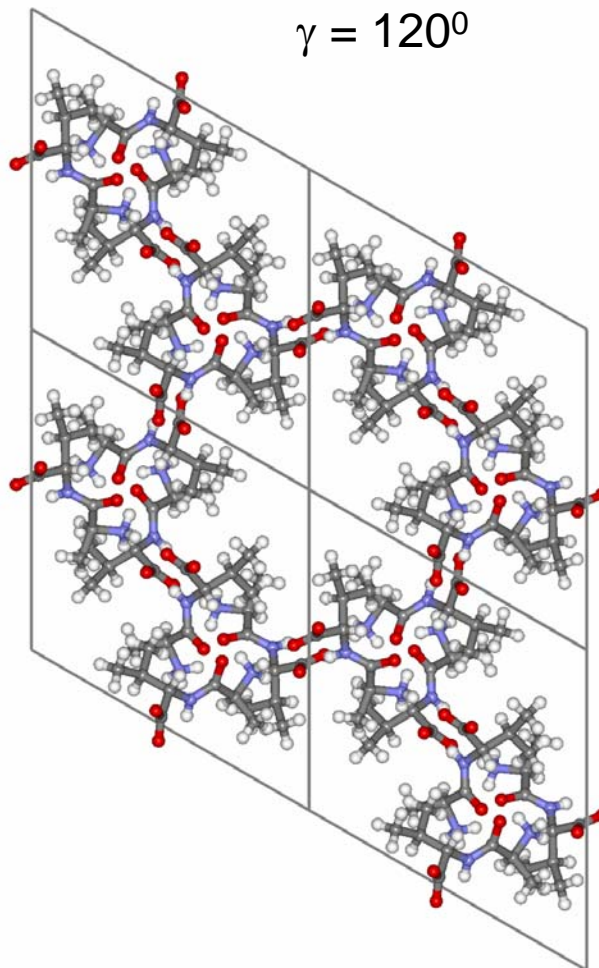
P61

$a = b = 14.461 \text{ \AA}$

$c = 10.083 \text{ \AA}$

$\alpha = \beta = 90^\circ$

$\gamma = 120^\circ$



L-Ala-L-Val

AV

P61

$a = b = 14.462 \text{ \AA}$

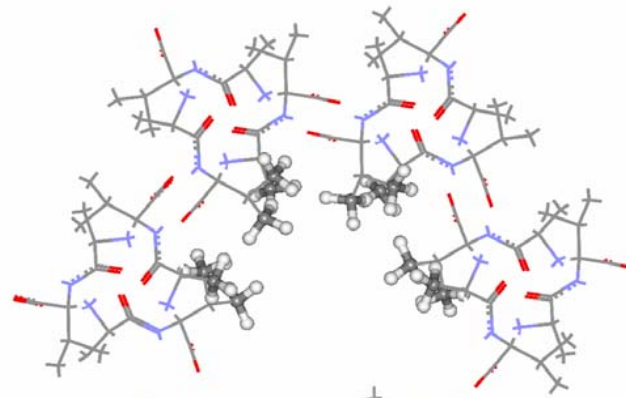
$c = 10.027 \text{ \AA}$

$\alpha = \beta = 90^\circ$

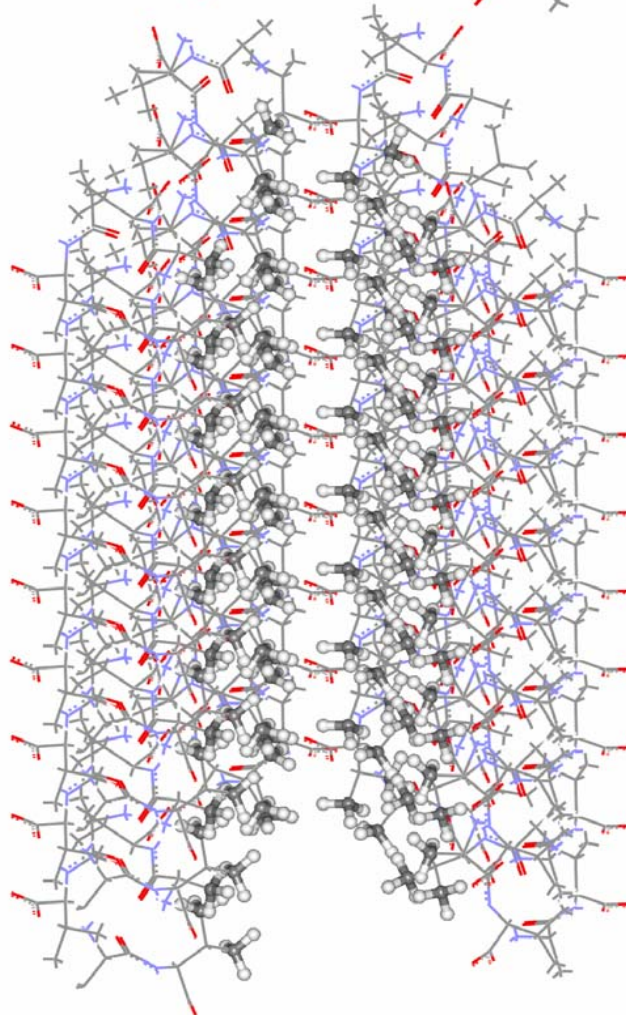
$\gamma = 120^\circ$

- From the perspective of the Xe only the side chain methyl groups are accessible

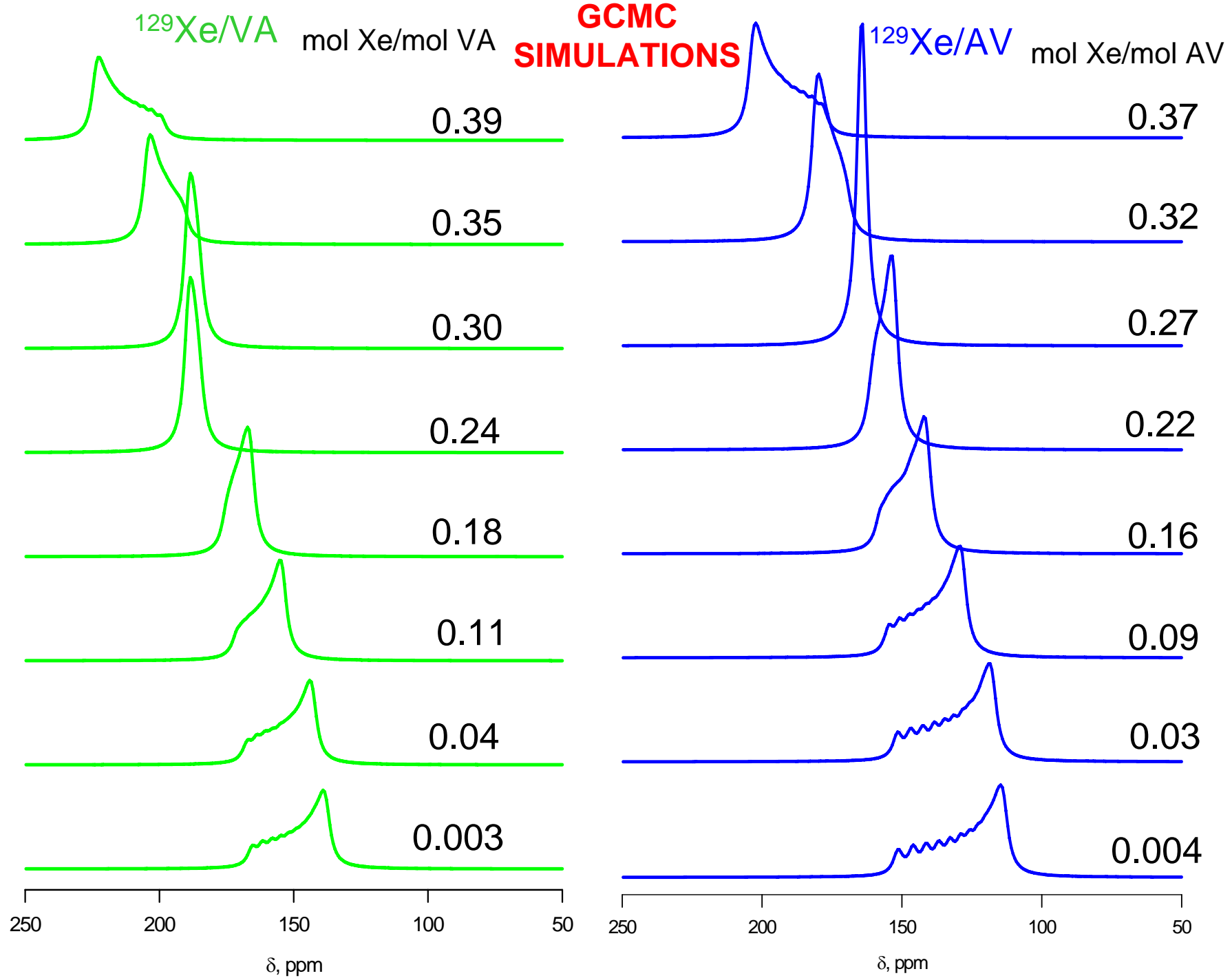
- Can we use the Xe- CH_4 shielding response surface and potential energy surface for our simulations?



Top view

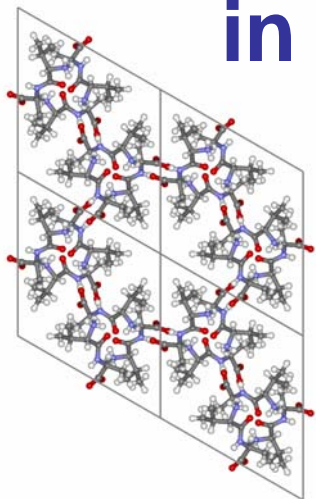


Tilted view



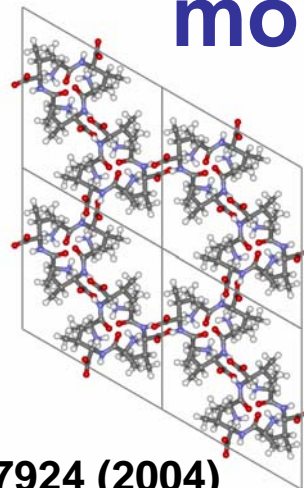
in channels of

molecular crystals



L-Val-L-Ala

VA



L-Ala-L-Val

AV

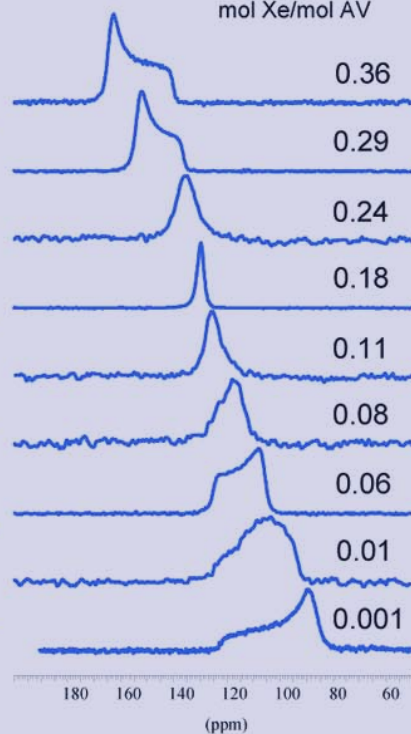
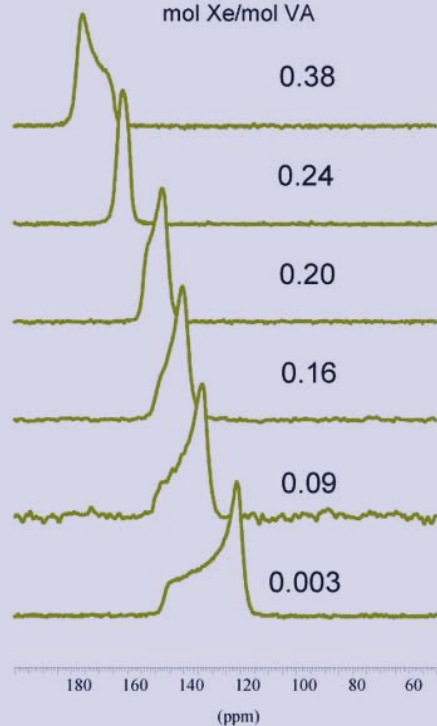
PNAS 101, 17924 (2004)

VA

mol Xe/mol VA

AV

mol Xe/mol AV



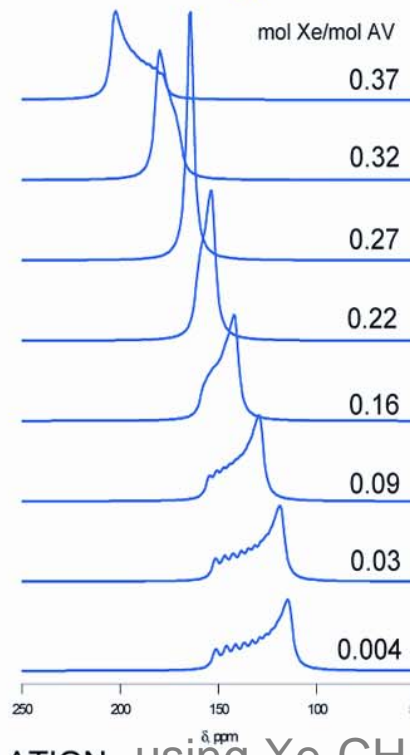
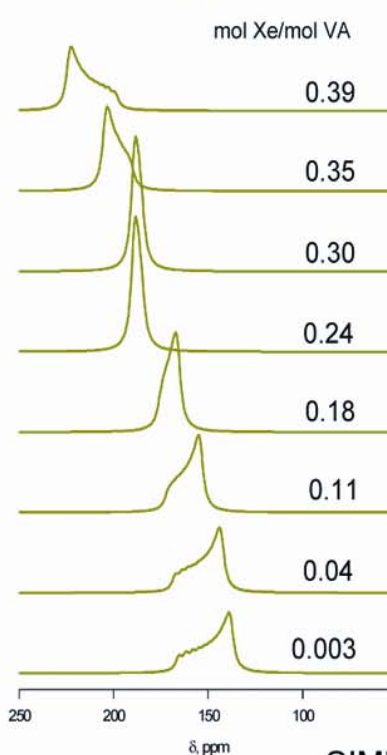
EXPERIMENT

