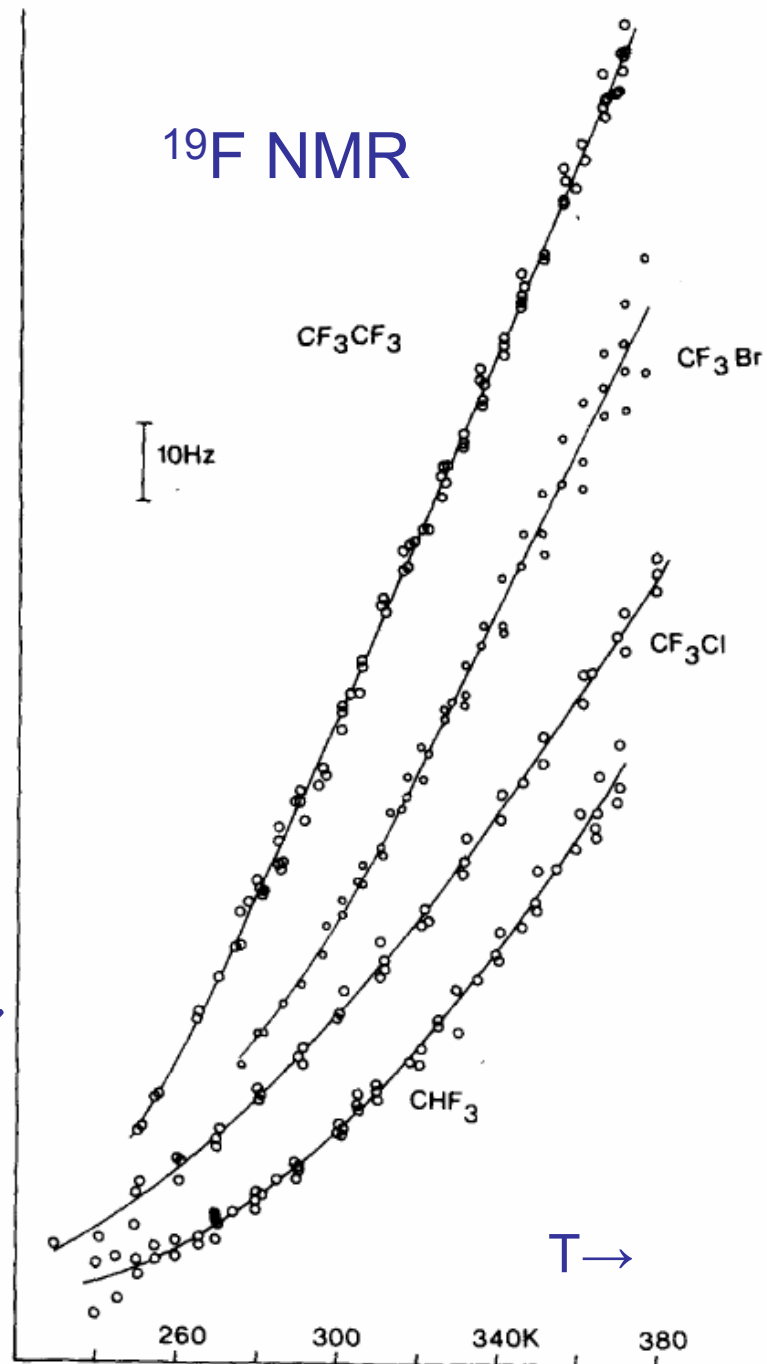


# *The temperature dependence of chemical shifts: mechanisms and contributions*

*Cynthia J. Jameson*

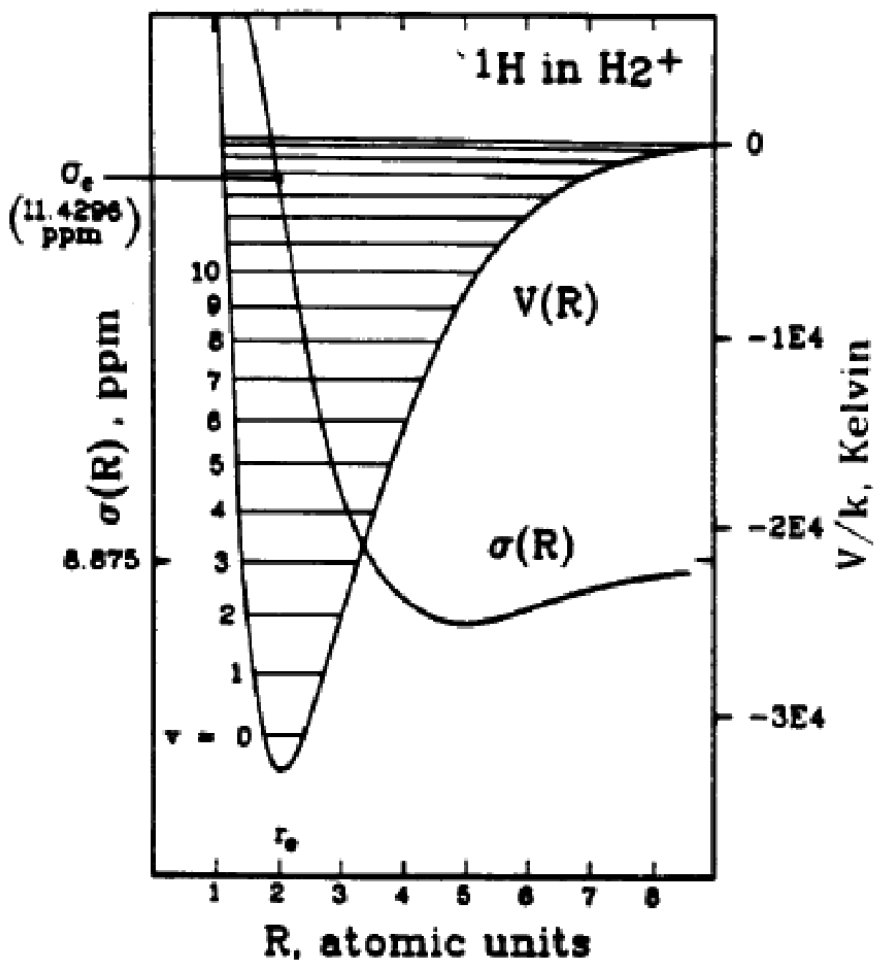
University of Illinois at Chicago



# outline

- the intramolecular shielding surface
- temperature dependence of the average chemical shift in an “isolated” diatomic molecule
- in an “isolated” polyatomic molecule
- temperature dependence of intermolecular chemical shifts in a constant volume homogeneous system
- temperature dependence of intermolecular chemical shifts in a constant pressure homogeneous system; the major contribution from expansion of the solvent
- temperature dependence in heterogeneous systems: one Xe in a cage; n Xe in a cage
- Xe in a channel; the major contribution from temperature dependence of the adsorption isotherm

# I. the intramolecular shielding surface



for  $\text{H}_2^+$  molecule  
the shielding function  
is known all the way  
from the value 8.875  
ppm at infinite  
separation through  
the 11.4296 ppm at  
the equilibrium  
geometry, and 35.5009  
ppm for the united  
one-electron atom,  $\text{He}^+$ .  
R. A. Hegstrom, Phys. Rev. A 19, 3  
17-30 (1979)

# Dynamic averages

To get the average value of a molecular electronic property:

$$\langle P \rangle_v = \int_{-\infty}^{+\infty} |\Psi_v(\mathbf{x})|^2 P(\mathbf{x}) d\mathbf{x}$$

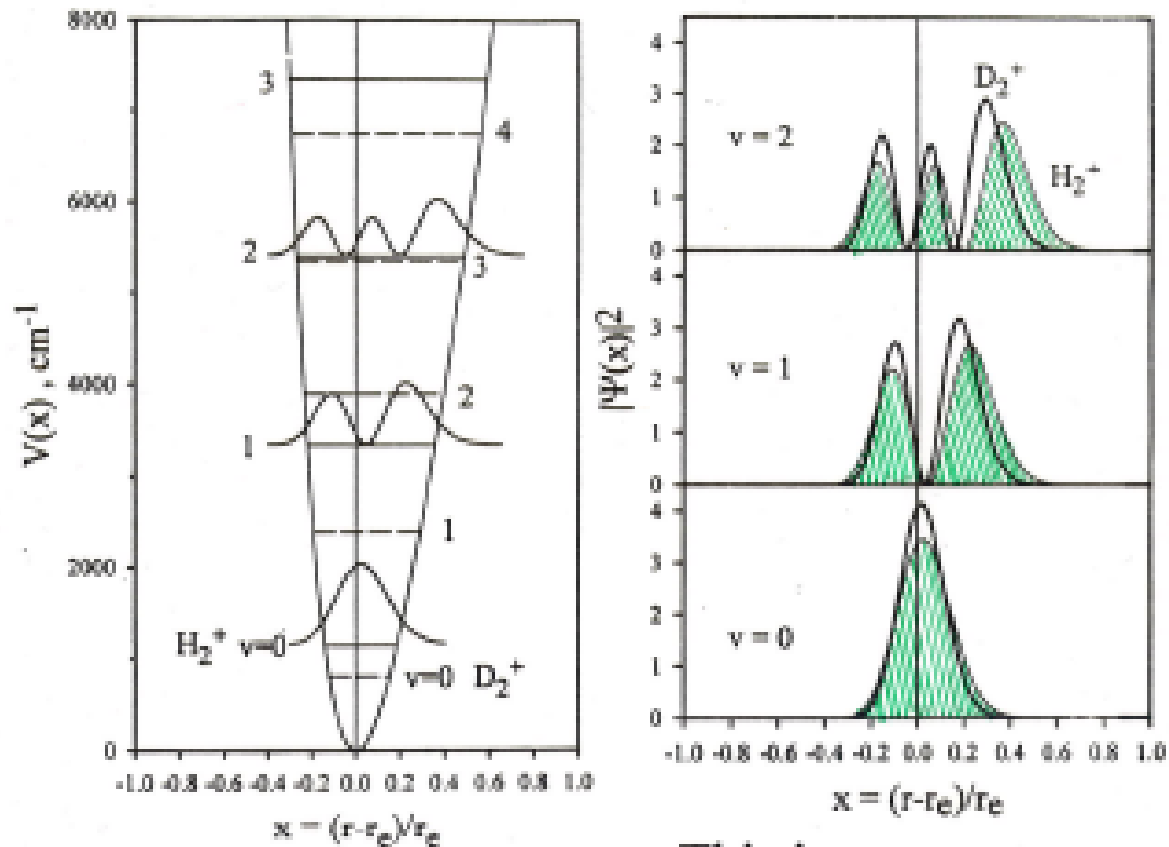
We can also find the rotational average.  
The thermal average is

$$\langle P \rangle^T = \frac{\sum_{v,J,K} (2J+1) g_{N_s} \langle P \rangle_{vJK} \exp(-E_{vJK}/kT)}{\sum_{v,J,K} (2J+1) g_{N_s} \exp(-E_{vJK}/kT)}$$

We can see that the low frequency vibrations are important, but also those vibrational modes that have large  $\langle P \rangle_{vJ}$

# H<sub>2</sub><sup>+</sup> vibrational wavefunctions

The probability of finding a molecule at a given nuclear configuration is given by  $|\Psi_{\text{vib}}|^2$ .



This is mass-dependent.

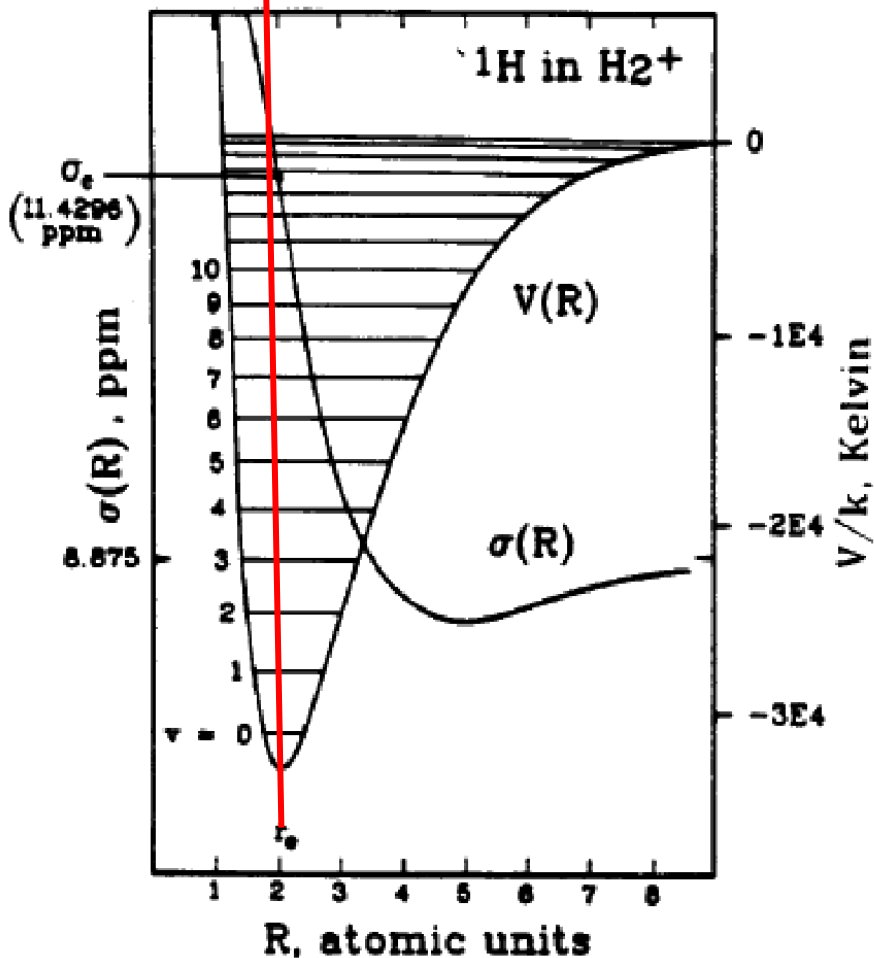
# vibrational averaging occurs around the equilibrium bond distance

- For a given  $v, J$  state, the averaging weights the **extended bond** values of shielding more than the compressed bond values of shielding because of
    - (a) anharmonicity of the vibration
    - (b) centrifugal stretching
- That is, the average bond length is longer than the equilibrium bond length, becoming more pronounced at higher  $v$  levels.
- Going to **higher temperatures** weights the higher vibrational levels more, thus **shifting further away from the shielding value at the equilibrium bond length.**

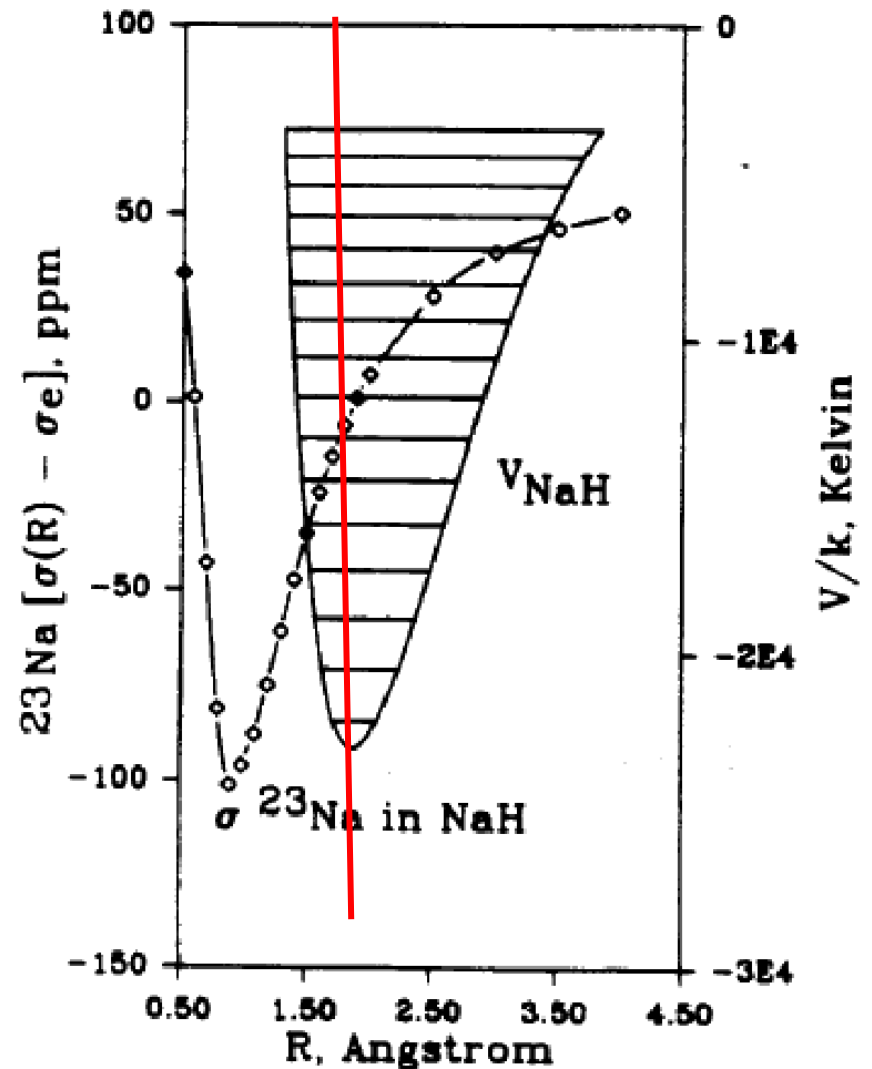
# the temperature coefficient of the chemical shift

- sign will depend on the sign of the derivative of the shielding function at the equilibrium geometry
- magnitude will depend on the magnitude of the derivative of the shielding function at the equilibrium geometry and the anharmonicity of the vibration

in the vicinity of the equilibrium geometry



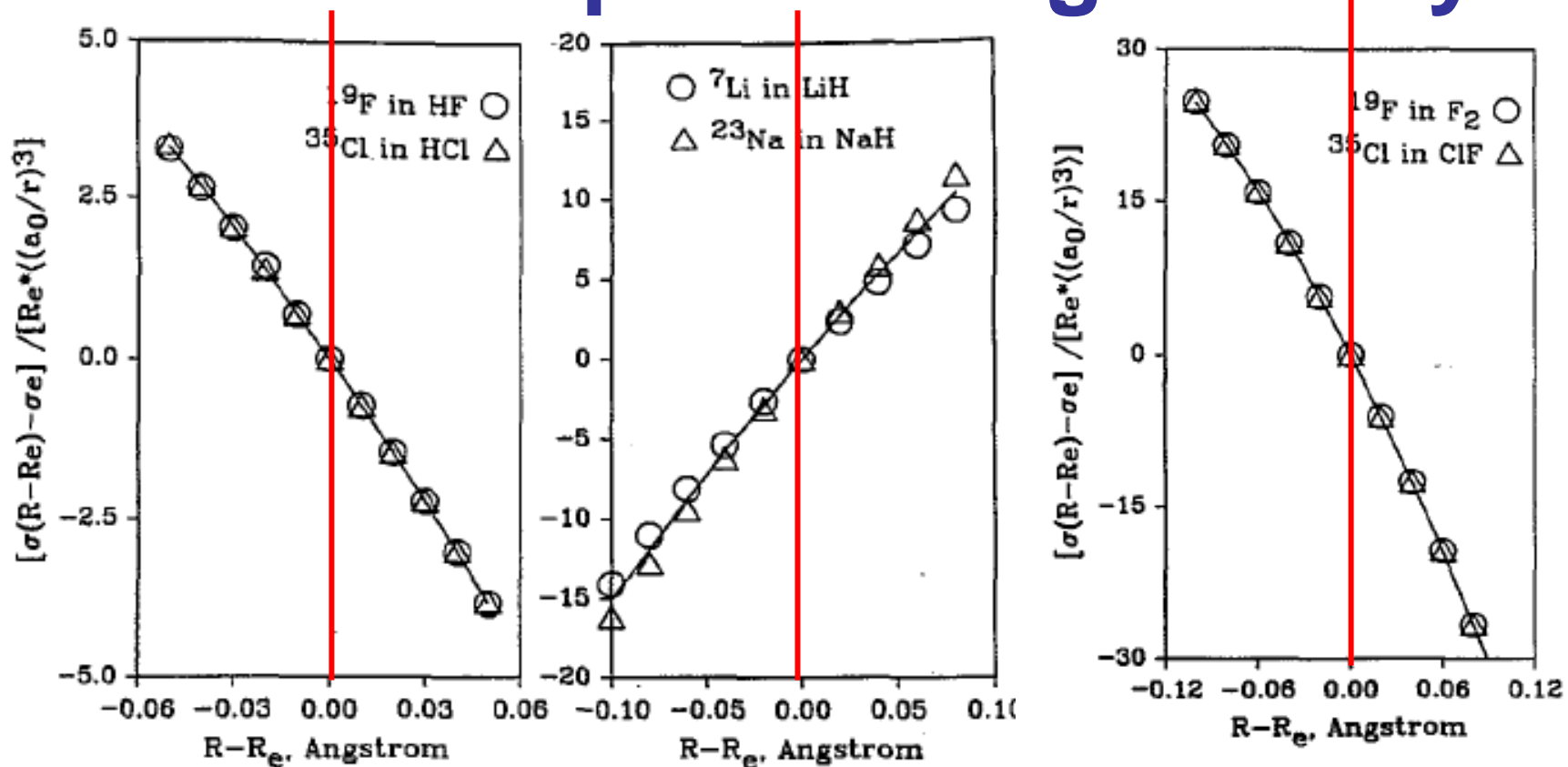
proton becomes less shielded with increasing bond length