VA

mol Xe/mol VA

AV

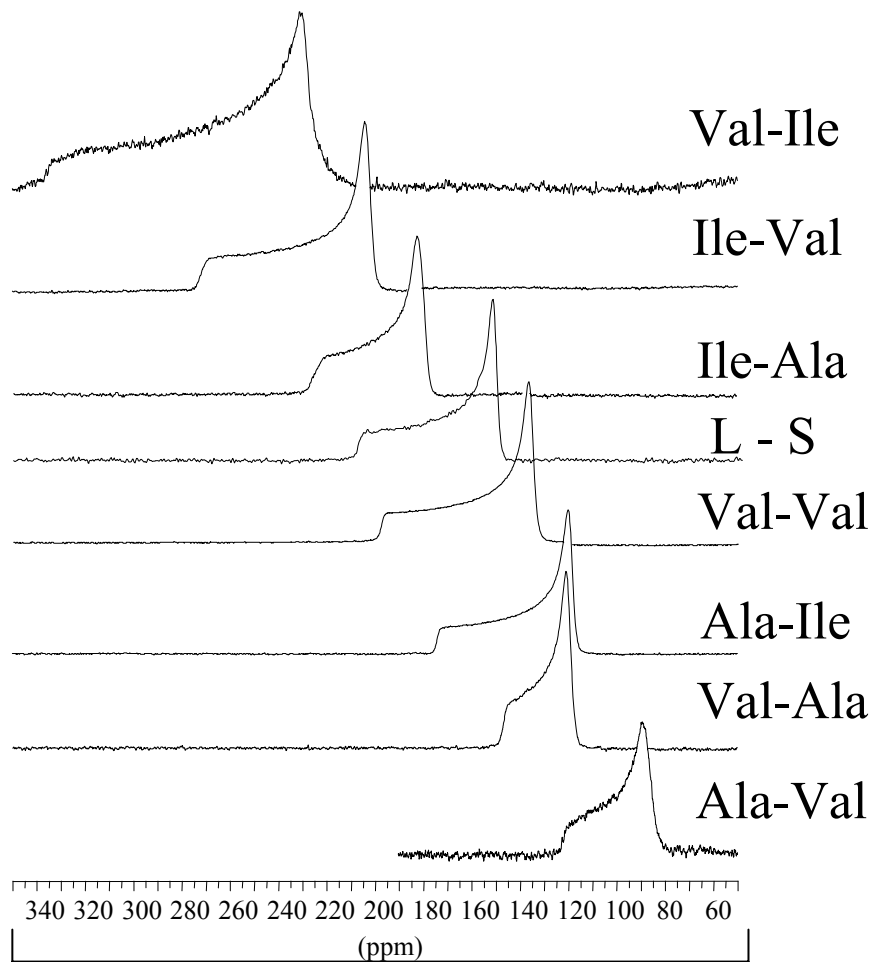
mol Xe/mol AV



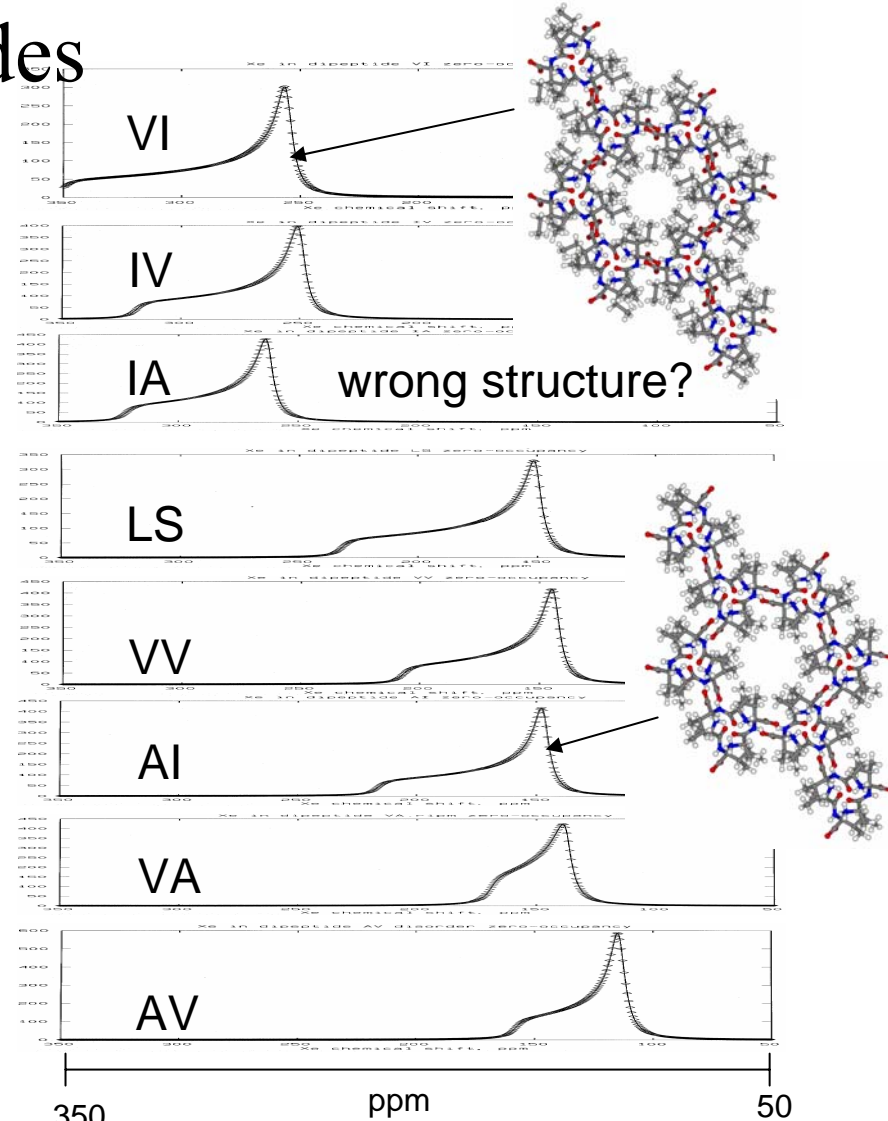
SIMULATION using Xe-CH₄

Xe NMR spectra

^{129}Xe NMR in dipeptides



EXPERIMENTS



SIMULATIONS



Xe line shape signatures in diamagnetic channels

- *# singularities at high $\langle N \rangle$* → aspect ratio of cross section (2 singularities: nearly circular; 3 singularities: elliptical)
- *1 constant tensor component with changing $\langle N \rangle$* → channel diameter does not permit two Xe to pass each other.
- *Significant change of δ_{\parallel} with $\langle N \rangle$* → cross section large enough to permit XeXe₂ groupings to achieve angles smaller than 150-180° at high $\langle N \rangle$.

Xe line shape signatures in diamagnetic channels

- *Linear behavior of each component with $\langle N \rangle$* → orderly arrangement of Xe atoms in channel; Xe sits in register with sites along walls. Xe unable to do this when sites too close together
- *Non-linear behavior of tensor components with $\langle N \rangle$* → non-uniform channel cross section.

Xe on single crystal surfaces

EXPERIMENTS by Heinz Jänsch

- Xe at the surface of bulk xenon has a different signal than Xe in the bulk
- Xe can tell which surface it is in contact with
- Xe can tell how many other Xe are on the same surface
- The chemical shift tensor can be mapped out by rotating the single crystal in the magnetic field

Xe on model surfaces

Grand canonical Monte Carlo

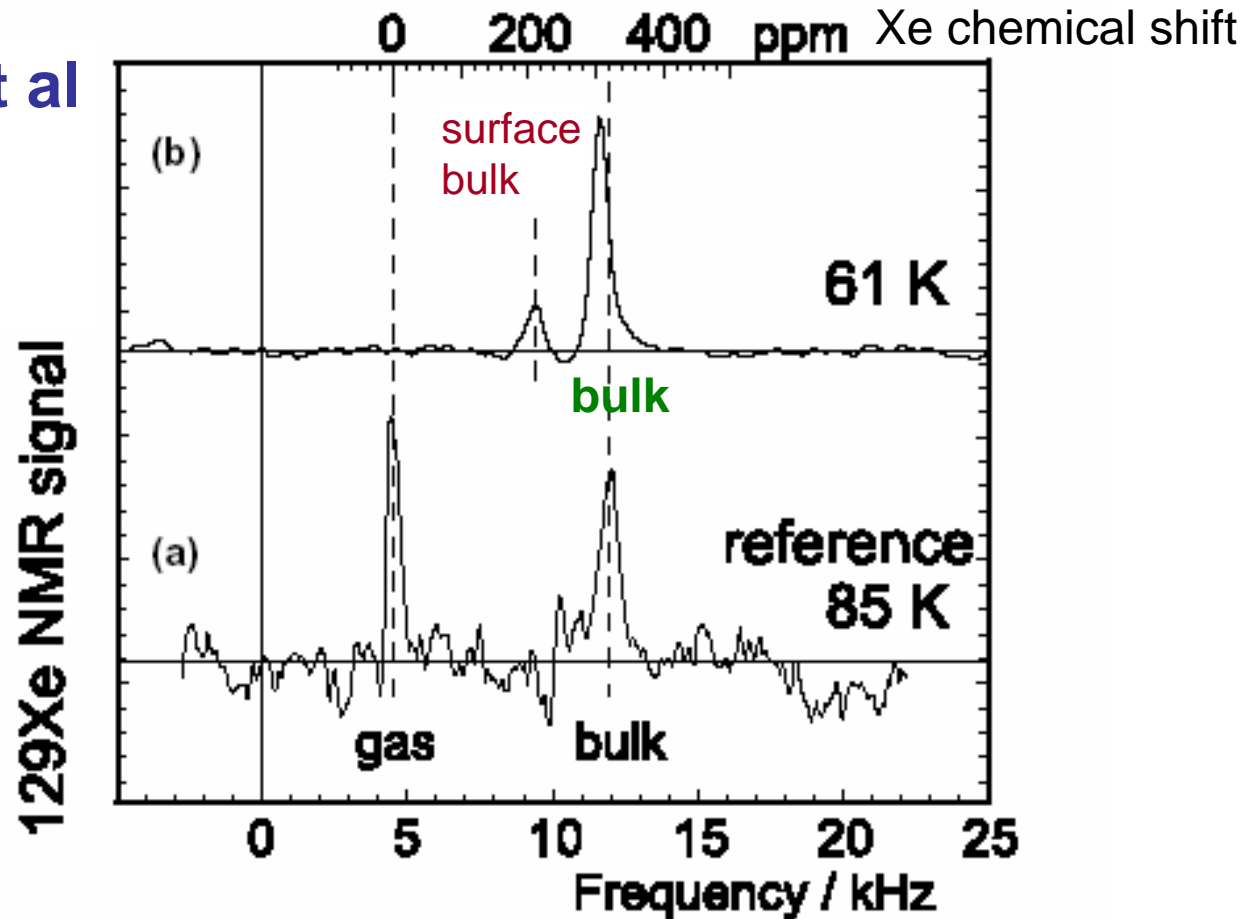
- Xe on a –CO monolayer
[using *ab initio* $\sigma(\text{Xe-Xe})$ and $\sigma(\text{Xe-CO})$
tensor functions]
- ^{129}Xe in a xenon sheet
[using *ab initio* $\sigma(\text{Xe-Xe})$ tensor function]

**Deduce Xe coverage (θ_{Xe})
from observed chemical shift?**

Xe on the surface of a single crystal metal surface

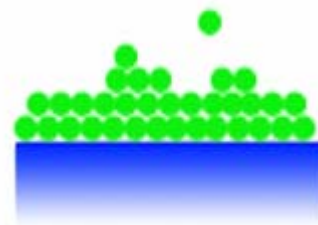
H.J. Jänsch et al

Chem. Phys. Lett.
372, 325 (2003)



The Xe atoms on the surface of the bulk Xe appear at **209** ppm
while Xe in the middle of the bulk is at **321** ppm **WHY?**

QUALITATIVELY



How many neighbor atoms?

- Xe atoms on the surface of the bulk Xe appear at 209 ppm

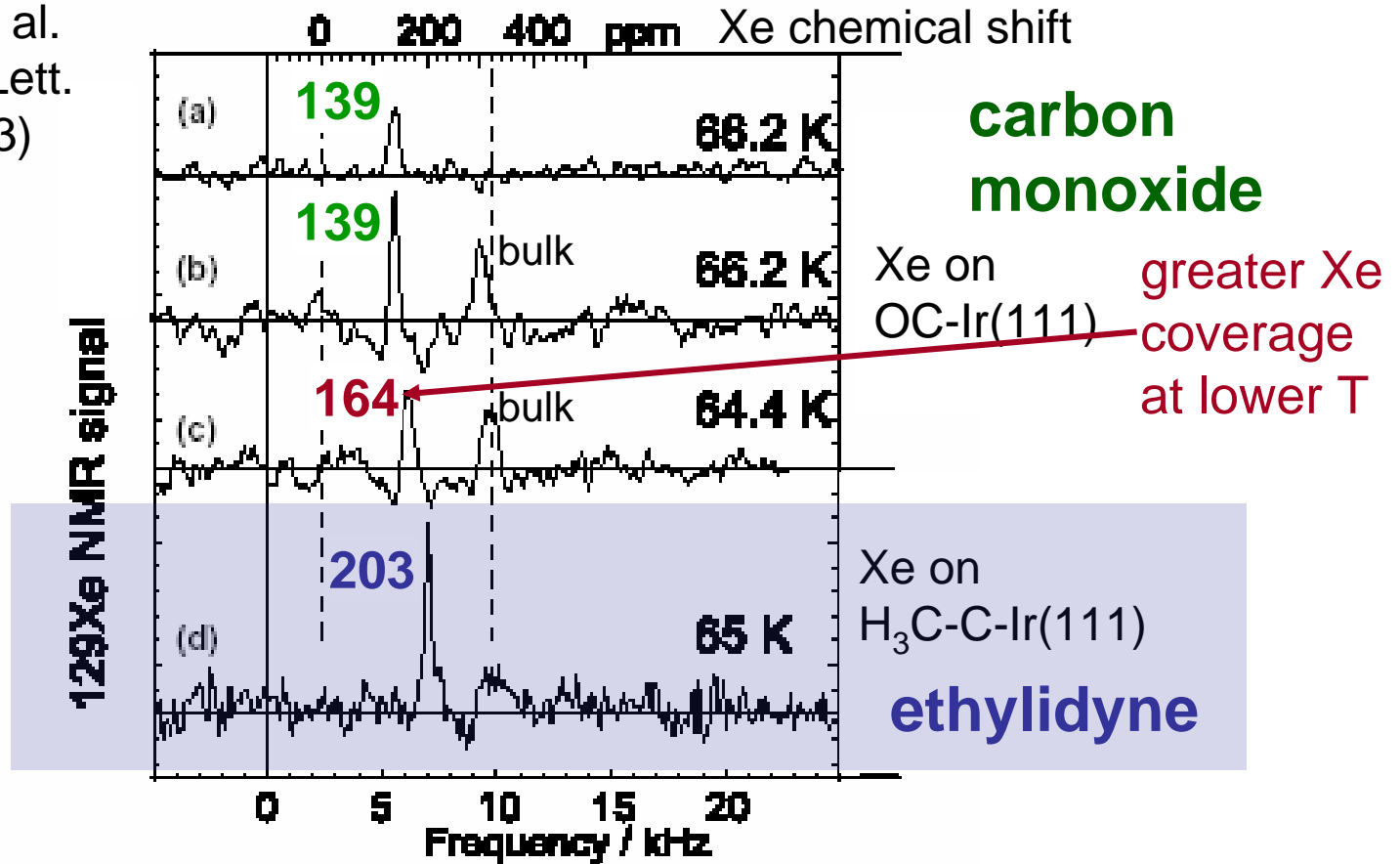
$\sigma = \sum \sigma(r_{\text{Xe-Xe}})$ nearest (short $r_{\text{Xe-Xe}}$) neighbors are below and in same plane.