$^{23}\text{Na}$  becomes more shielded with increasing bond length<sup>8</sup>



# shielding changes in the vicinity of the equilibrium geometry



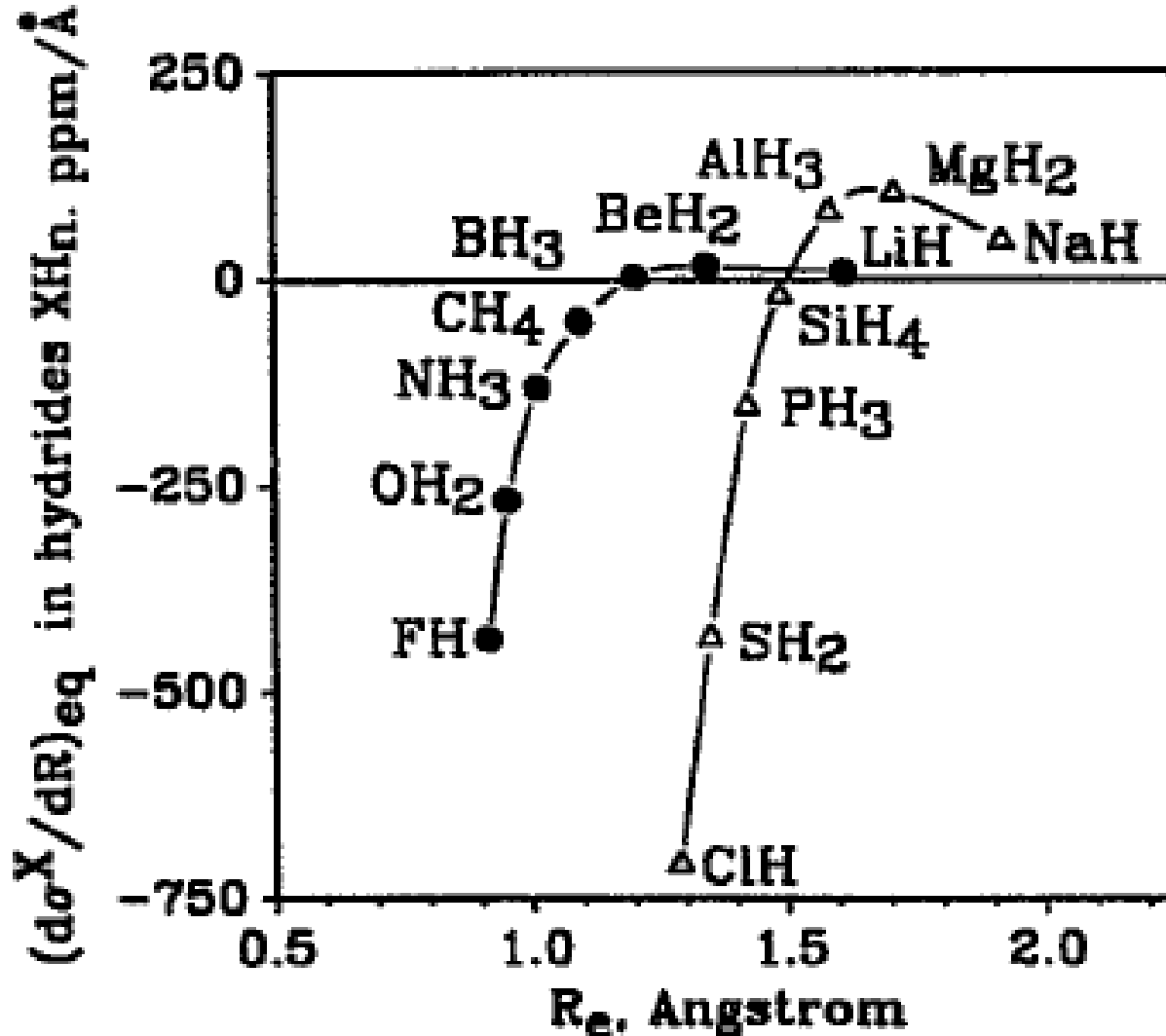
HF, HCl,

LiH, NaH,

$\text{F}_2$ , ClF

scaling permits direct comparison of F with Cl, Li with Na,

# compare shielding derivatives across the Periodic Table

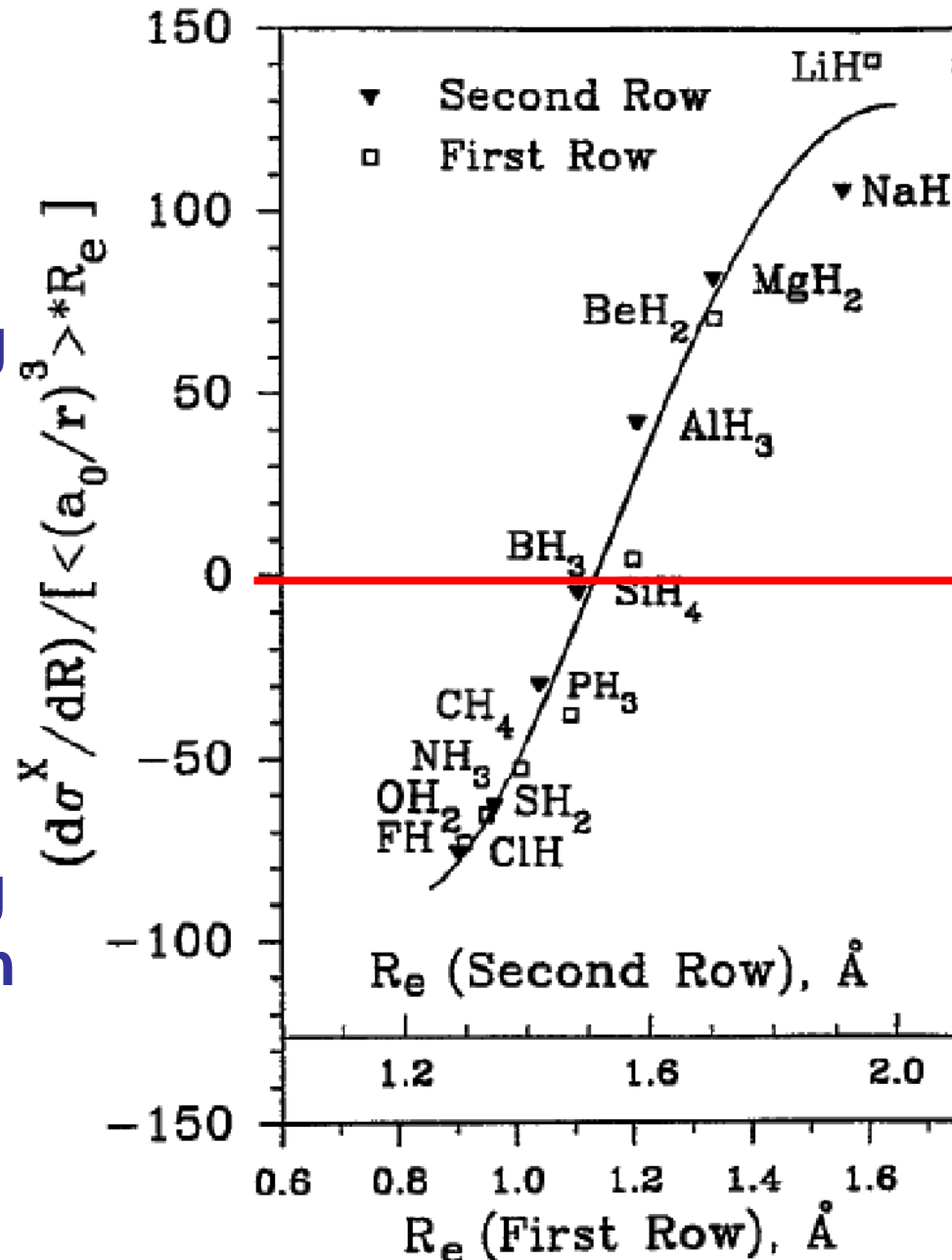


# scaling places first and second row on same graph

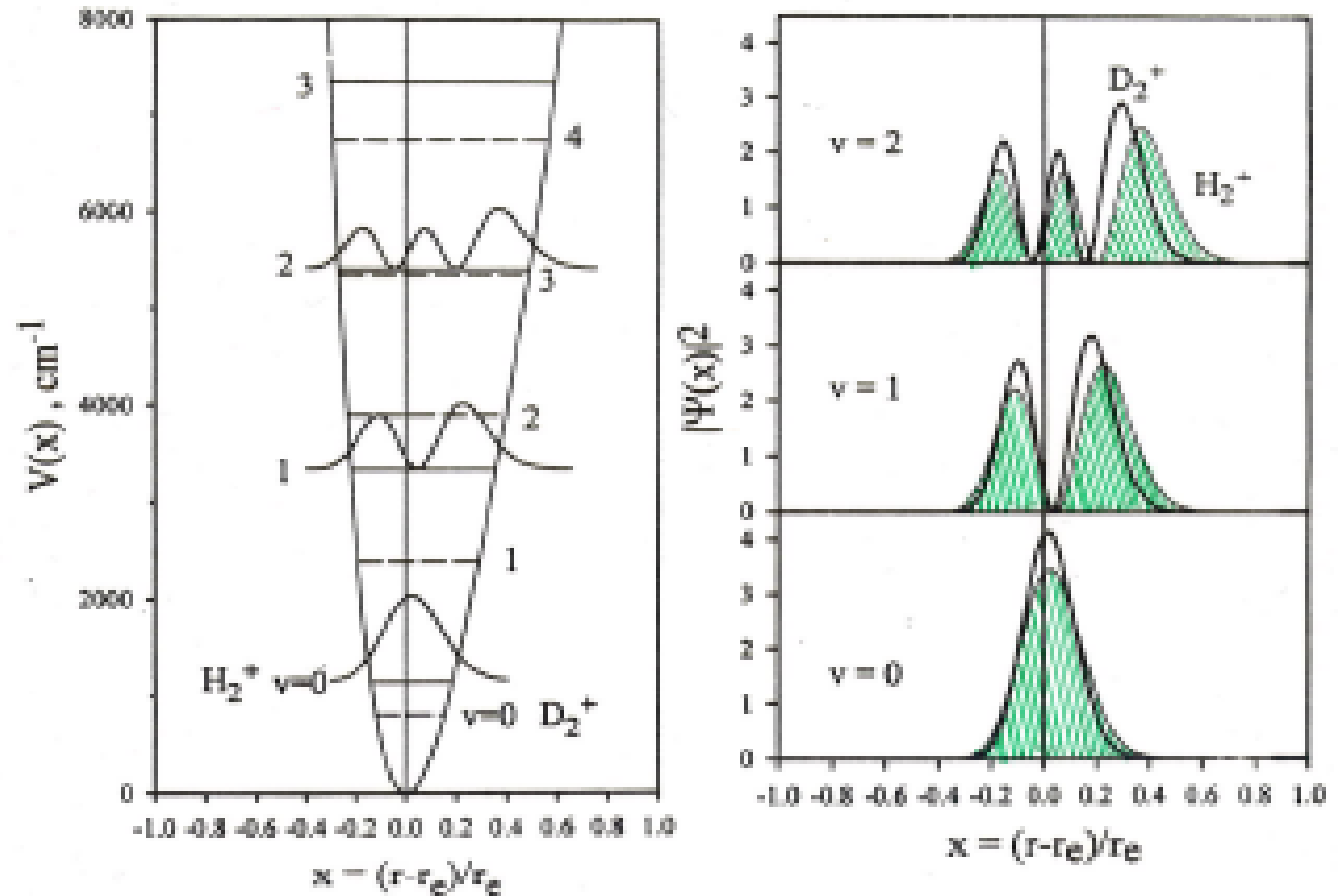
greater shielding with bond stretch leads to **decreasing chemical shift with increasing T**

---

less shielding with bond stretch leads to **increasing chemical shift with increasing T**

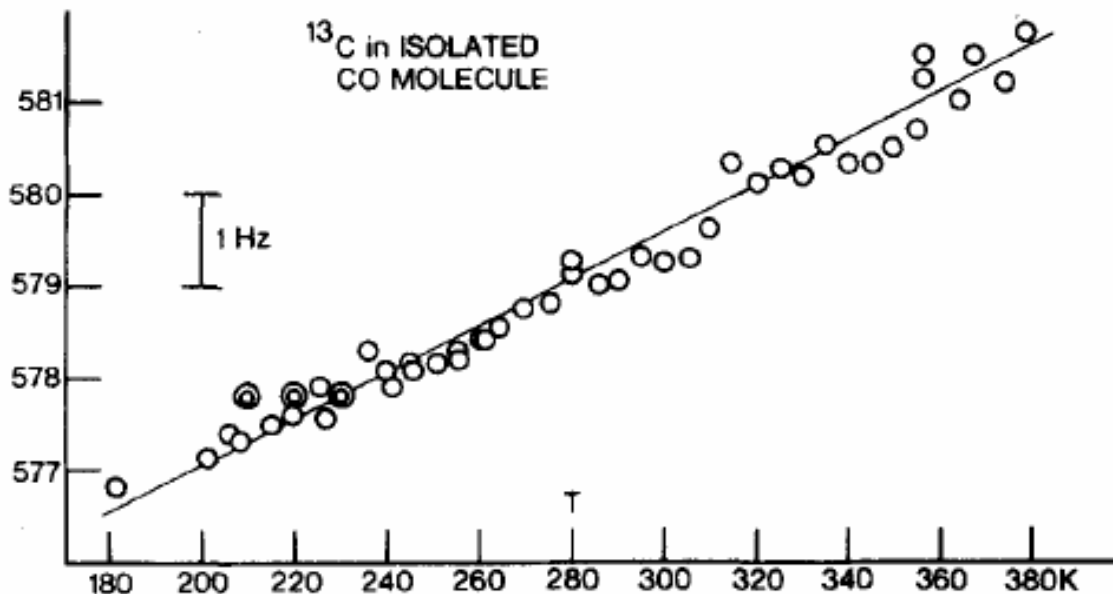


sign of chemical shift with lighter atom substitution is same as with increasing temperature, both correspond to greater average bond lengths



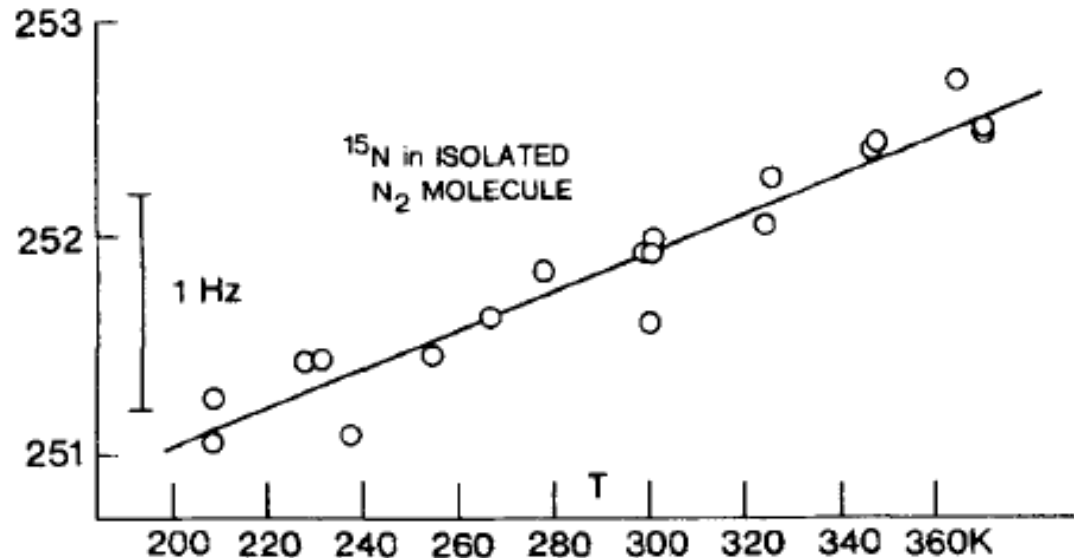
# **II. T dependence of chemical shift in an isolated diatomic molecule**

# $^{13}\text{C}$ in isolated CO molecule



increasing chemical shift with increasing T

# $^{15}\text{N}$ in isolated $\text{N}_2$ molecule



increasing chemical shift with increasing T

# diatomic molecule rovib averaging

$$\xi = (R - R_e)/R_e \text{ is }^{32}$$

$$\sigma(\xi) = \sigma_e + (d\sigma/d\xi)_e \xi + \frac{1}{2} (d^2\sigma/d\xi^2)_e \xi^2 + \dots$$

$$\xi_{v,J} = -3a_1(B_e/\omega_e) (v + \frac{1}{2}) + 4(J^2 + J) (B_e/\omega_e)^2$$

$$\xi_{v,J}^2 = 2(B_e/\omega_e) (v + \frac{1}{2}) , \quad a_1 = -[1 + (\alpha\omega_e/6B_e^2)]$$

$$\langle v + \frac{1}{2} \rangle = \frac{1}{2} \coth(hc\omega_e/2kT)$$

$$\langle J^2 + J \rangle = kT/hcB_e ,$$

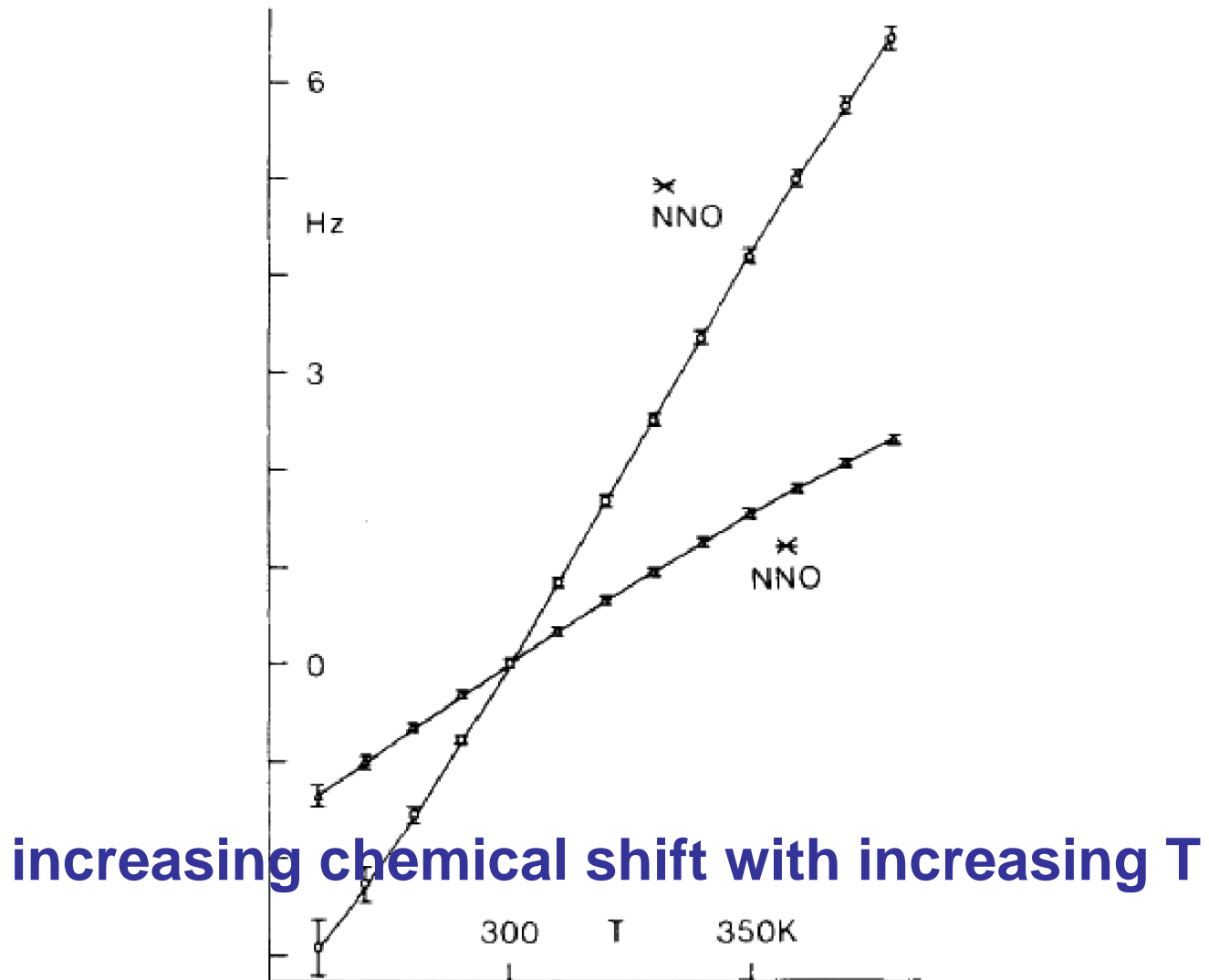
$$\begin{aligned} \langle \sigma \rangle^T - \langle \sigma \rangle^{300} &= (B_e/2\omega_e) [(d^2\sigma/d\xi^2)_e - 3a_1(d\sigma/d\xi)_e] \\ &\quad \times [\coth(hc\omega_e/2kT) - \coth(hc\omega_e/2k300)] \\ &\quad + (4k/hc) (B_e/\omega_e^2) (d\sigma/d\xi)_e (T - 300) . \end{aligned}$$



# III. an isolated polyatomic molecule

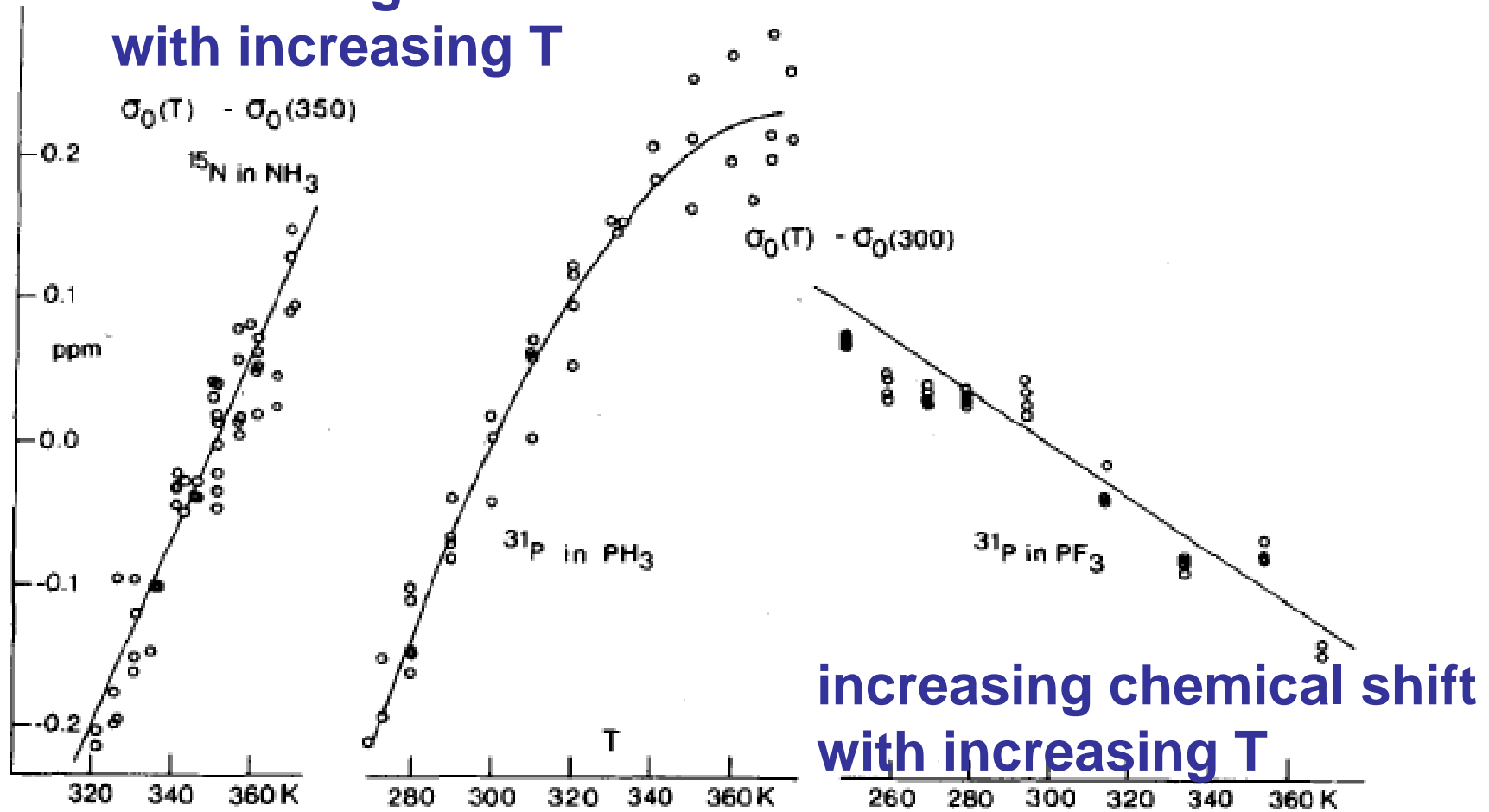
- experimental observations in samples of various known densities, followed by extrapolation to zero density finds a temperature dependence that is intrinsic to an isolated molecule

# $^{15}\text{N}$ in isolated NNO molecule



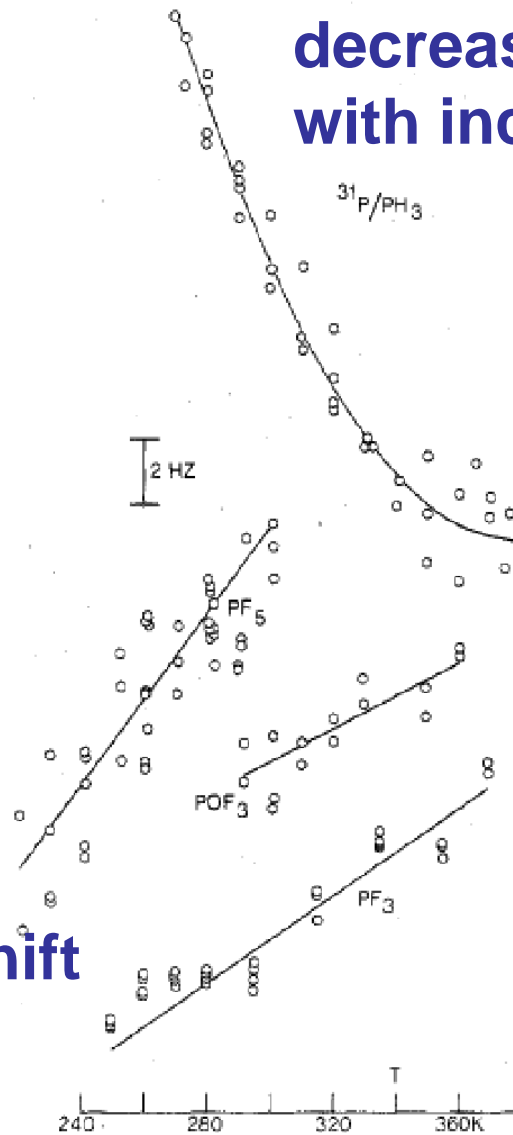
# $^{15}\text{N}$ in $\text{NH}_3$ , $^{31}\text{P}$ in $\text{PH}_3$ and $\text{PF}_3$ isolated molecules

decreasing chemical shift  
with increasing T



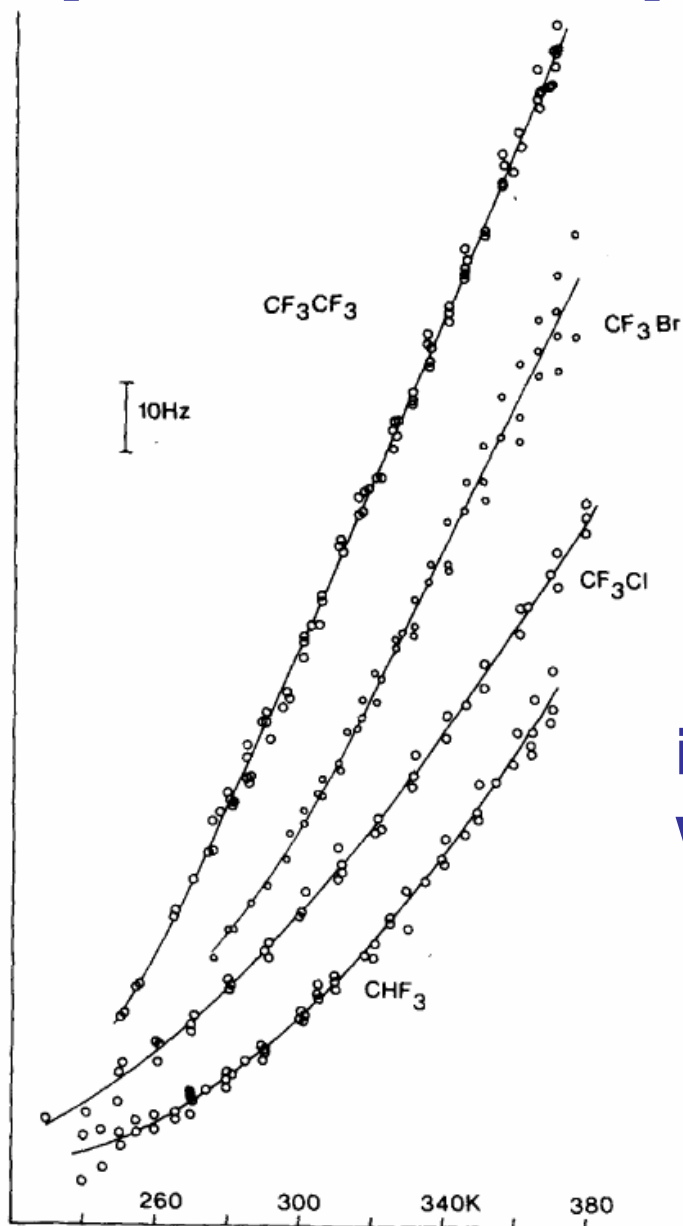
# $^{31}\text{P}$ in isolated molecules

decreasing chemical shift  
with increasing T



increasing chemical shift  
with increasing T

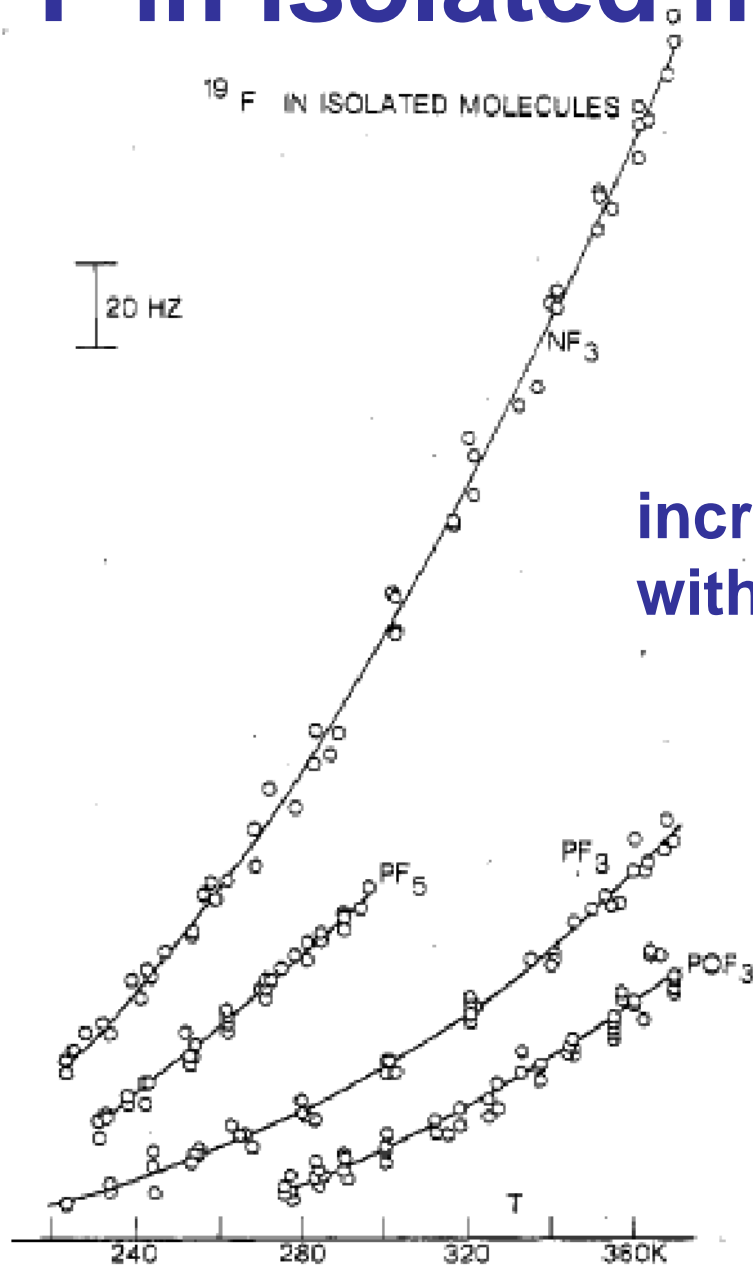
# Temperature dependence of $^{19}\text{F}$



fluoroalkanes

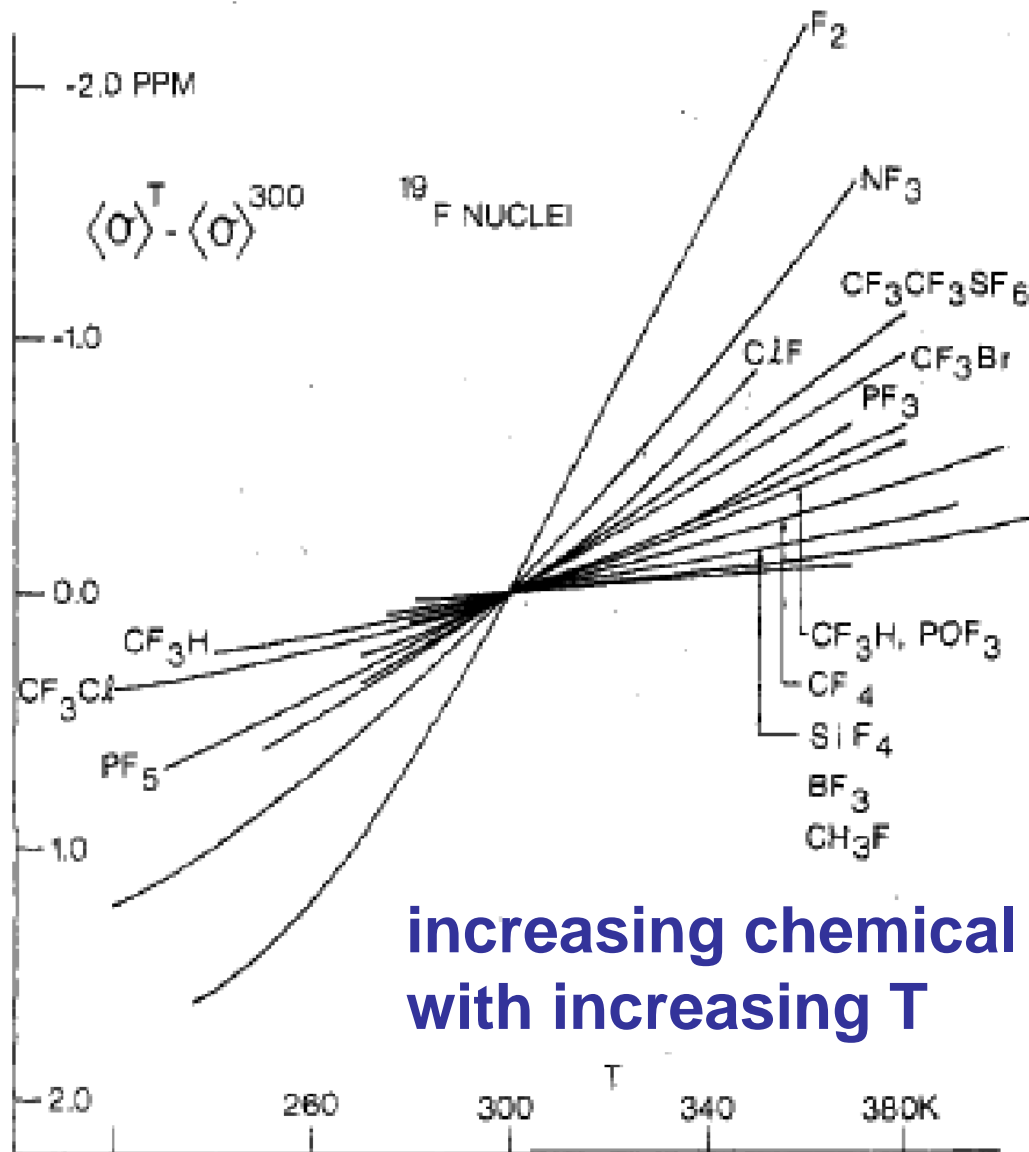
increasing chemical shift  
with increasing T