- Xe in the middle of the bulk appear at 321 ppm

$\sigma = \sum \sigma(r_{\text{Xe-Xe}})$ nearest neighbors are below, above, and in same plane.

Xe on a chemically modified metal surface

H.J. Jänsch et al.
Chem. Phys. Lett.
372, 325 (2003)



Xe can tell the difference between **OC** and **H₃C-C** surfaces.

Xe can report on surface coverage

QUALITATIVELY:

Xe @OC-Ir(111):

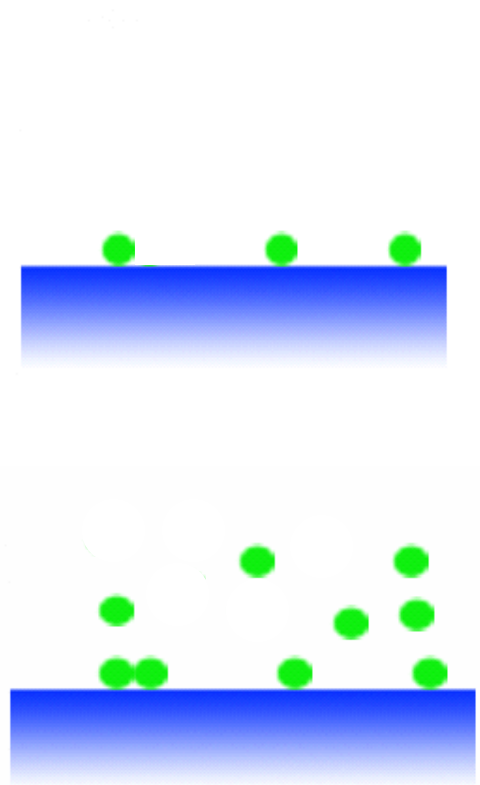
- At low Xe coverage, θ_{Xe} ,

$$\sigma = \sum \sigma(r_{\text{Xe-O}}) \text{ only}$$

- At lower T, larger θ_{Xe} ,

$$\sigma = \sum \sigma(r_{\text{Xe-O}}) + \sum \sigma(r_{\text{XeXe}})$$

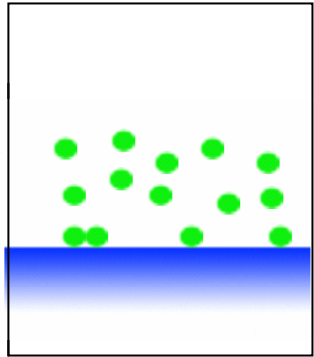
once in a while, Xe runs
into other Xe



Xe can tell the difference between OC and H₃CC surfaces

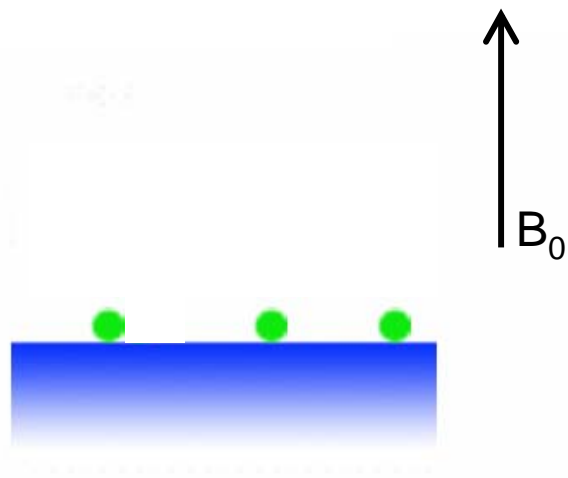
- intrinsic shielding response from Xe-OC is greater than the shielding response from Xe-H₃C at same distance
- however, potential functions permit Xe to stay closer to H₃C than OC, resulting in larger average Xe chemical shifts for the same coverage at the same temperature

GCMC simulations of Xe on surfaces

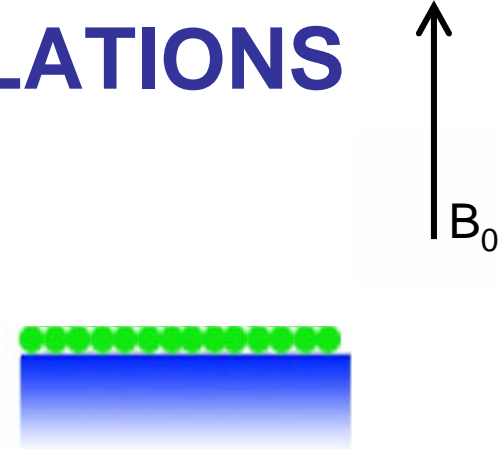
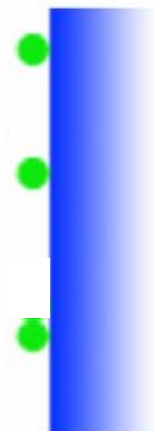


The chemical shift tensor can be mapped out by rotating the single crystal in the magnetic field

GCMC SIMULATIONS

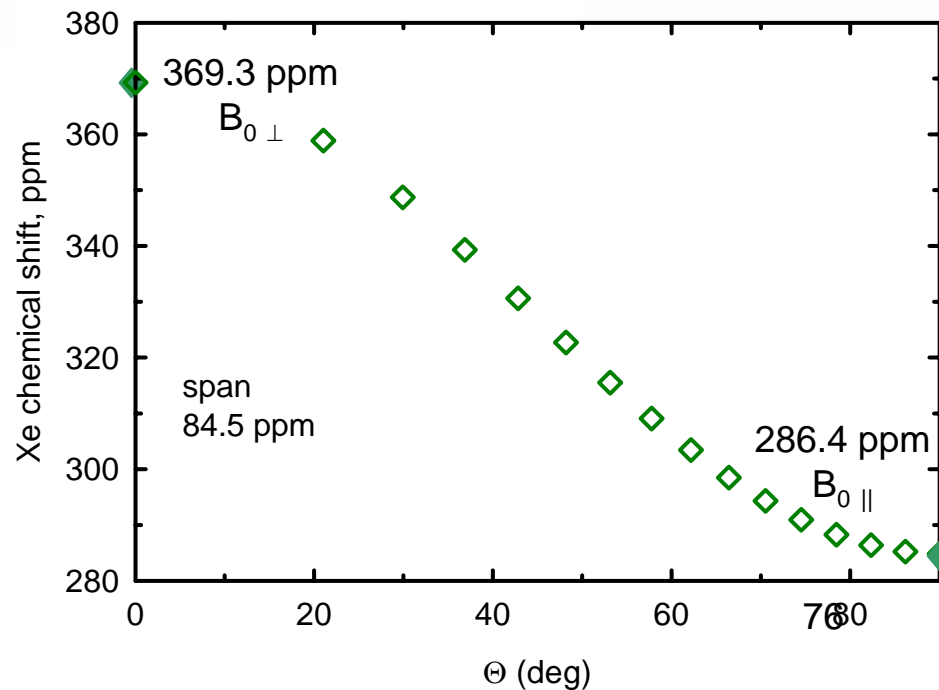
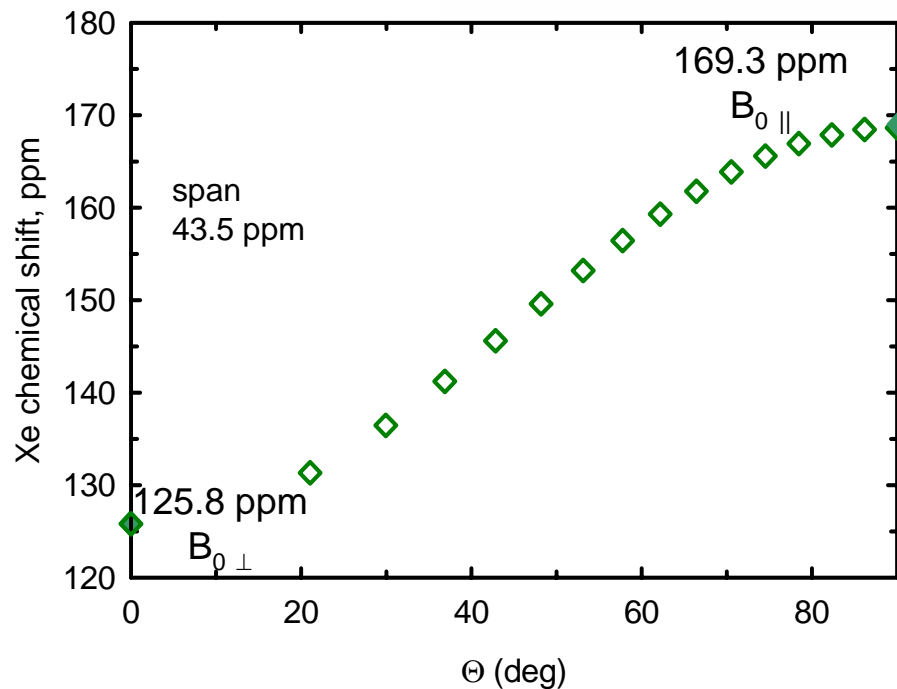


Xe on OC-M
very small θ_{Xe}
seeing Xe-O



Xe on OC-M
 $\theta_{\text{Xe}} = 0.358$

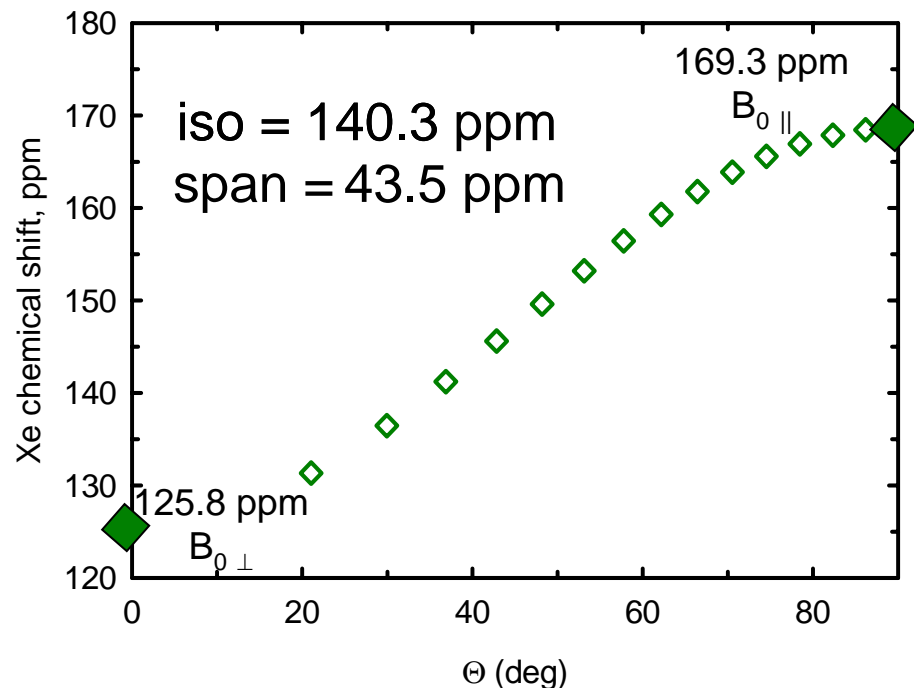
seeing Xe-O and Xe-Xe



Comparison with Jänsch's experiments

Xe on OCIr(111)
very small θ_{Xe}

GCMC SIMULATIONS



Xe on OCIr(111)
small θ_{Xe}

EXPERIMENTS

iso = 165.2 ppm
span = 56.7 ppm

the same angle
dependence

- The **difference between CO and ethynidyne is predictable** from isolated Xe-OC, Xe-H₃CH shielding response
- **Dependence on crystal orientation in the field is reproduced.** For sample geometry, the dominant Xe dimer is, respectively, perpendicular (Xe-O) or parallel (Xe-Xe) to the crystal surface
- **Can deduce Xe coverage from chemical shift**, very sensitive because each Xe-Xe contribution larger than Xe-OC or Xe-H₃C

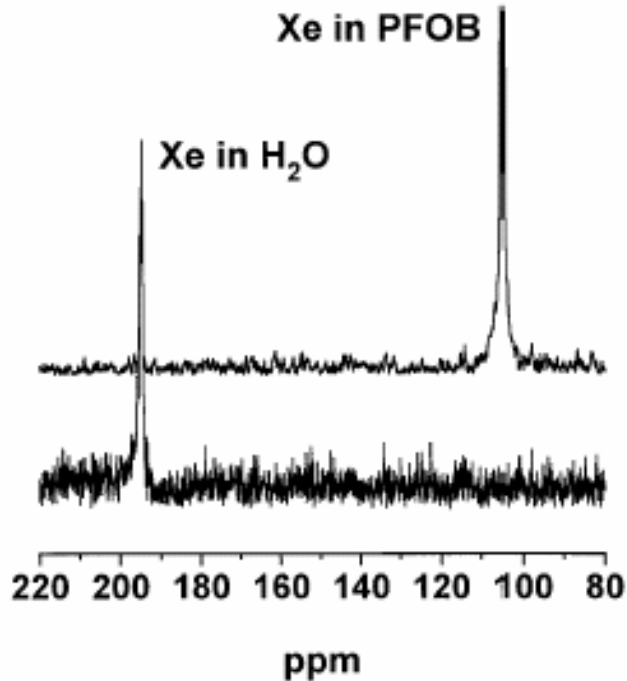
The chemical shift tensor can be mapped out by rotating the single crystal in the magnetic field

- Our GCMC simulations predict the average Xe chemical shift **tensor**
- Component along the field direction is qualitatively predictable from knowing only the numbers and types of neighbors that Xe has in the plane containing the Xe atom in question and perpendicular to the field direction

Xe in liquids

QUESTION:

What information is encoded into the Xe chemical shift of a Xe atom dissolved in a liquid?