# $^{19}\text{F}$ in isolated molecules

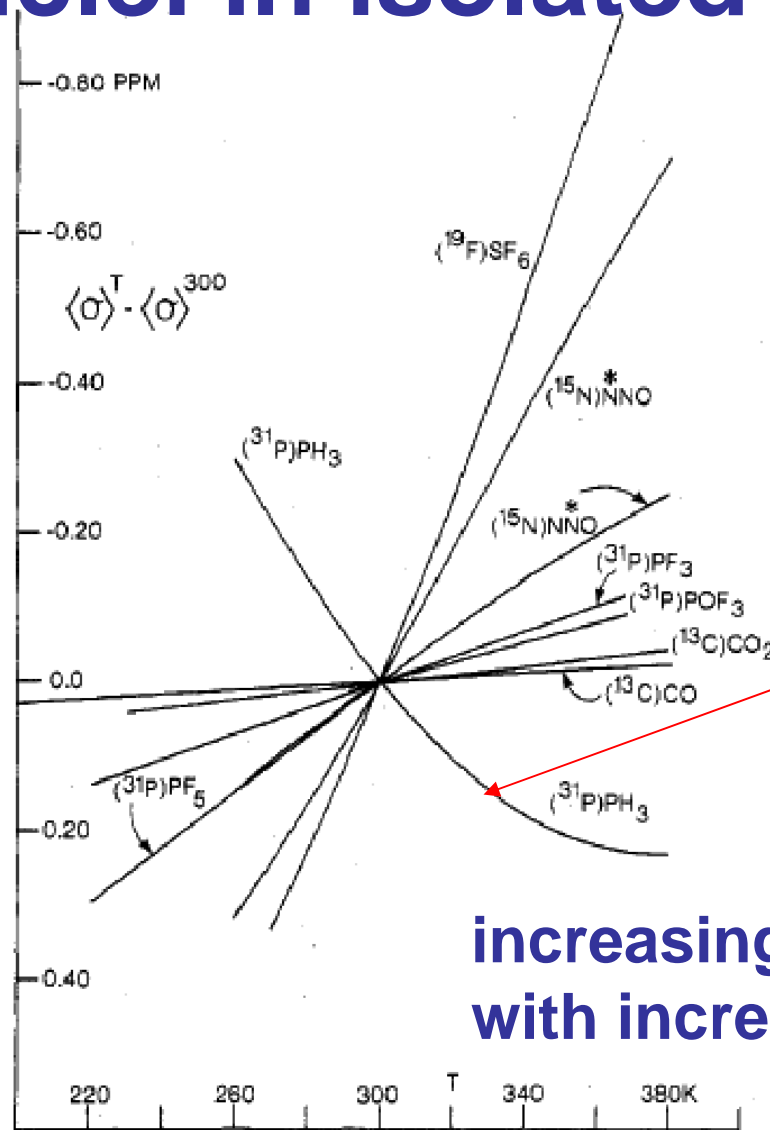


increasing chemical shift  
with increasing T

# Temperature dependence of $^{19}\text{F}$



# various nuclei in isolated molecules



but not for  
 $^{31}\text{P}$  in  $\text{PH}_3$

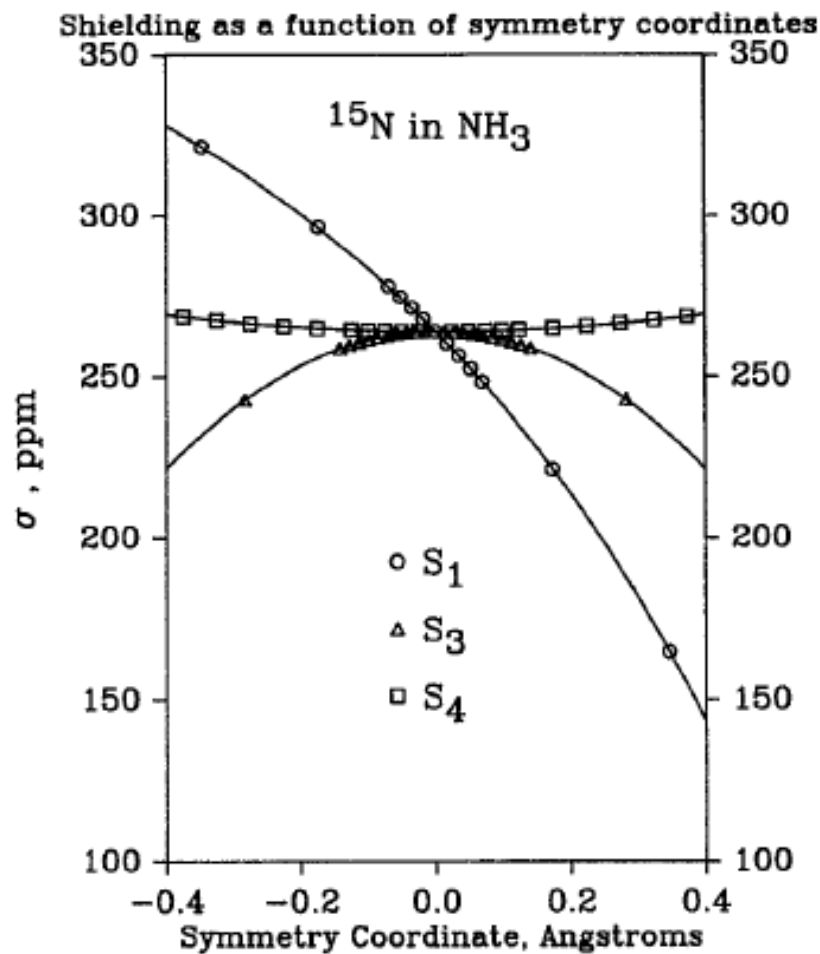
increasing chemical shift  
with increasing T



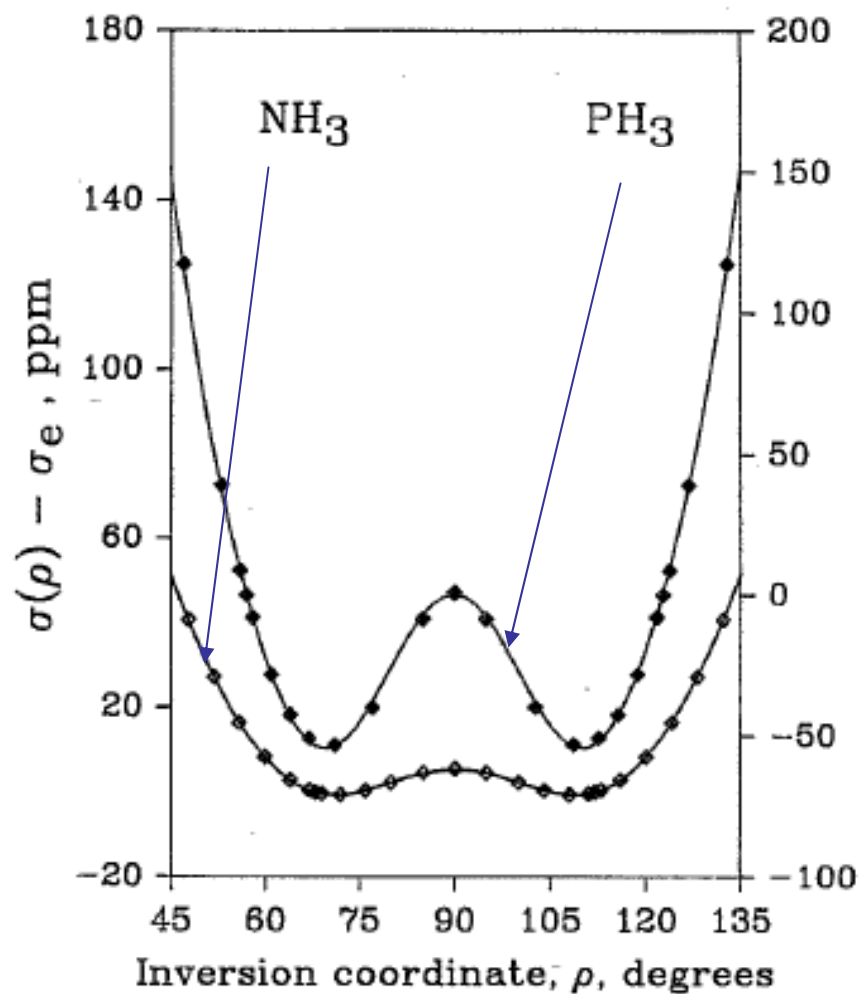
# quantum mechanical calculations of shielding surfaces in polyatomic molecules

- $\text{NH}_3$ ,  $\text{PH}_3$
- $\text{CH}_4$ ,  $\text{OH}_2$

# $^{15}\text{N}$ shielding surface in $\text{NH}_3$ molecule

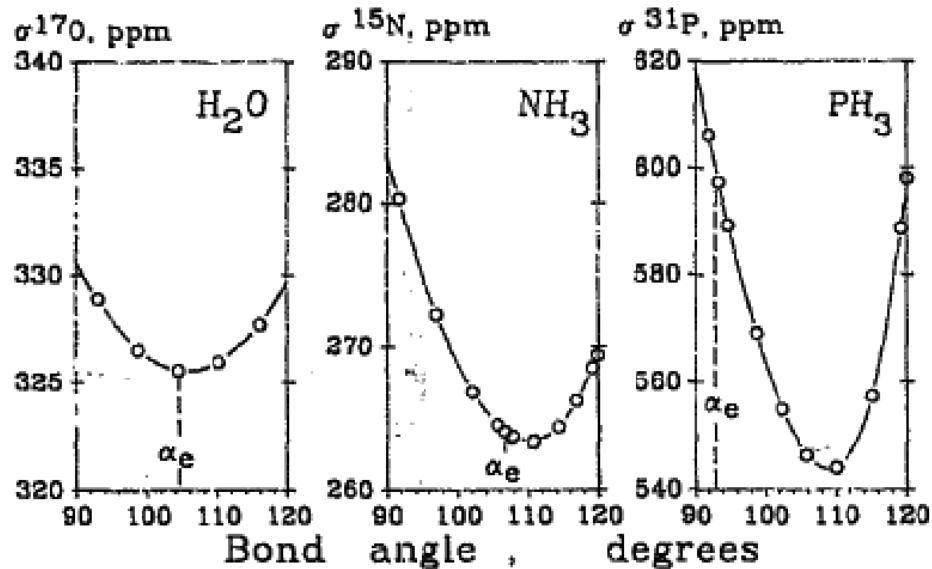
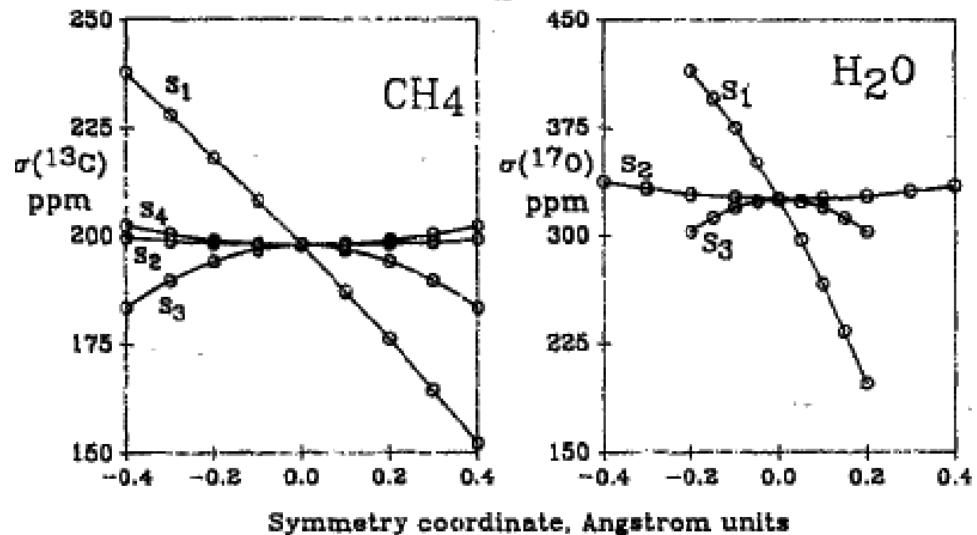