- instantaneous solvent cage sizes and shapes
- accurate representation can only be accomplished by molecular dynamics (MD)
- Molecular Dynamics simulations provide quick convergence of Xe chemical shift

Previous interpretations of Xe chemical shifts in liquids

- Strictly empirical (refractive index)
- Based on dispersion model of chemical shift
- No explanation for intercepts in correlation plots

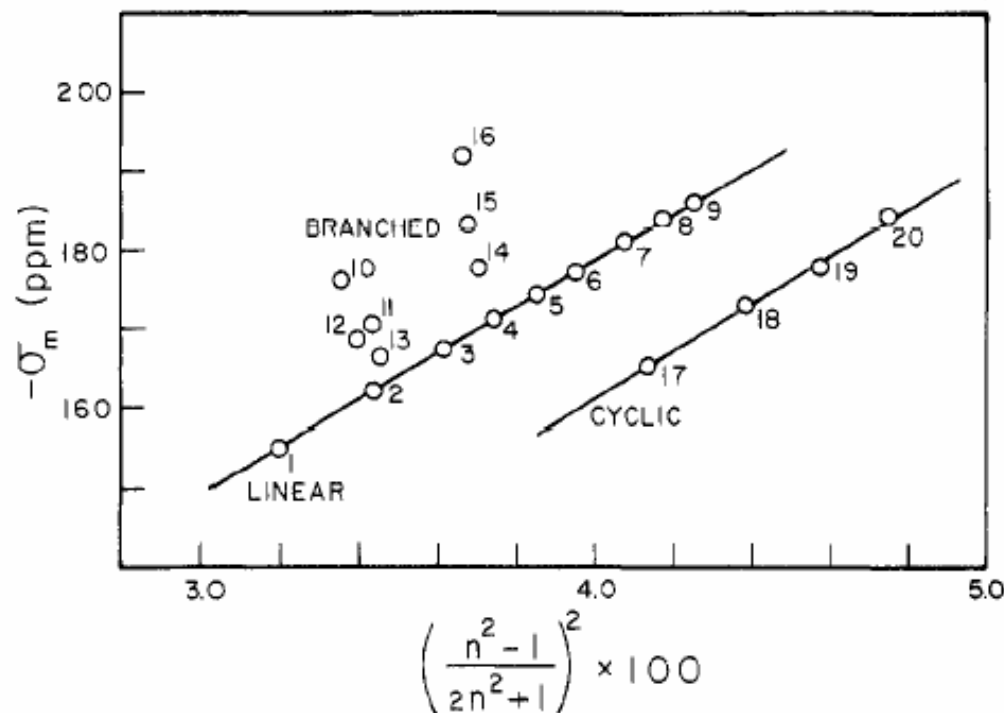
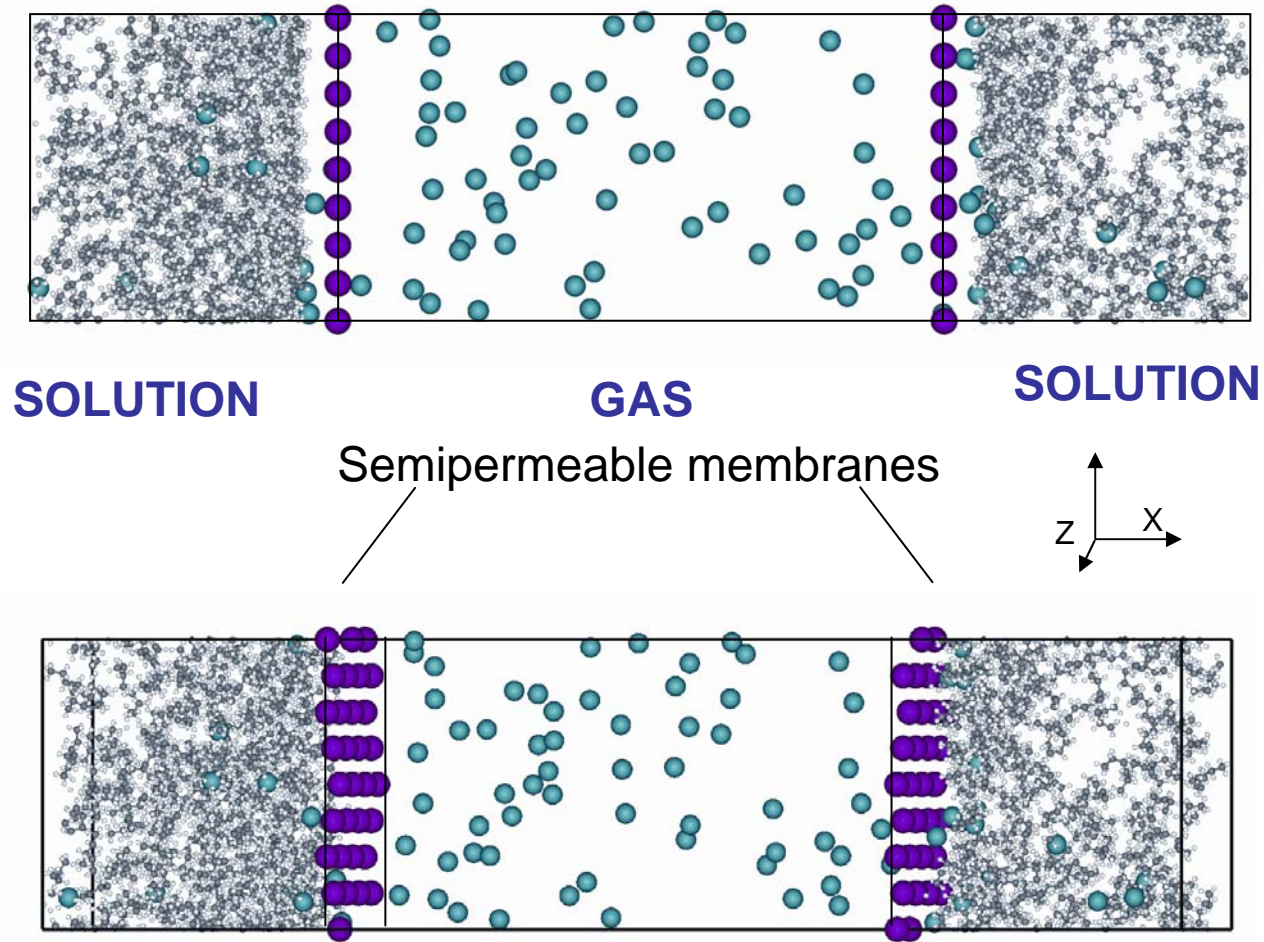
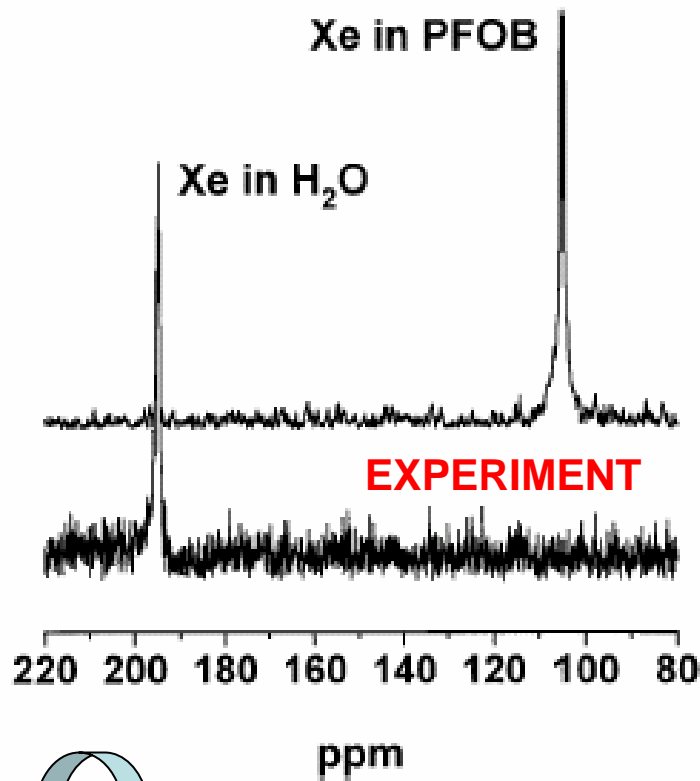


Figure taken from: Stengle et al., J. Phys. Chem. 85, 3772 (1981).

MD Simulation Box

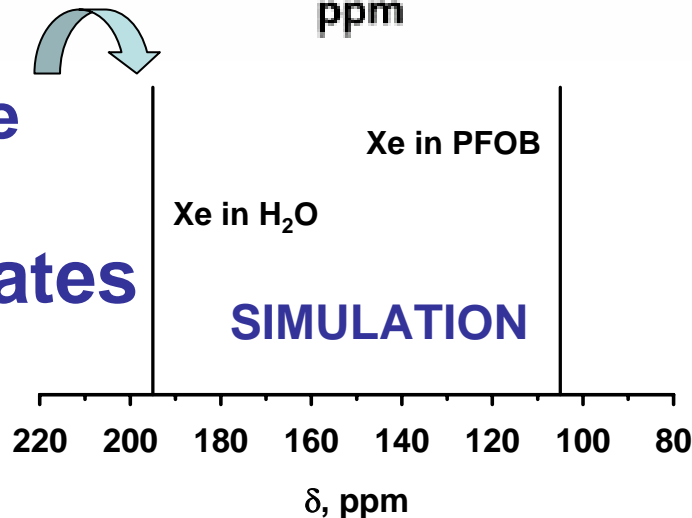


MD Simulation box design: Murad et al, Fluid Phase Equil. 187-188, 29 (2001)
Murad et al, Chem. Phys. Lett. 319, 60 (2000)



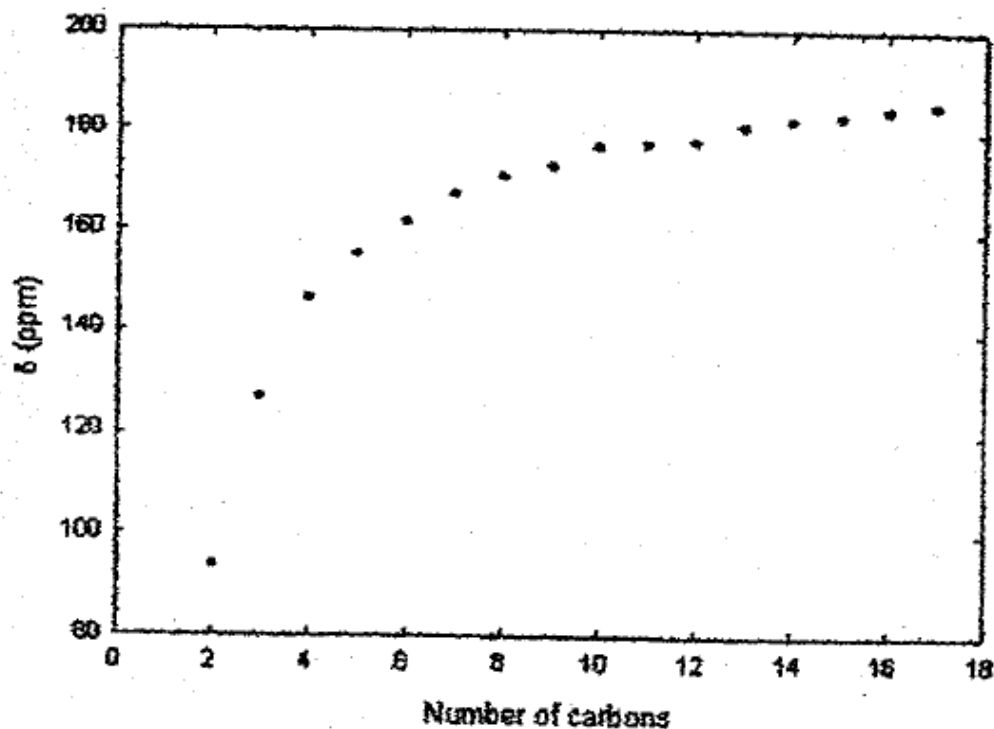
Bifone et al,
Magn. Reson.
Medicine 41,
442 (1999).