# $^{15}\text{N}$ and $^{31}\text{P}$ shielding function of the inversion coordinate in $\text{NH}_3$ and $\text{PH}_3$



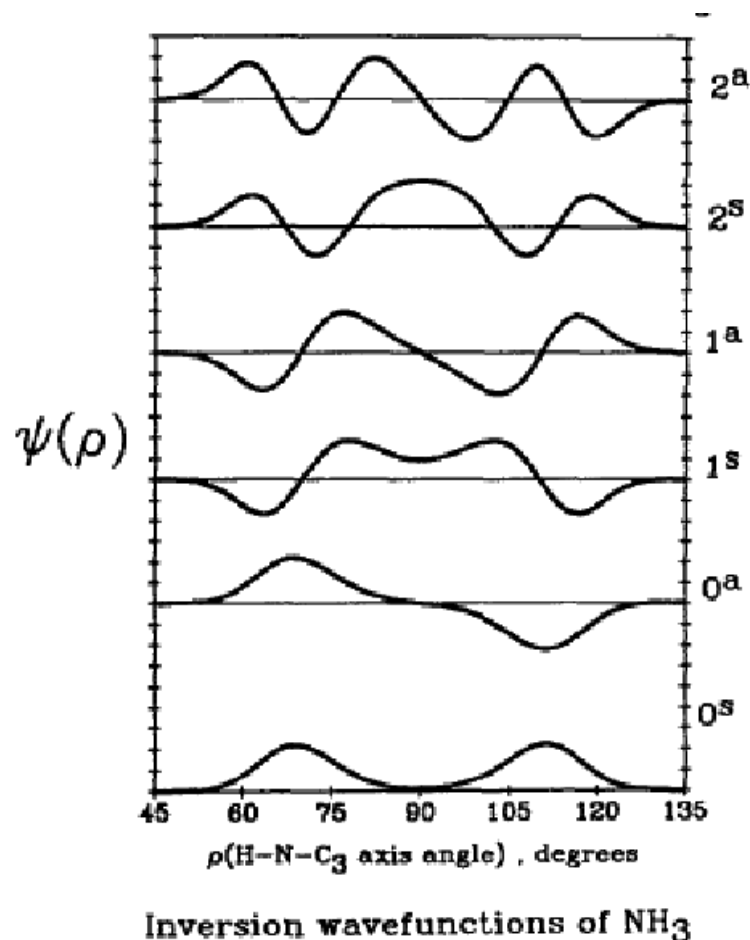
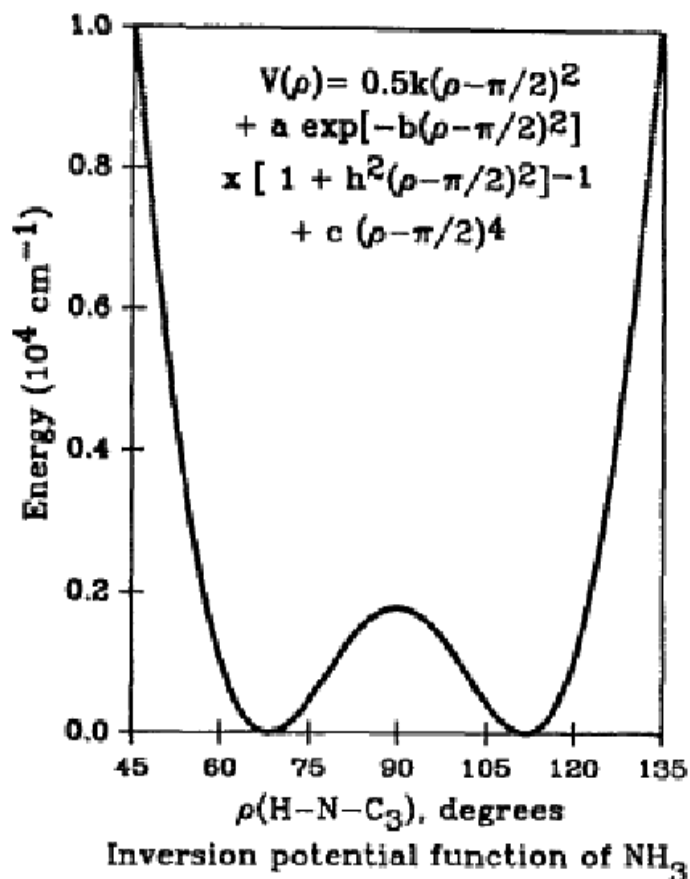
shielding surfaces for  $^{13}\text{C}$  in  $\text{CH}_4$ ,  $^{17}\text{O}$  in  $\text{H}_2\text{O}$  compared with  $^{15}\text{N}$  in  $\text{NH}_3$  and  $^{31}\text{P}$  in  $\text{PH}_3$

Shielding Traces

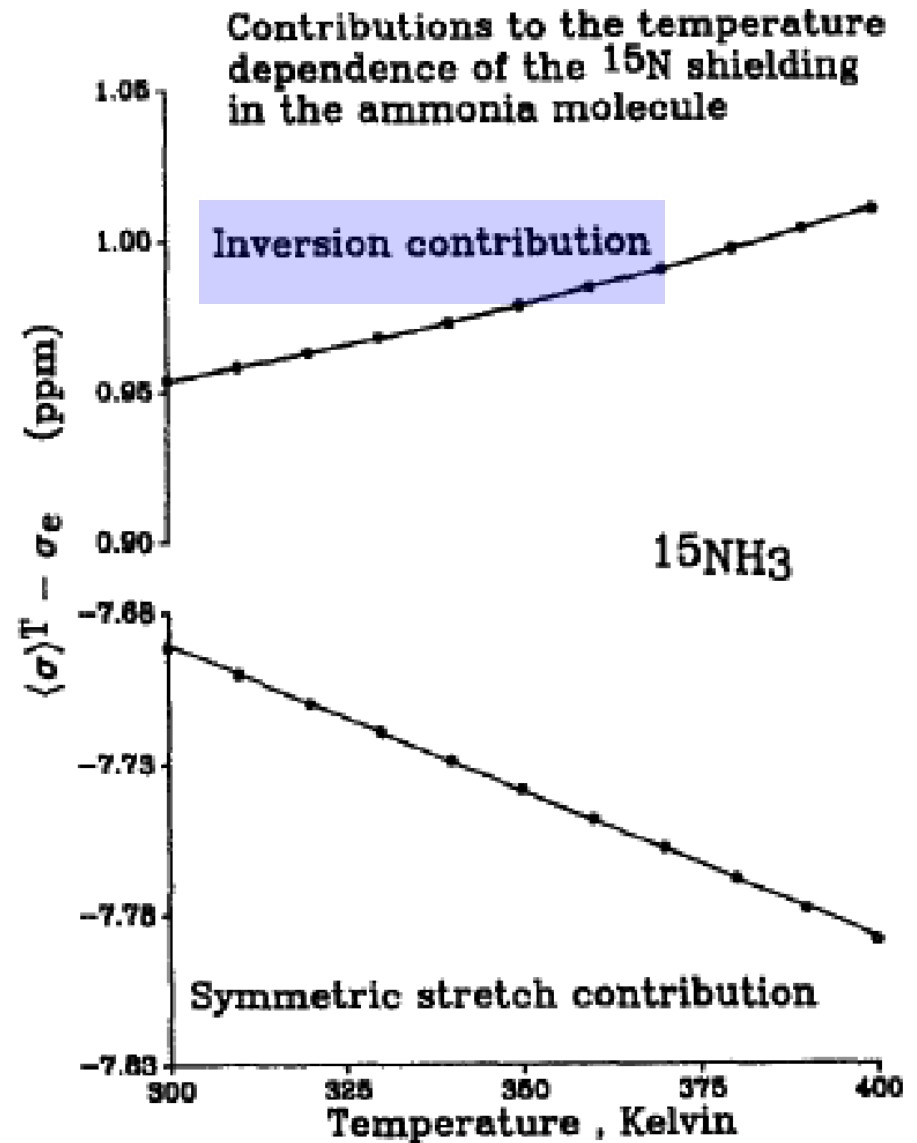


# dynamic averages in polyatomic molecules

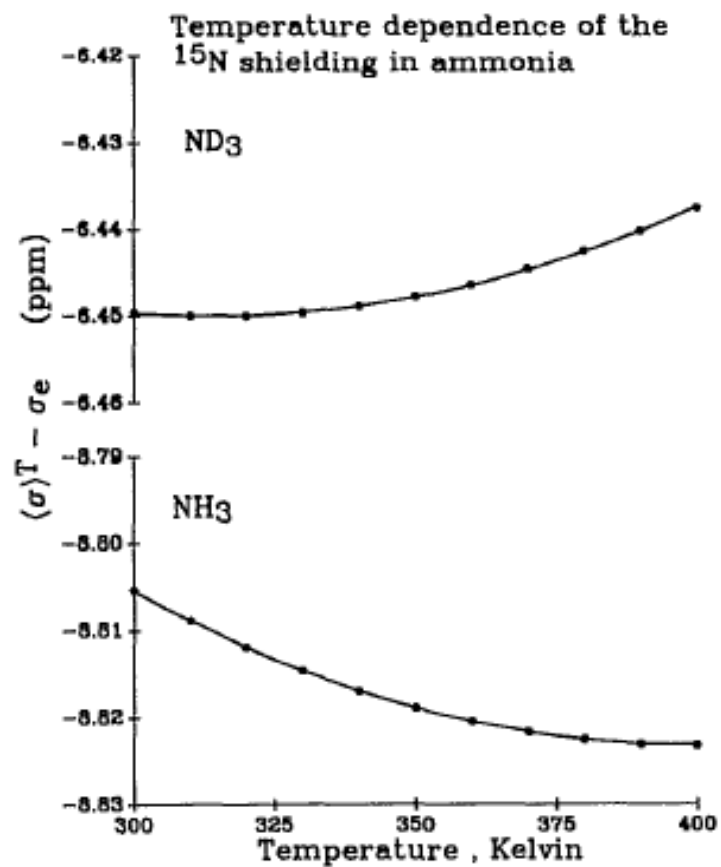
# the inversion potential and its wavefunctions for NH<sub>3</sub>



# calculated T dependence of $^{15}\text{N}$ shielding in $\text{NH}_3$

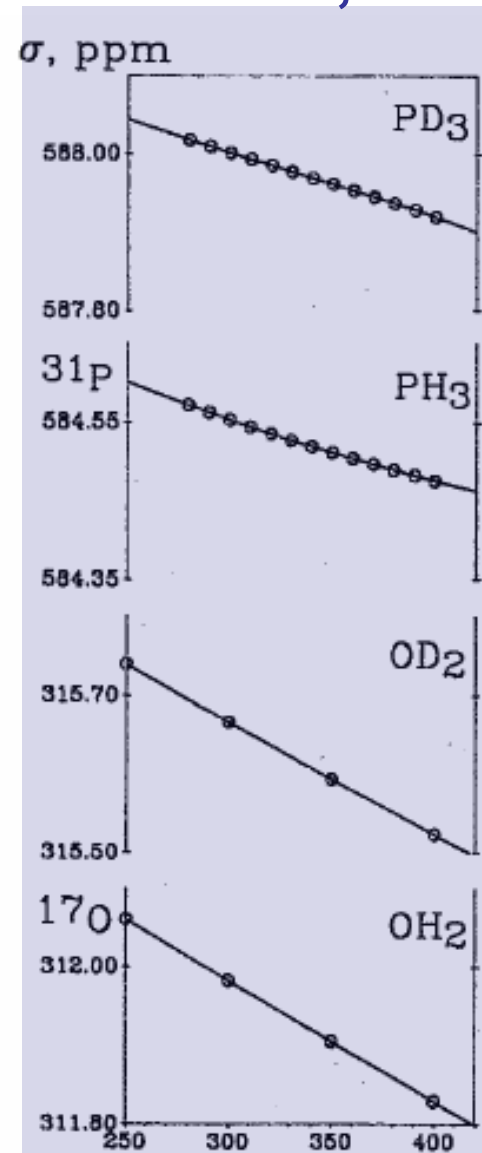
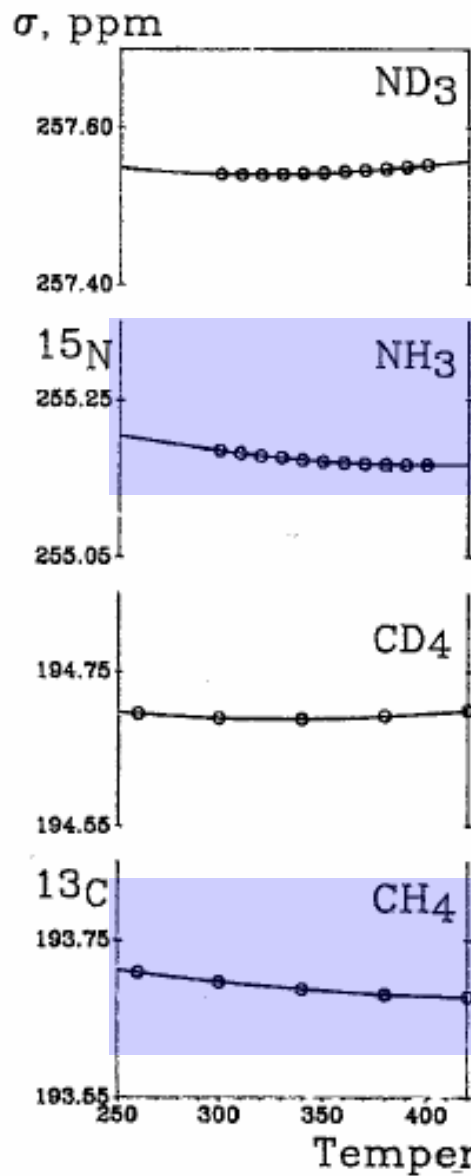