Using quantum
mechanical Xe
shielding surface
calculated for
clathrate hydrates



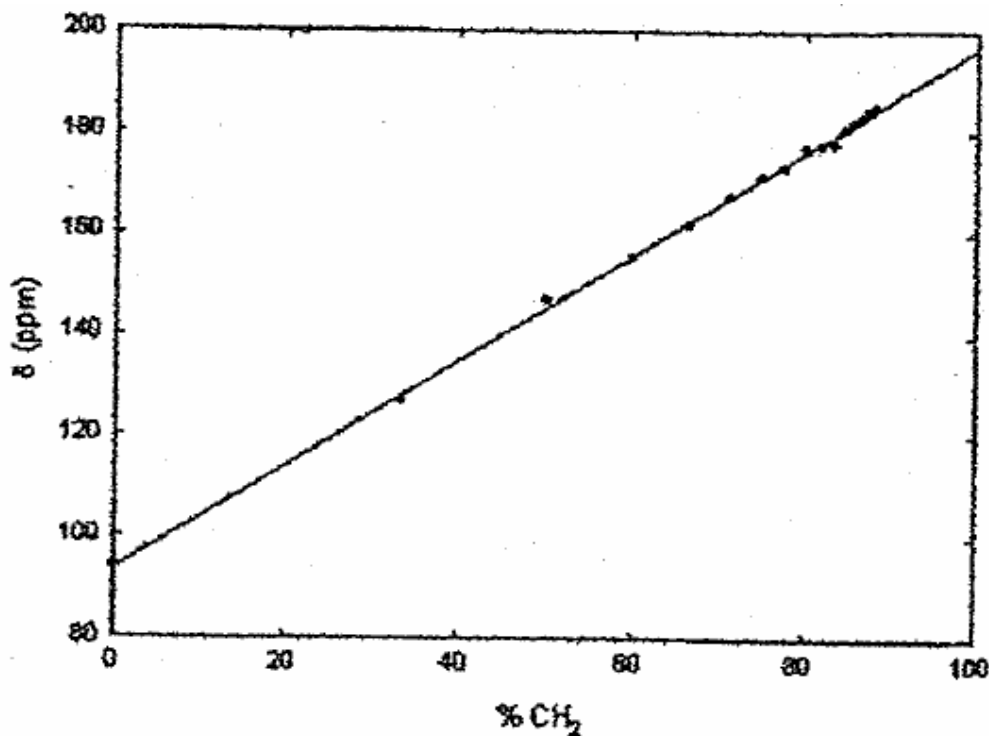
C. J. Jameson,
D. N. Sears, S.
Murad, J. Chem.
Phys. 121, 9581
(2004)

Dependence of Xe chemical shift on number of carbons in linear alkanes



Lim et al., J. Phys. Chem. 1993

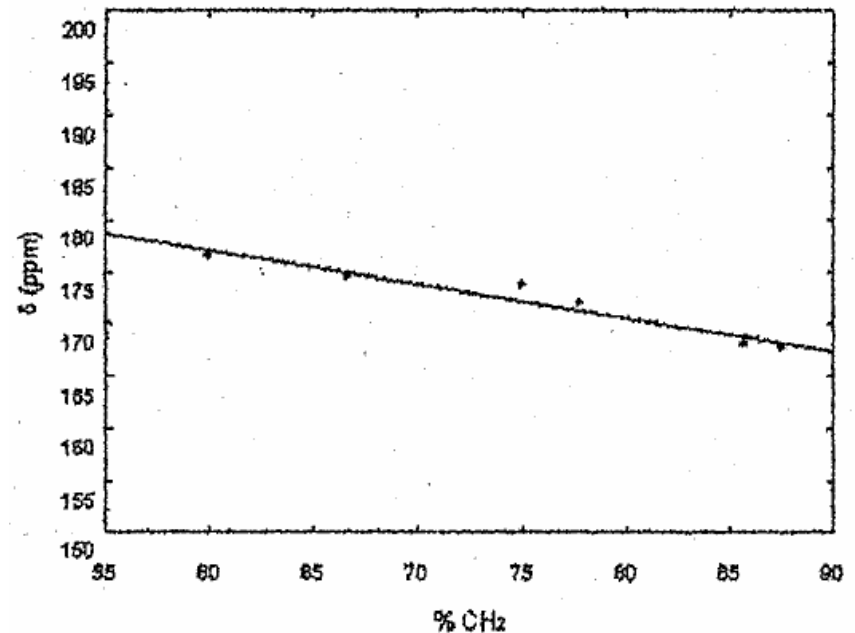
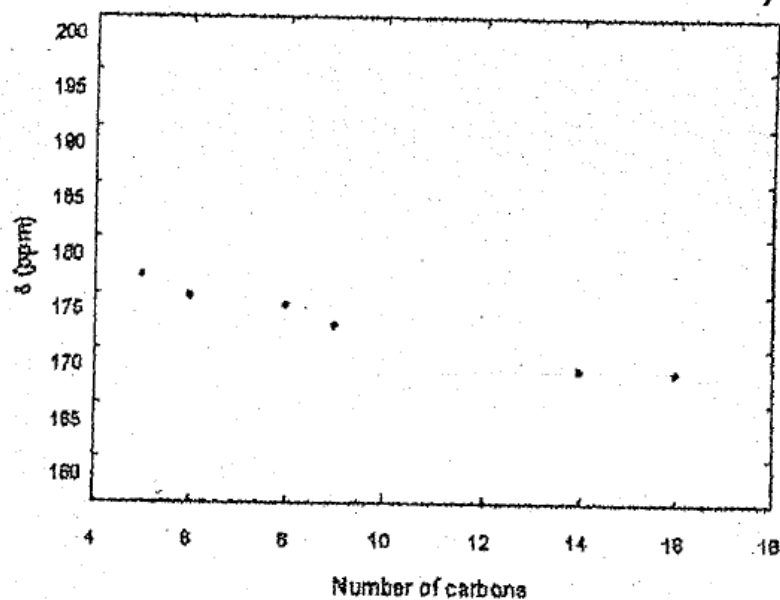
Dependence of Xe chemical shift on %CH₂ in linear alkanes



Lim et al., J. Phys. Chem. 1993

Appears counter-intuitive! What is wrong here?

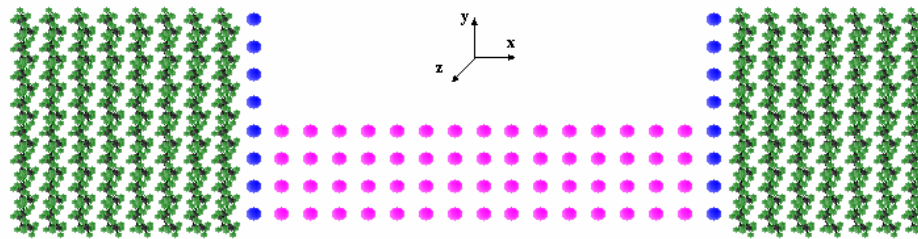
R. Bonifacio & Eduardo J.M. Filipe: XeMAT 2000: Compare Xe chemical shift in the liquids at same thermodynamic state, at $T^* = 0.5$



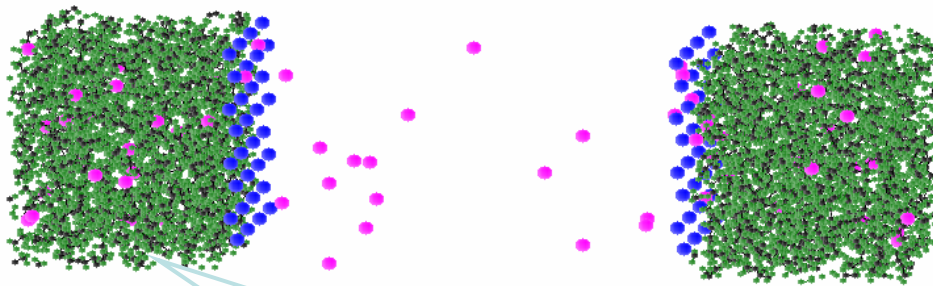
Looks more like what we should expect

Simulation System

Xe and *n*-hexane

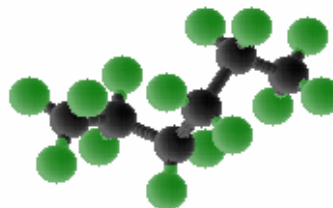


initial



10 ns

Typical *n*-hexane structure:



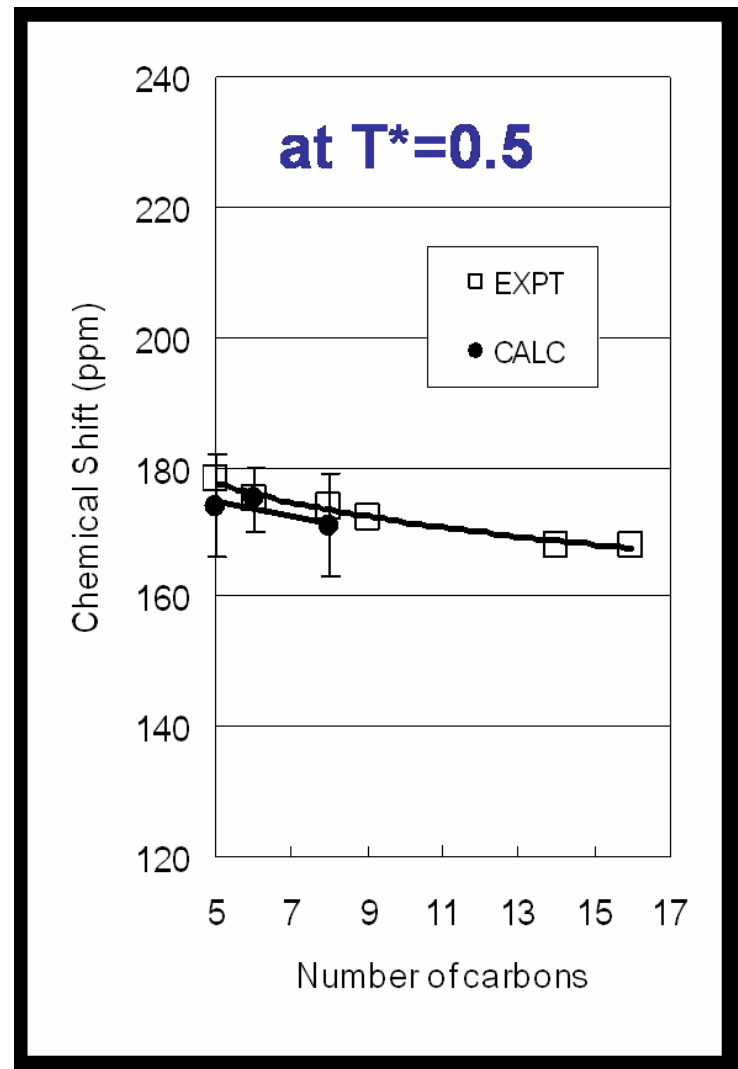
Comparable chemical shifts in solution

Xe chemical shift at the same thermodynamic state

□ EXPT: R. Bonifacio
& E. J. M. Filipe,
XeMAT 2000

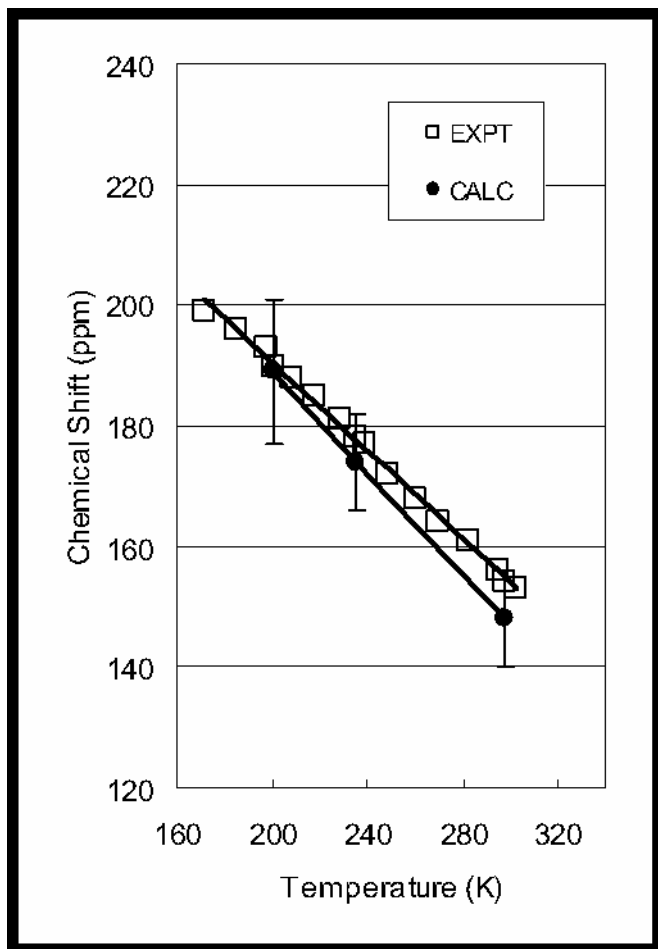
● Molecular Dynamics simulations

J. Phys. Chem. C, 111, 15771-15783 (2007).

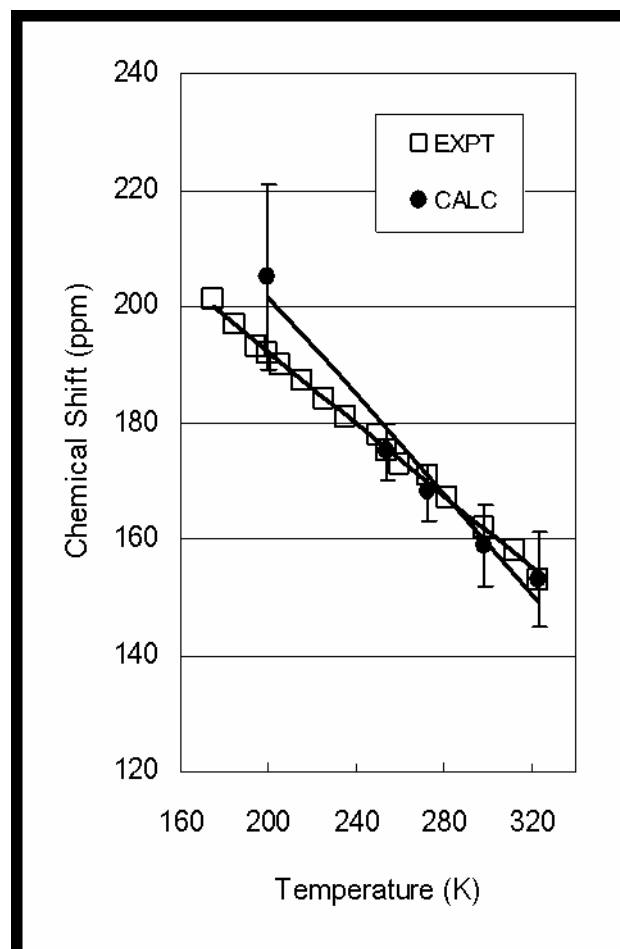


Xe chemical shift temperature dependence

n-pentane :



n-hexane :