# calculated T dependence of $^{15}\text{N}$ shielding in $\text{NH}_3$ and $\text{ND}_3$





# calculated temperature dependence for $^{15}\text{N}$ , $^{13}\text{C}$ , $^{31}\text{P}$ , $^{17}\text{O}$



decreasing  
chemical shift  
with increasing T

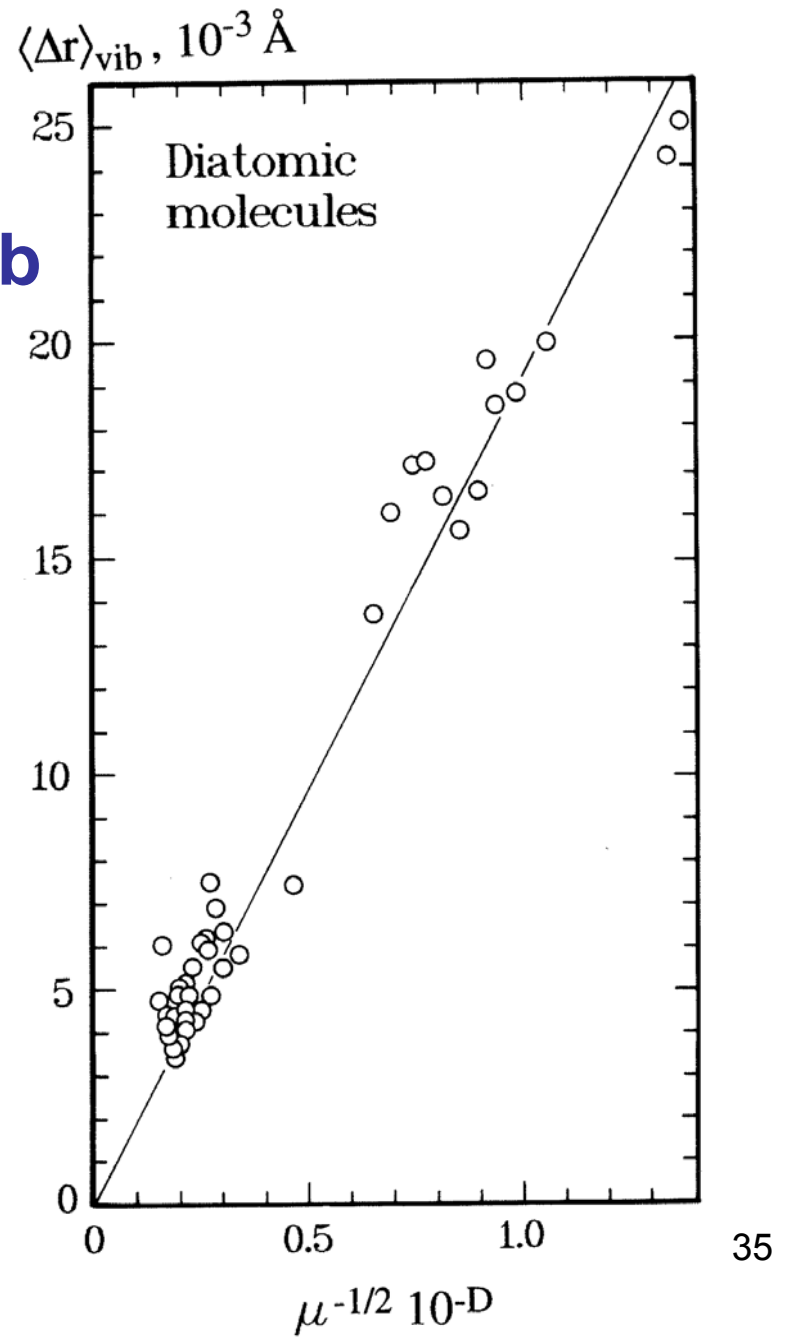
for “central”  
atoms the T  
dependence  
is not simple  
to calculate

# approximate analysis of $^{19}\text{F}$ temperature dependence

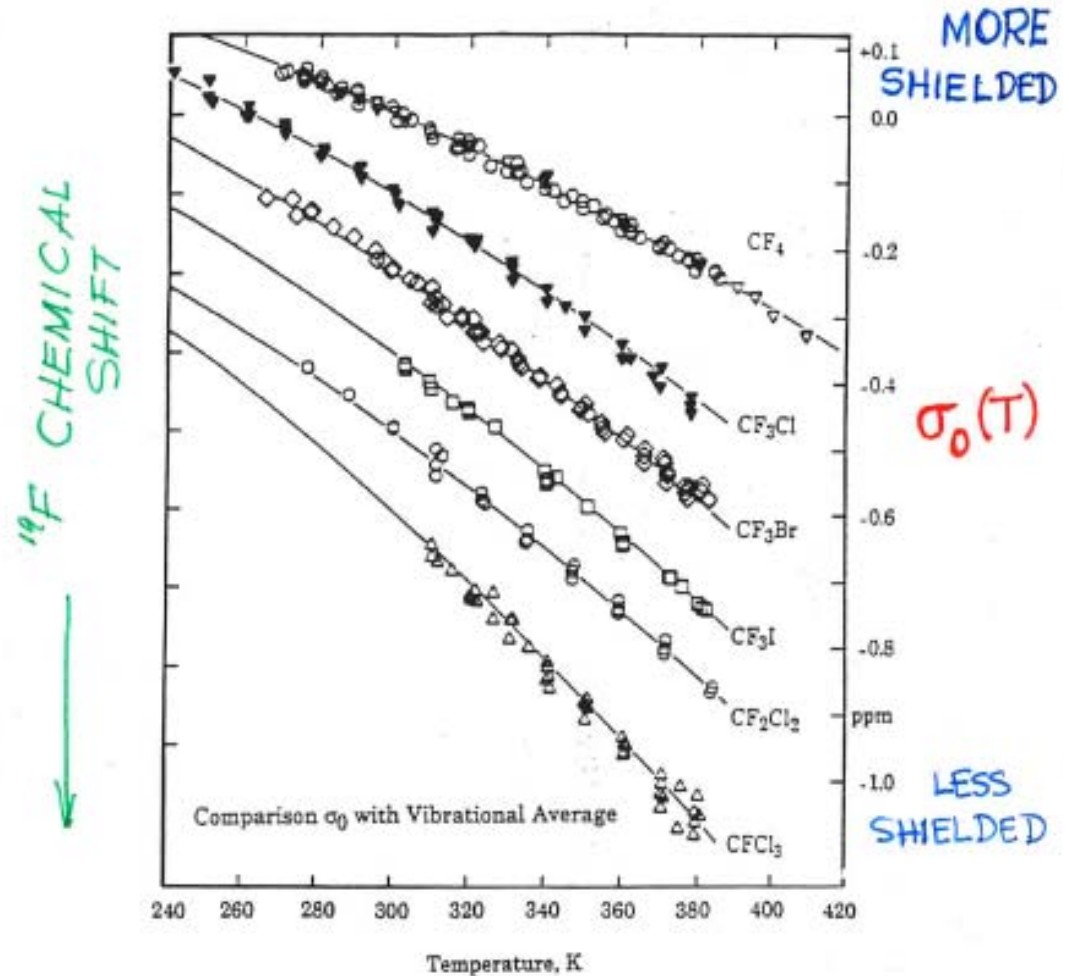
$$d\langle\sigma\rangle^{\text{T}}dT \simeq (\partial\sigma/\partial\Delta r)_e (d\langle\Delta r\rangle^{\text{T}}/dT) \\ + (\partial\sigma/\partial\Delta\alpha)_e (d\langle\Delta\alpha\rangle^{\text{T}}/dT) + \dots$$

for nuclei of any terminal atom in a molecule,  
there is one dominant bond stretch term and  
the angle deformation terms are less  
important

**can estimate  $\langle \Delta r \rangle_{\text{vib}}$**   
from position of two  
atoms in the Periodic  
Table using  
Herschbach and Laurie  
parameters



calculated temperature dependence of  $^{19}\text{F}$  using one parameter fit to isolated molecule data



$$d\langle\sigma\rangle^T dT \simeq (\partial\sigma/\partial\Delta r)_e (d\langle\Delta r\rangle^T / dT)$$

**When system is not an isolated molecule, temperature dependence of intermolecular interactions come into play.**

# IV. intermolecular shifts in a constant volume homogeneous system

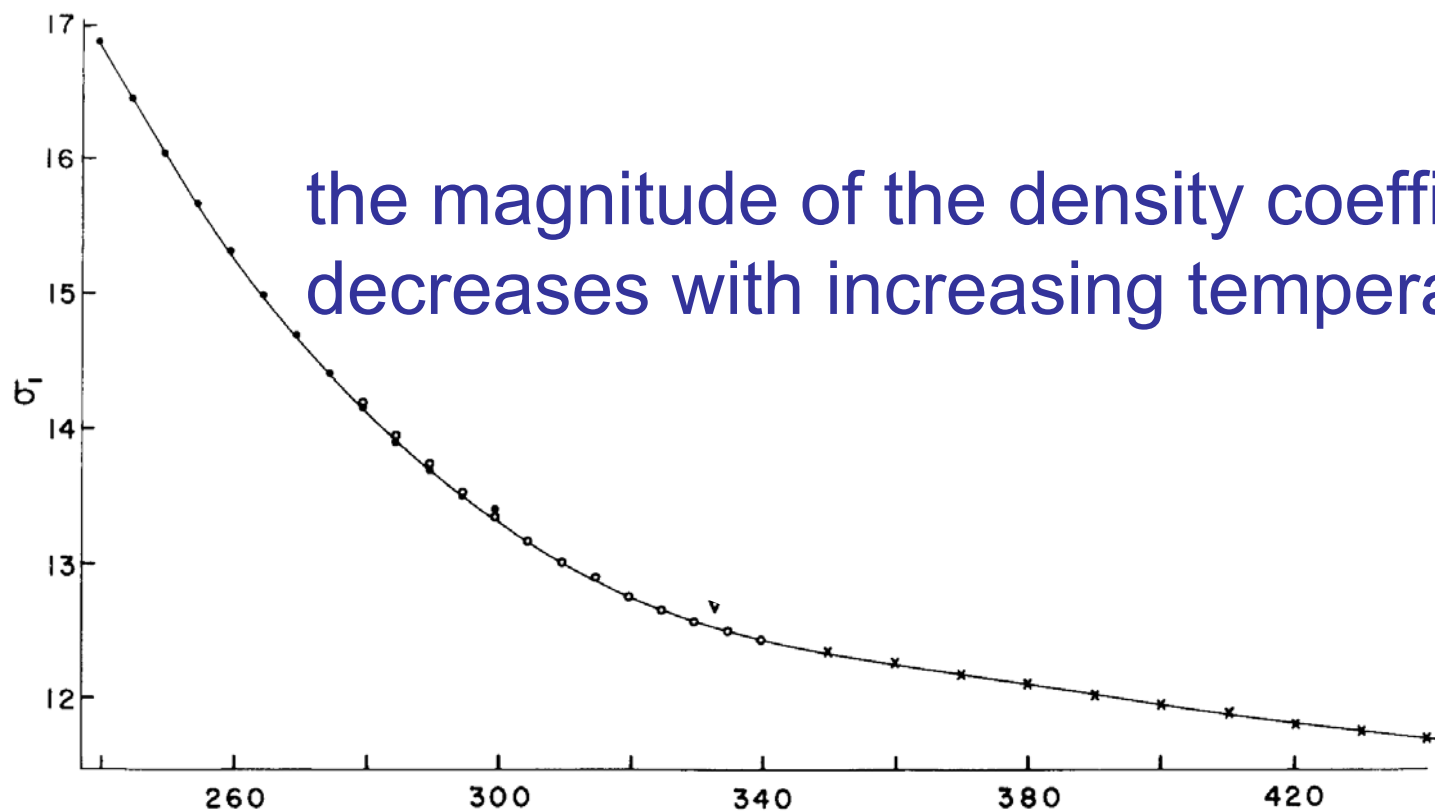
- In a sealed sample of fluid above the critical point or at  $T, \rho$  above the liquid-vapor equilibrium curve: the temperature dependence of the chemical shift comes entirely from that in the isolated molecule plus that due to the virial expansion of the shielding.

$$\sigma(T, \rho) = \sigma_0(T) + \sigma_1(T)\rho + \sigma_2(T)\rho^2 + \dots$$

(see 'Intermolecular Chemical Shifts' for details)

(usually) **increasing chemical shift with increasing density**

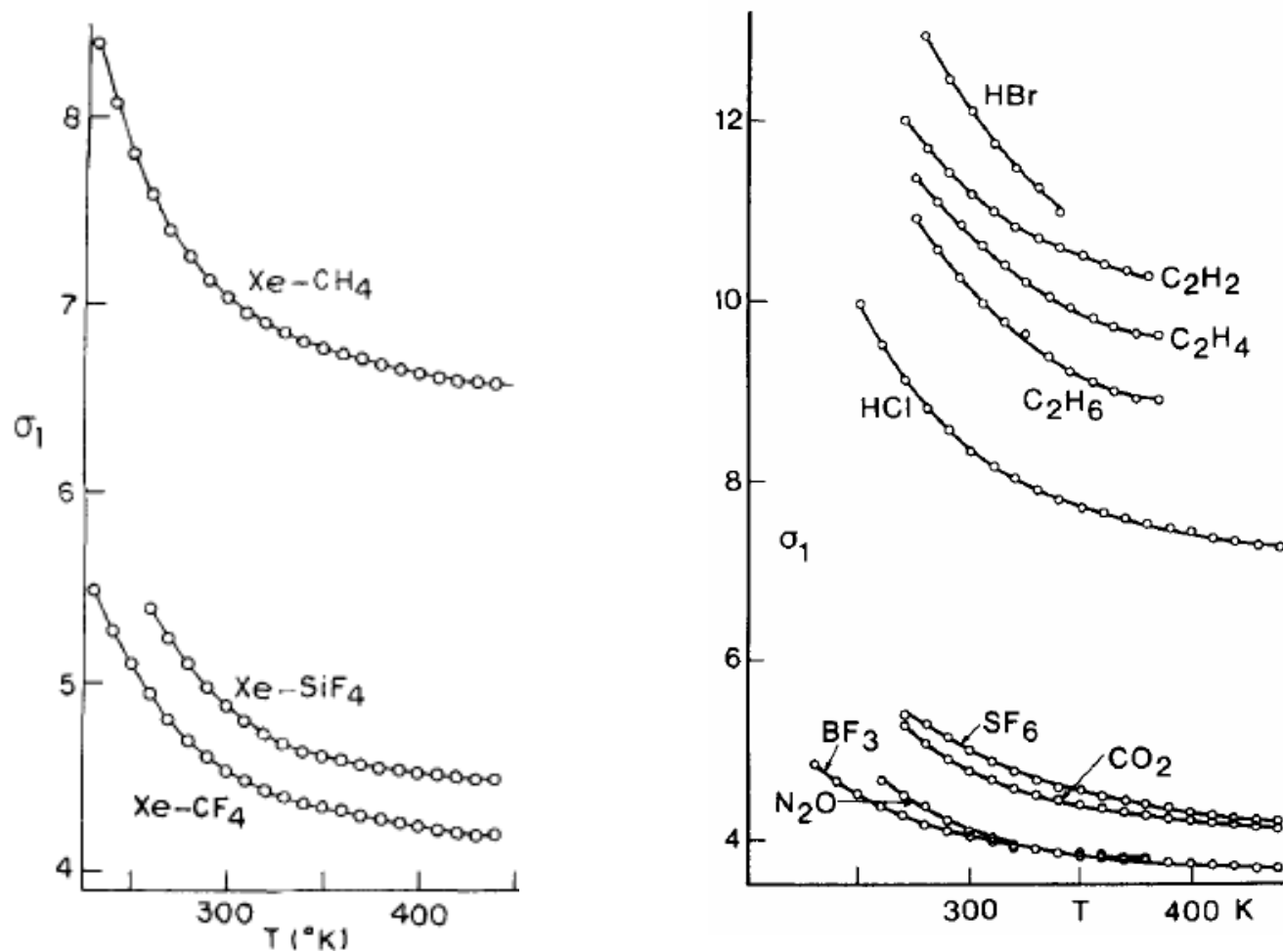
# density coefficient of the $^{129}\text{Xe}$ chemical shift, the second virial coefficient of shielding, $\sigma_1(T)$



the magnitude of the density coefficient decreases with increasing temperature.