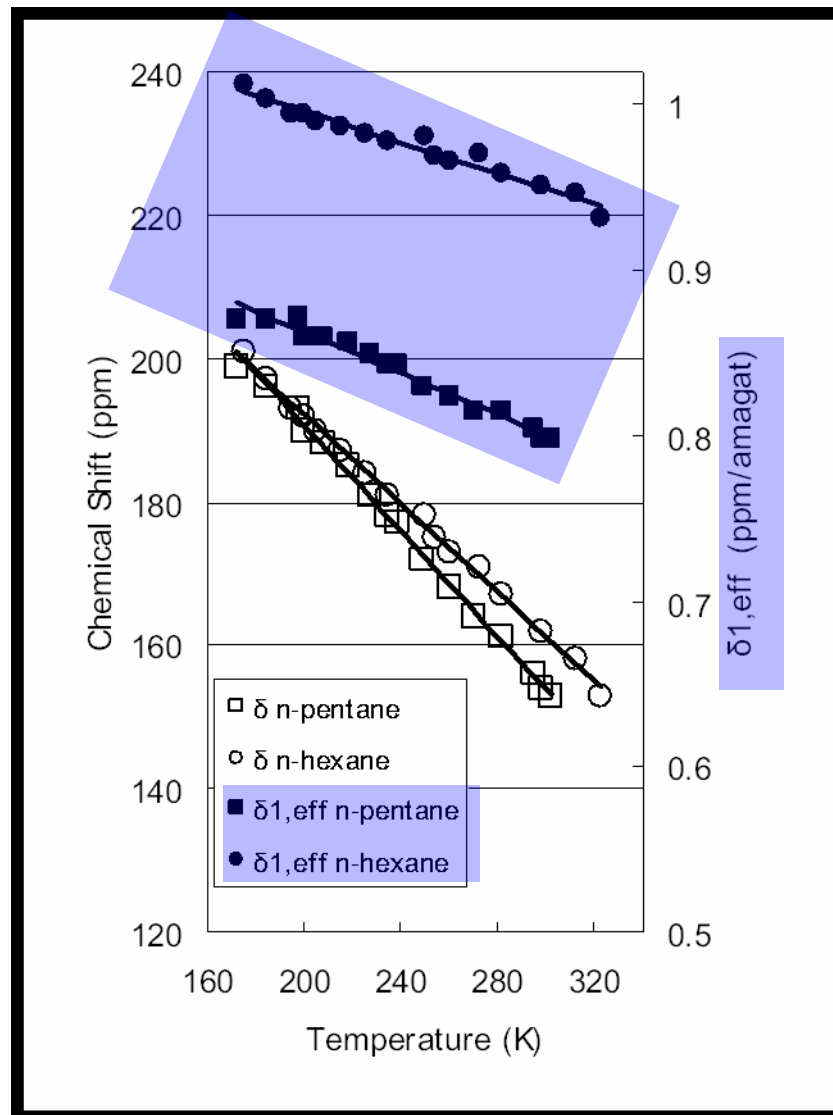


Molecular Dynamics simulations results

J. Phys. Chem. C, 111, 15771-15783 (2007).

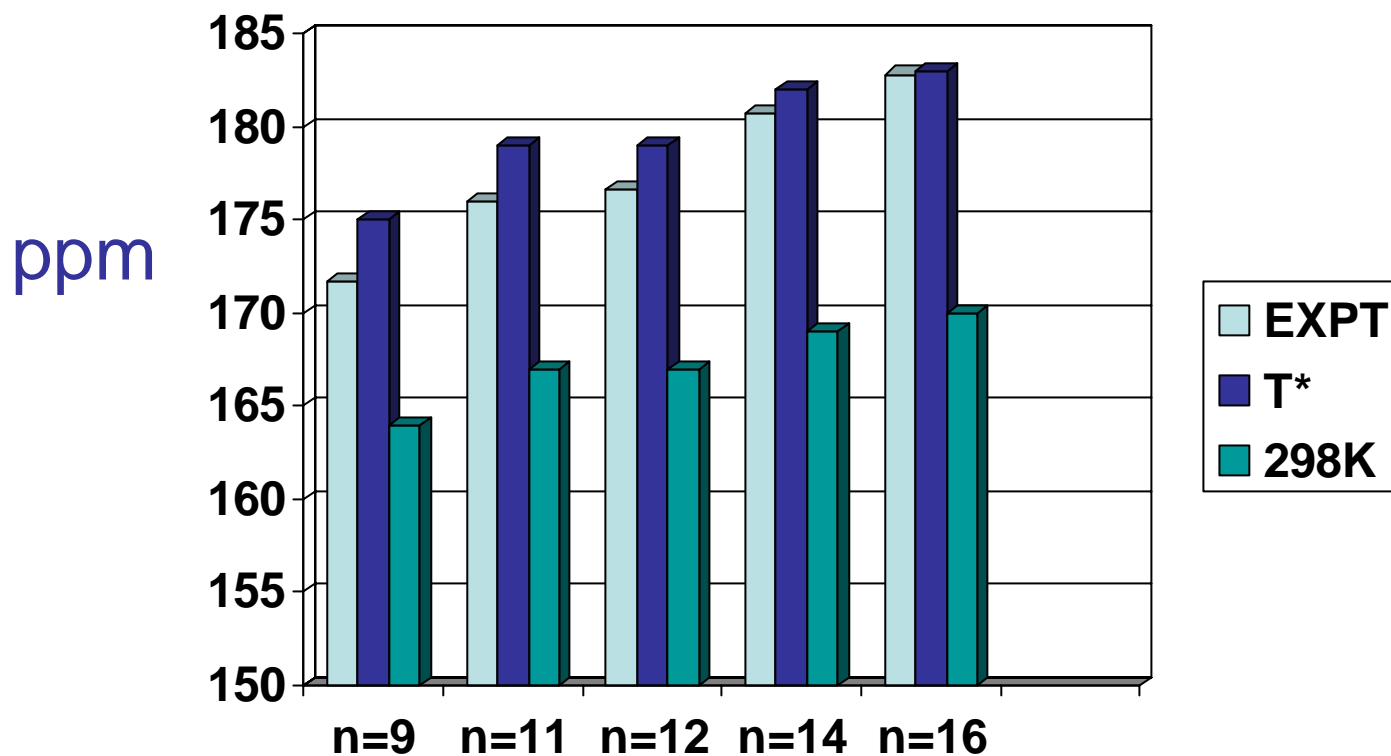
Contributions to the temperature dependence of Xe chemical shifts

T dependence of the solvent density is responsible for most of the observed steep T dependence of Xe chemical shifts in solution



divide out the density to get δ_1

Prediction of Xe chemical shifts in *n*-alkanes from constitutive contributions based on simulations for Xe in C_nH_{2n+2} , $n = 4, 5, 6, 8$ calculated at $T^*=0.5$, or calculated at $T=298$



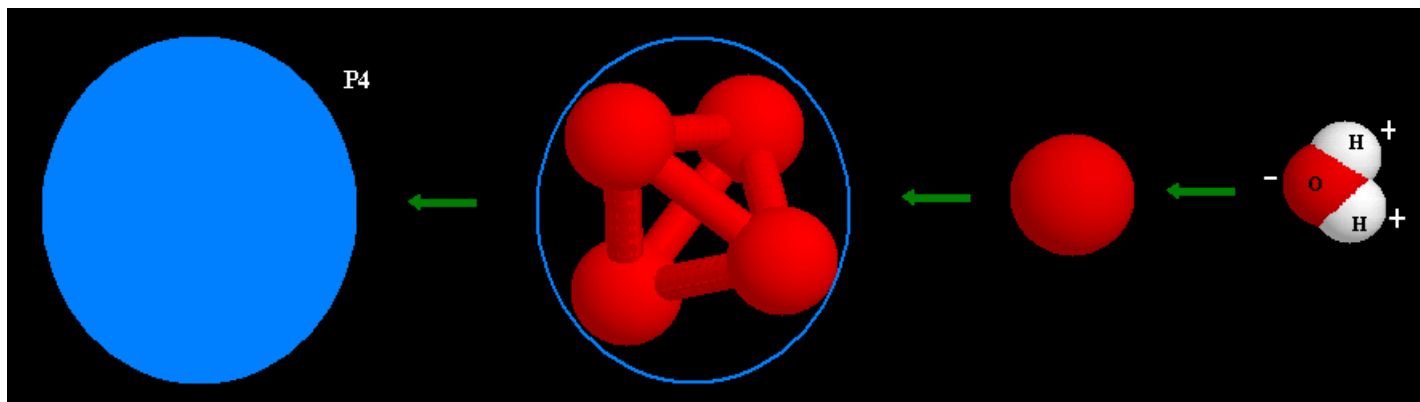
at $T^*=0.5$: CH_2 3.1 ppm/ (mole L^{-1}) CH_3 4.7 ppm/ (mole L^{-1})

Coarse grain force field

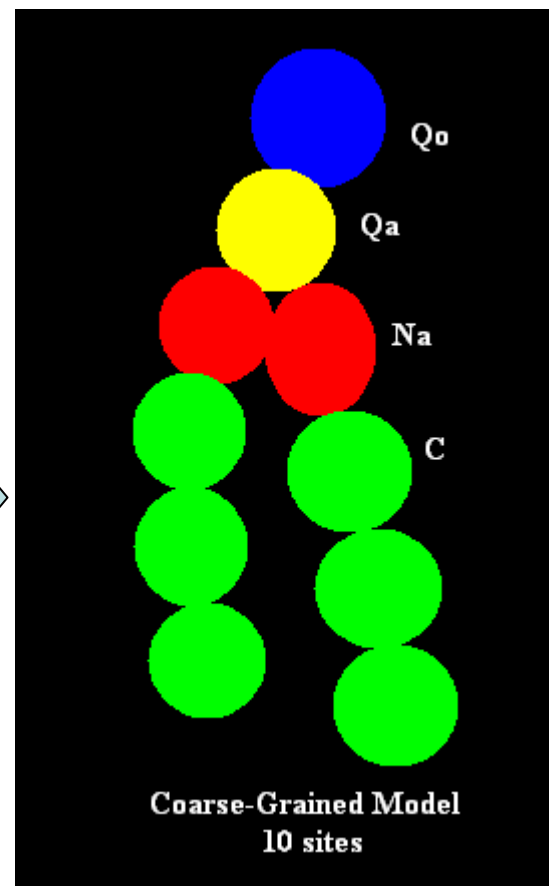
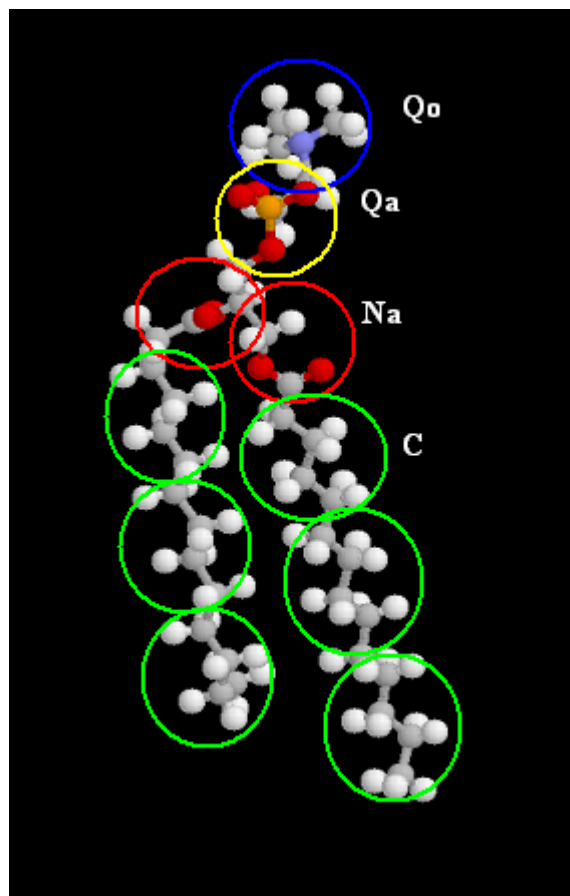
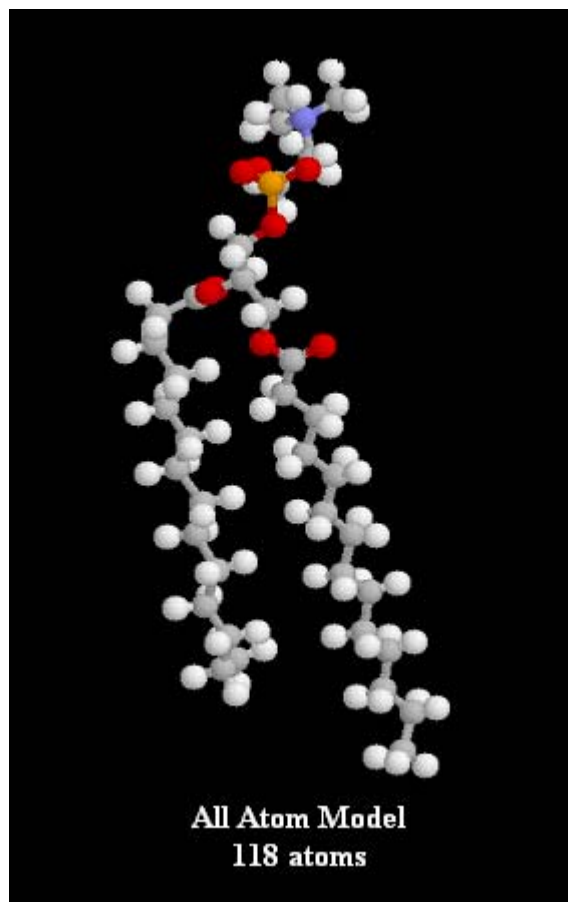
MARTINI force field by Marrink et al J.Chem.Theory and Comput. 2008, 4, 819-834

Coarse grain mapping strategy

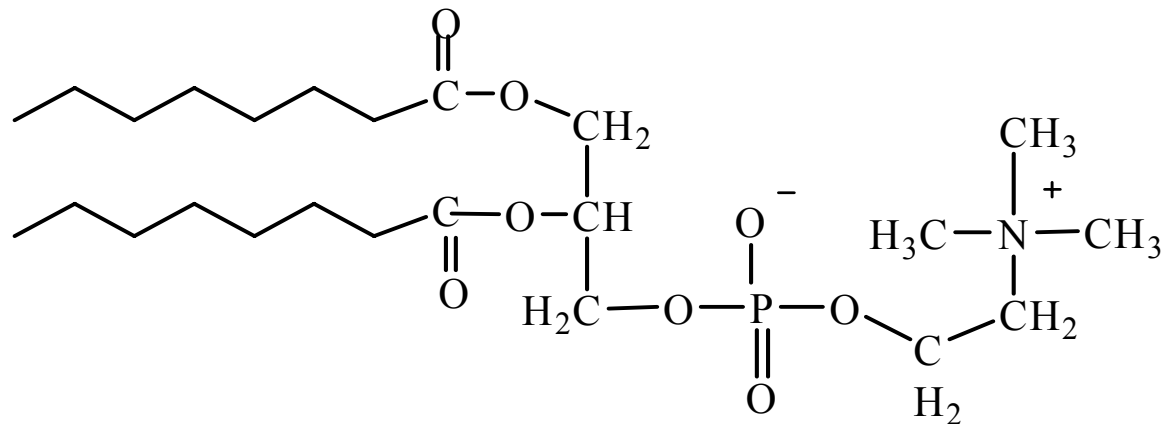
4 \rightarrow 1



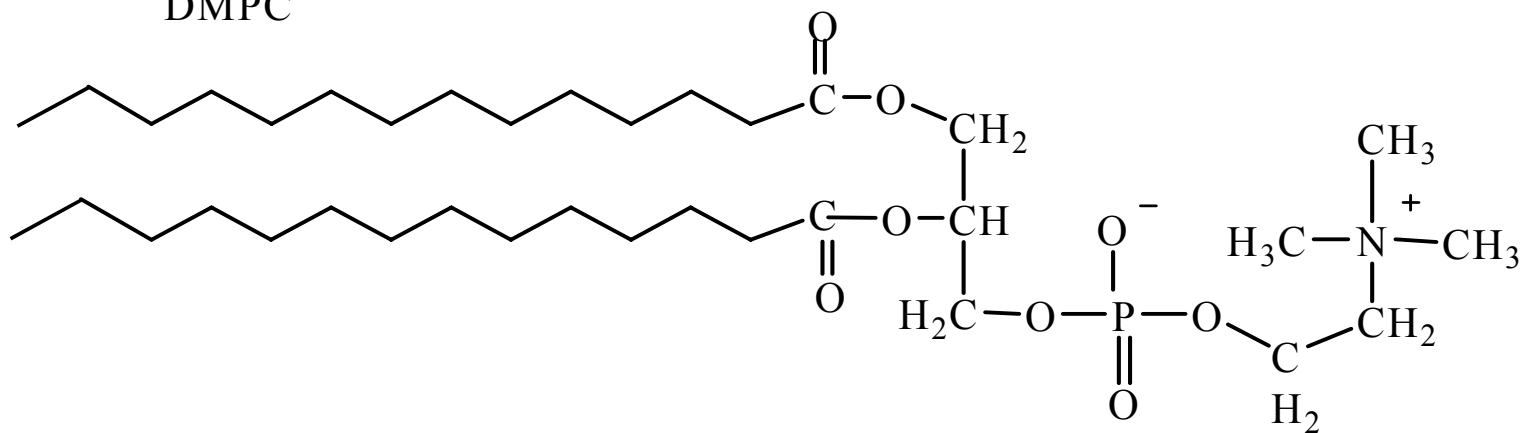
Lipid (DMPC):



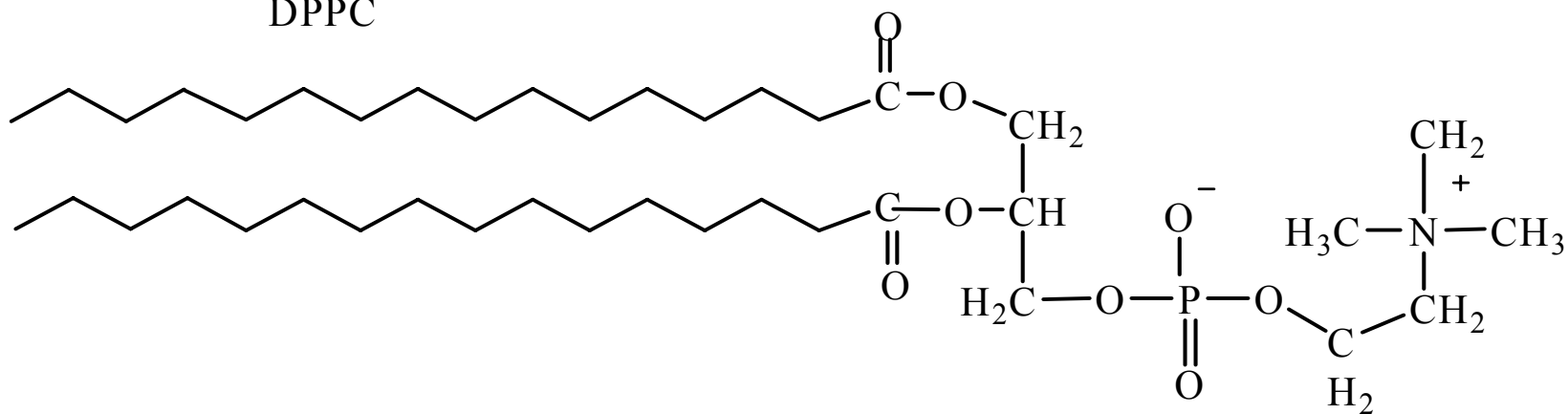
DCPC

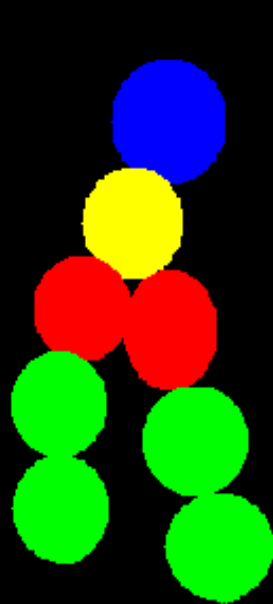


DMPC

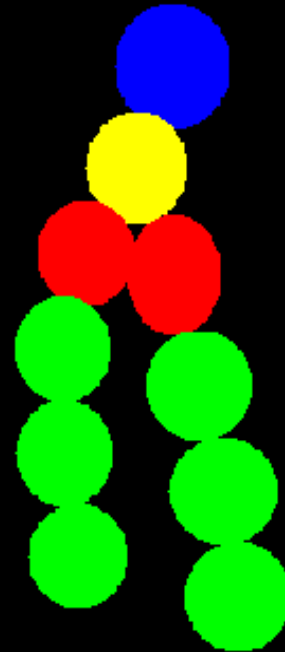


DPPC

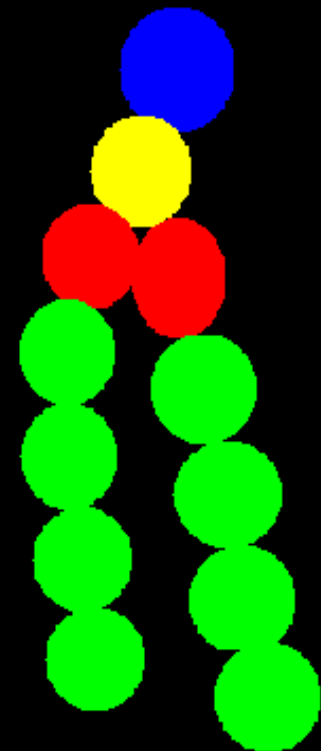




DHPC
8 sites

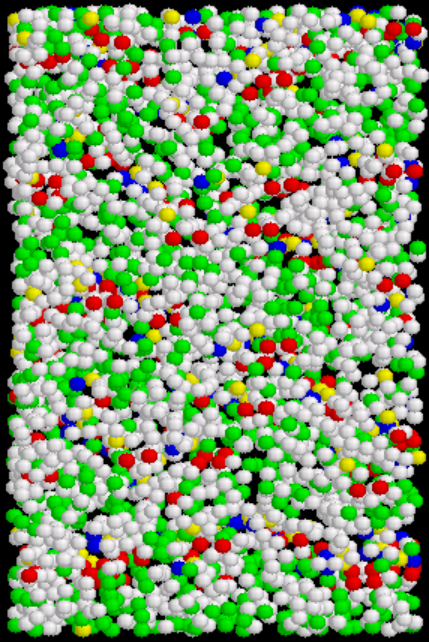


DMPC
10 sites

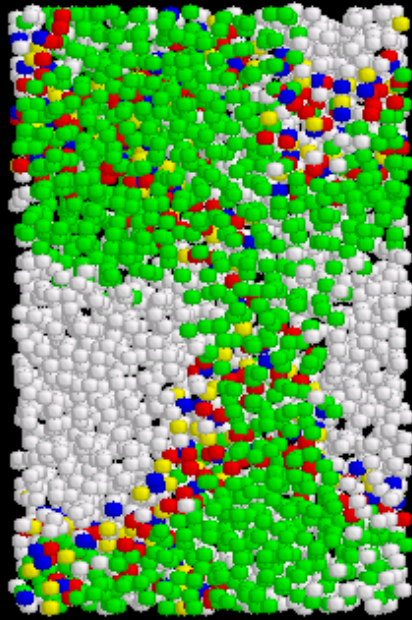


DPPC
12 sites

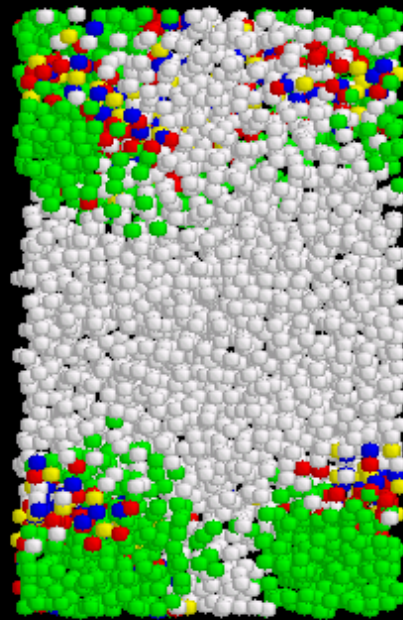
Self-Assembly occurs at 323K :



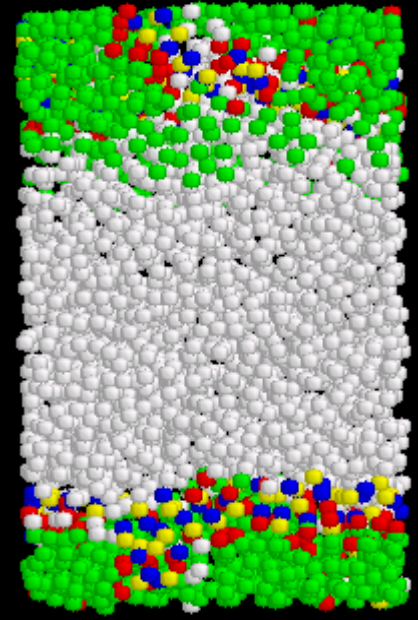
$t = 0 \text{ ns}$



$t = 1 \text{ ns}$

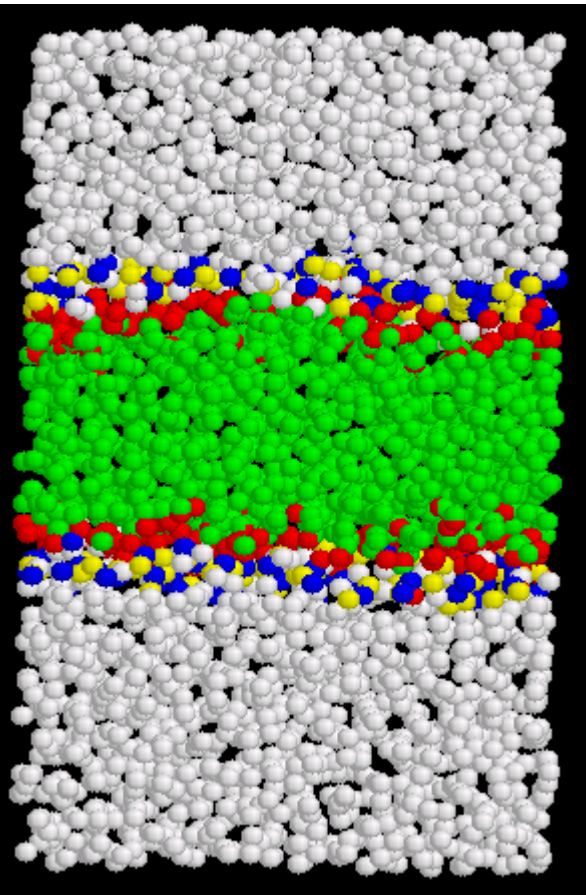


$t = 10 \text{ ns}$

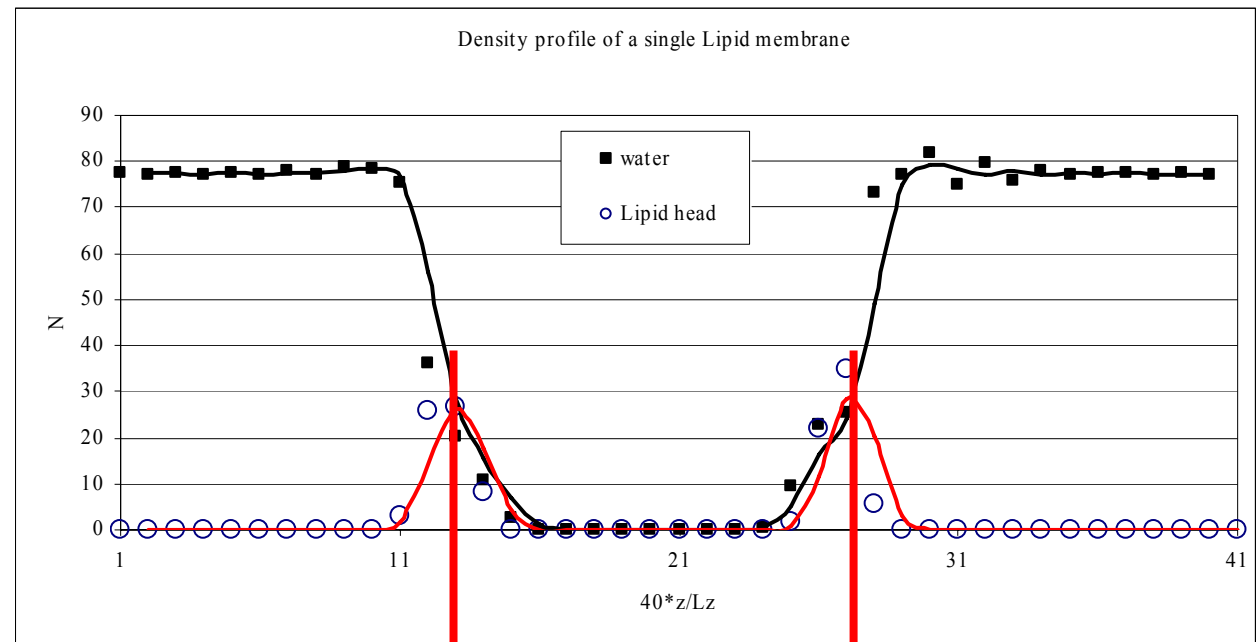


$t = 100 \text{ ns}$

Lipid Bilayer in water at 323K: 128DPPC+2000H₂O



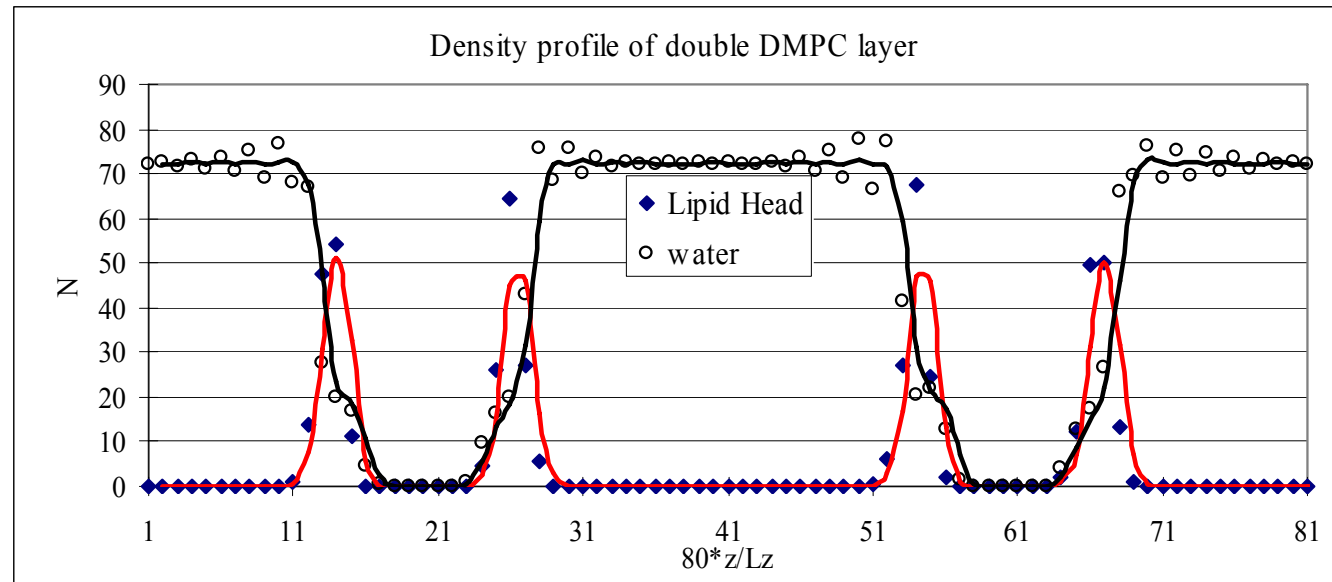
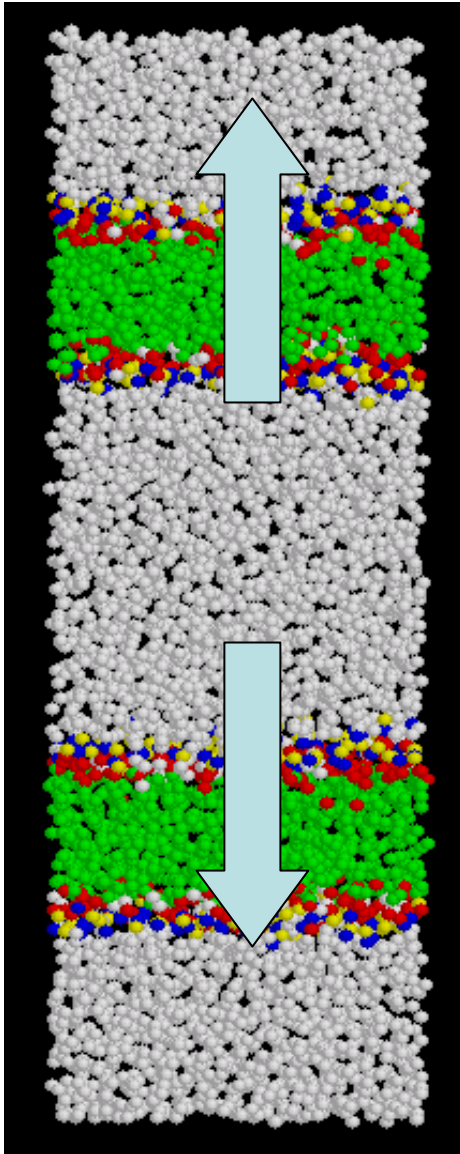
Density profile at equilibrium



3.75 nm

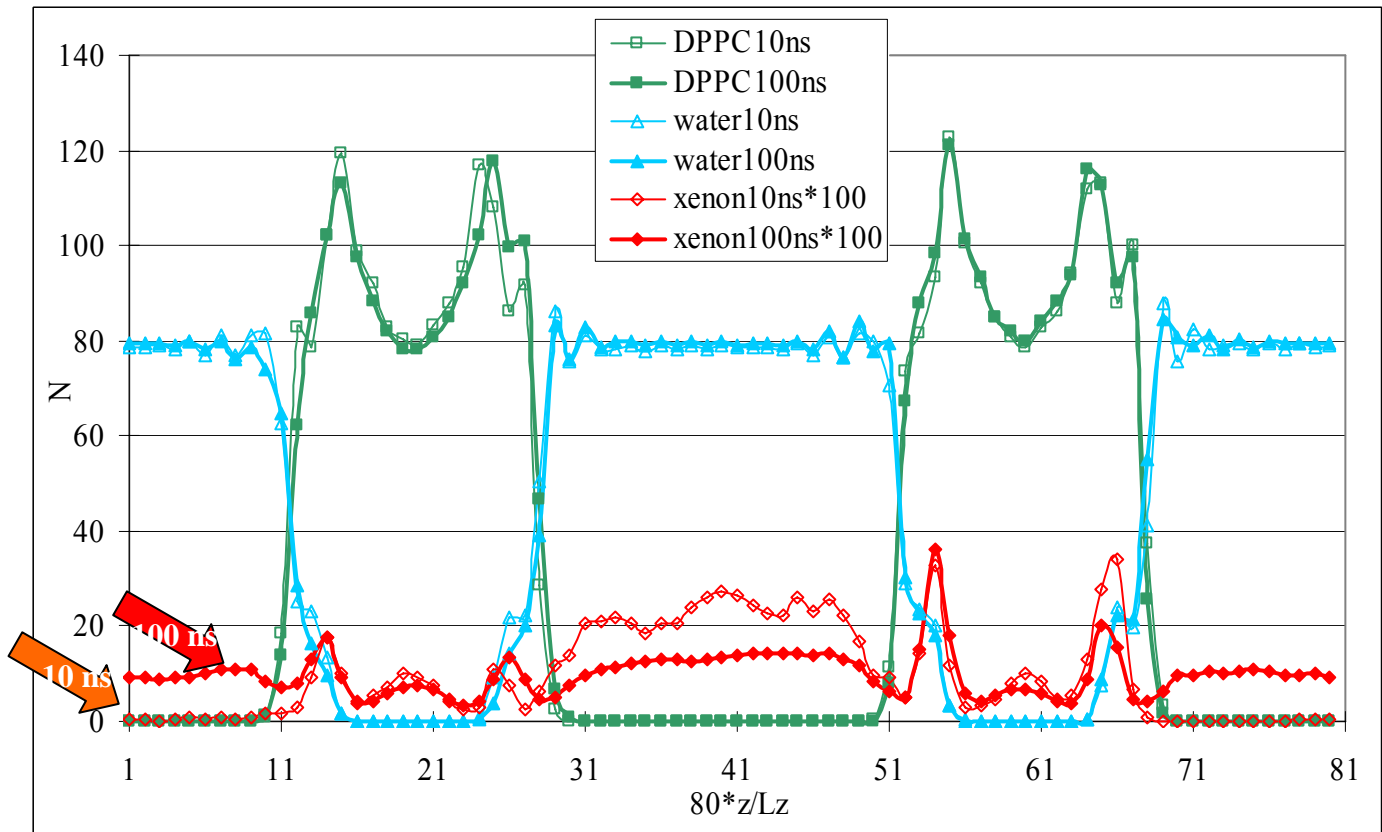
Expt. 3.85 nm

Simulation box for transport studies



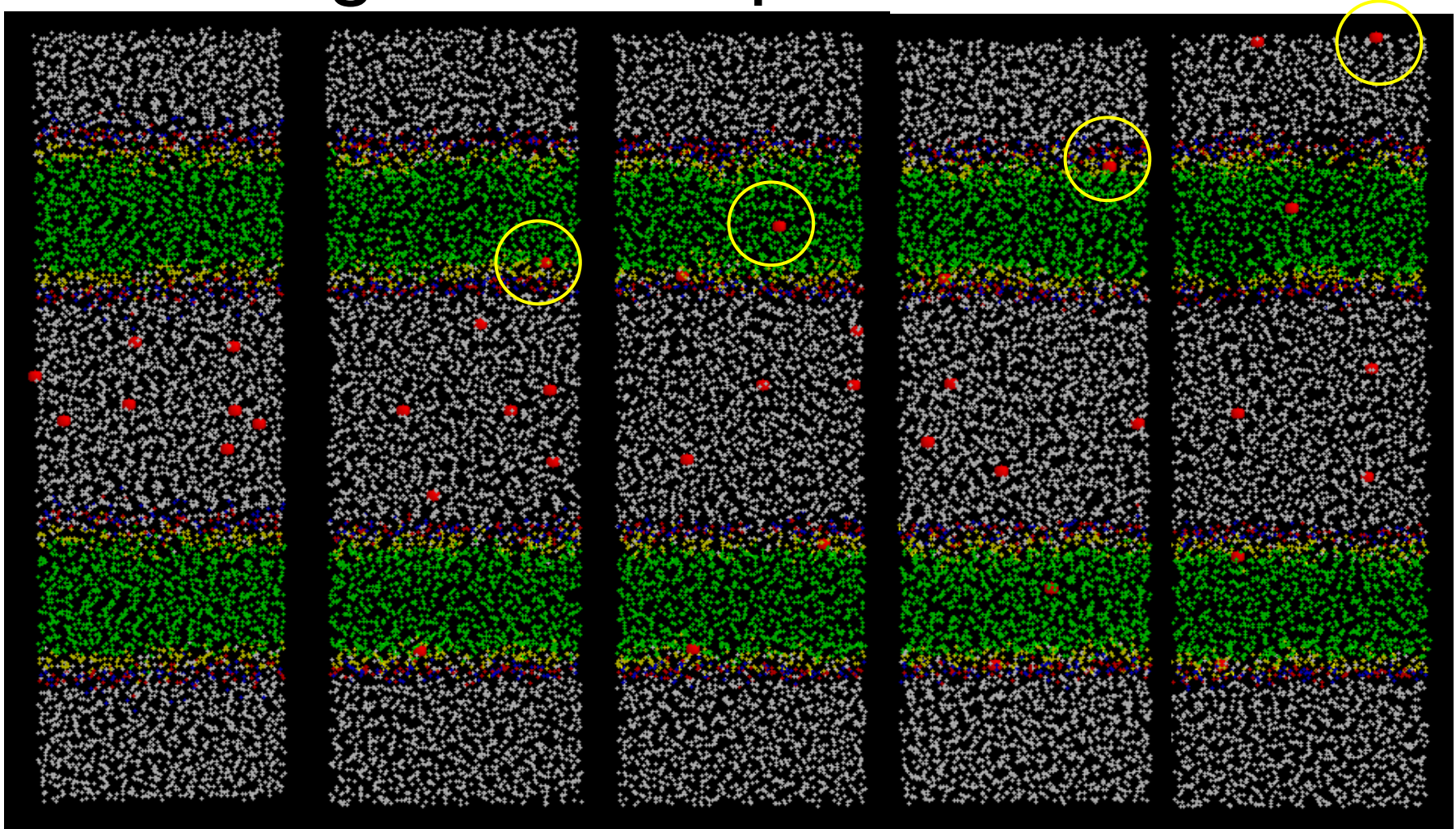
Xe placed initially in the center compartment
will diffuse through the membrane to the outside compartments

Gas permeation: DPPC + Xe, 323K



Empty symbol--density profile at 10 ns
Filled symbol --density profile at 100 ns

Observation of Xe atom permeation through DPPC lipid membrane



CONCLUSIONS

- The Xe NMR chemical shift is exquisitely sensitive to the environment in which the Xe atom finds itself.
- Encoded in the ***intrinsic shielding response surface*** is the electronic structure of the system (a supermolecule or a crystal fragment) as a function of nuclear configuration.
- The ***dynamic averaging*** encodes further information about the nuclear environment into the observed chemical shift.
- It is possible to use a combination of ***quantum mechanical calculations and grand canonical Monte Carlo or MD simulations in model systems*** in order to understand the Xe chemical shifts. From such understanding may come some insight into the encoded information in more complex, real-world systems.

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Funding for CJJ's lab

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