Jameson et al. J. Chem. Phys. 59, 4540-4546 (1973).

# density coefficient of the $^{129}\text{Xe}$ chemical shift in various gases



Jameson et al. J. Chem. Phys. 65, 3401-3406 (1976);  
J. Chem. Phys. 66, 5226-5230 (1977).



# V. intermolecular shifts in a constant pressure homogeneous system

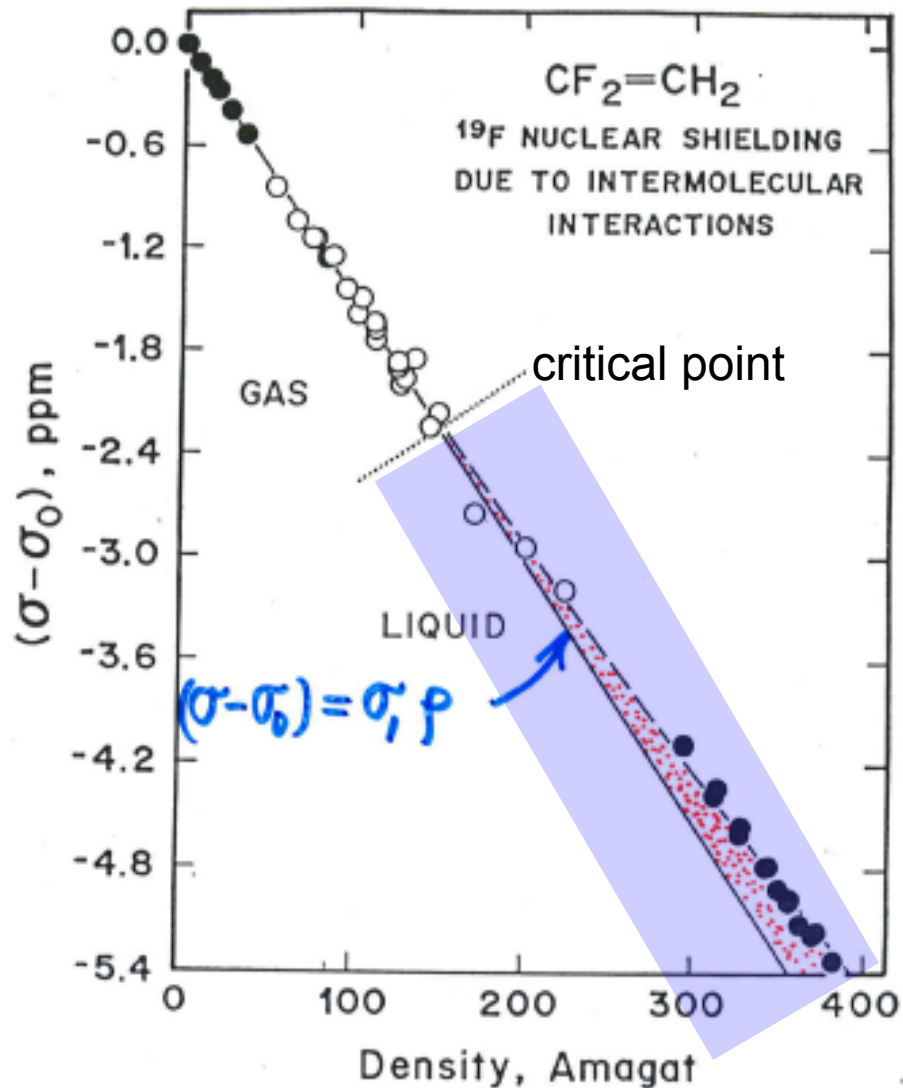
the major contribution from expansion of the liquid

$$\delta(T, \rho) \approx \delta_0(T) + \delta_{1\text{eff}}(T) \rho_{\text{LIQ}}(T) + \dots$$

where  $\rho_{\text{LIQ}}$  is the number density of molecules in the liquid and  $\delta_{1\text{eff}}(T)$  is the density coefficient of the chemical shift in cases where a linear dependence on density is observed.

$$^{19}\text{F} \quad \sigma(T, \rho) - \sigma_0(T) \approx \sigma_{1\text{eff}}(T) \rho_{\text{LIQ}}(T) + \dots$$

increasing chemical shift with increasing density

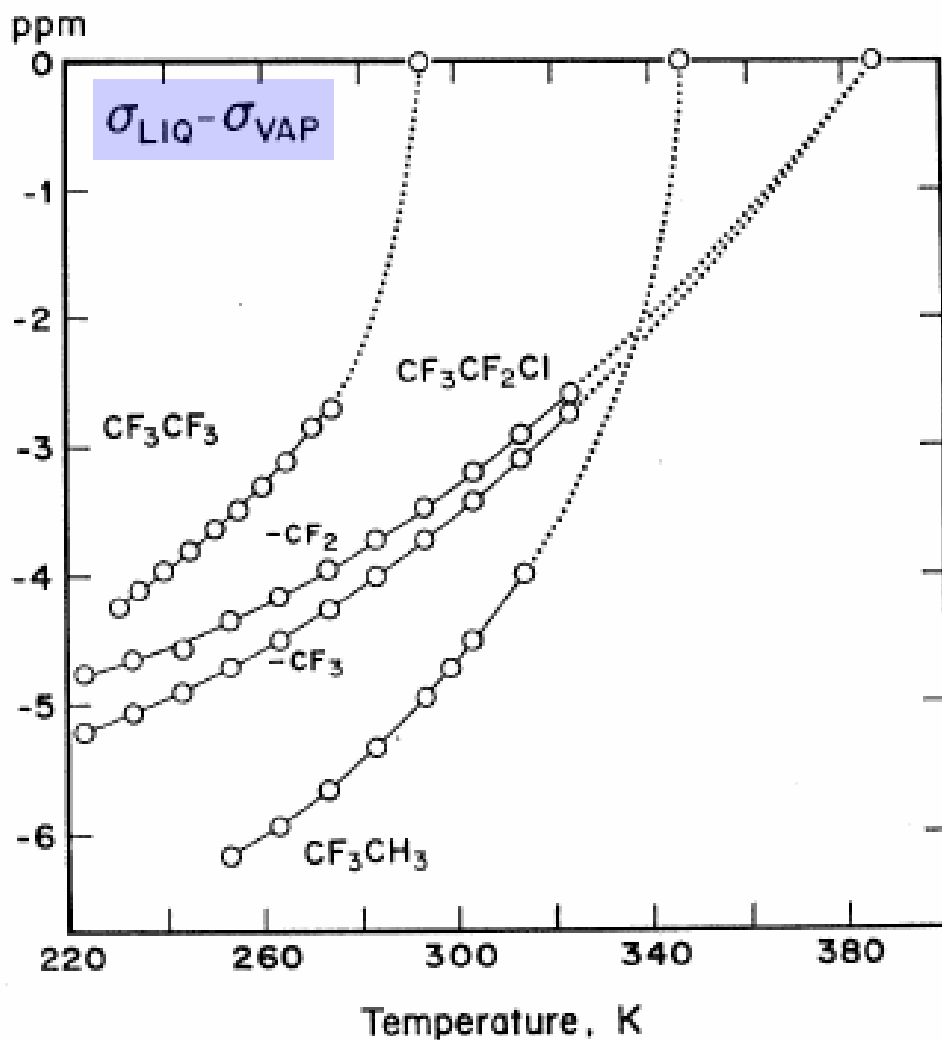
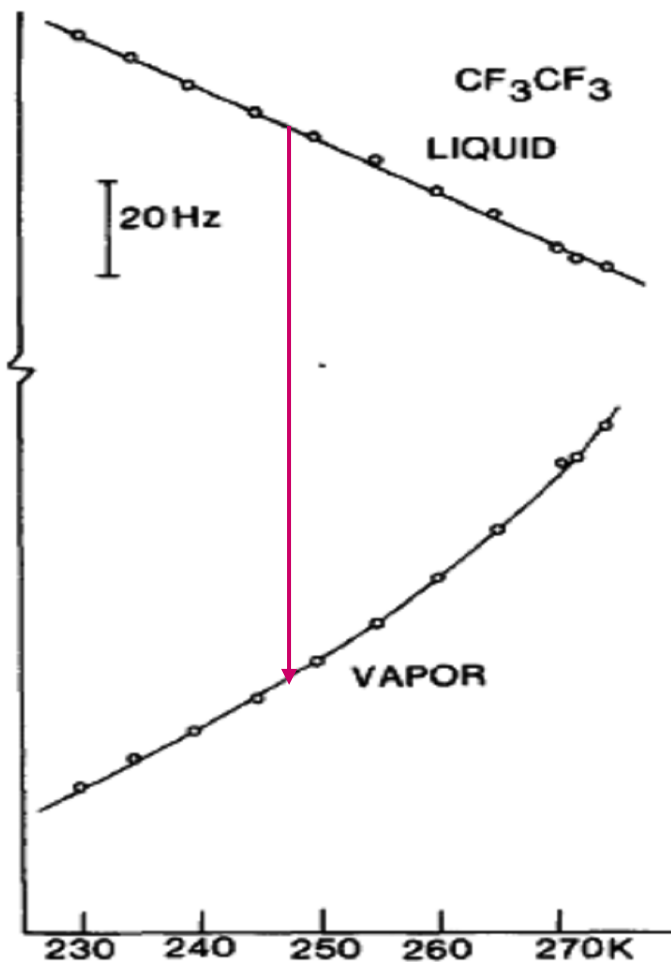


nearly linear  
dependence  
on density  
of liquid, but  
smaller slope

from gas to liquid shifts:  $\sigma(T,\rho) - \sigma_0(T)$

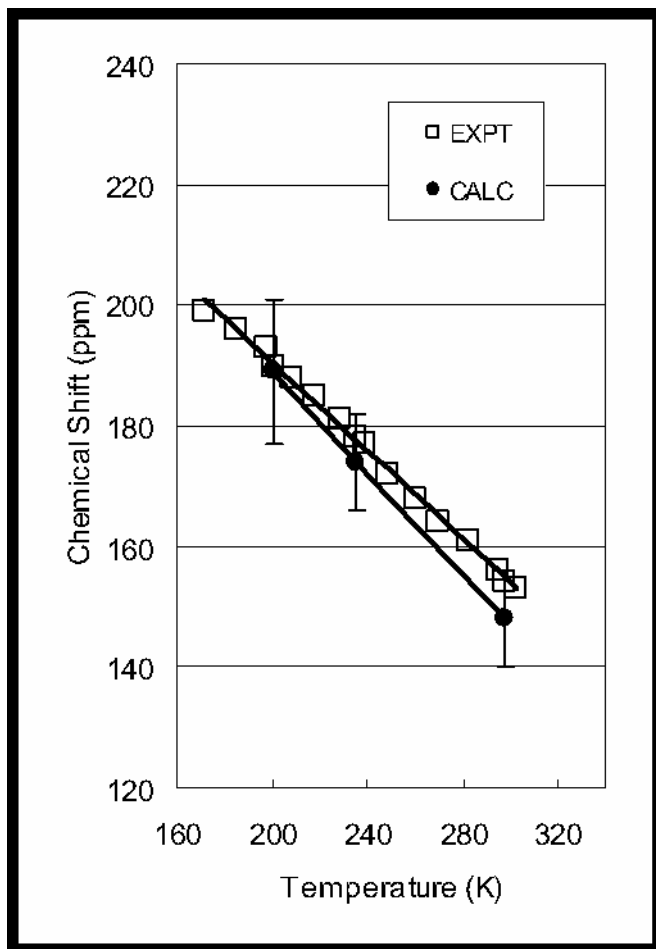
$$\approx \sigma_{1\text{eff}}(T) \rho_{\text{LIQ}}(T) + \dots$$

increasing chemical shift  $\uparrow$

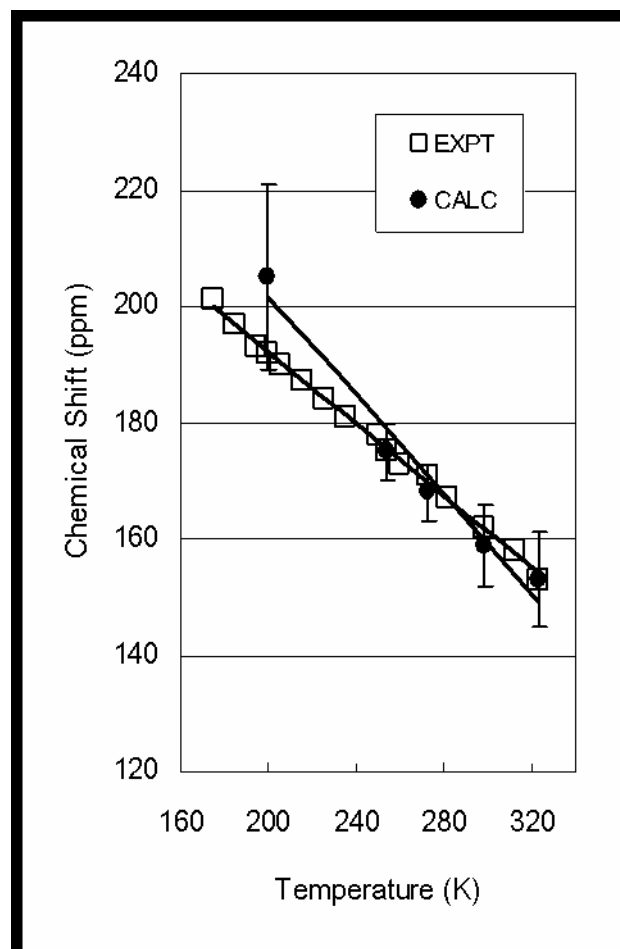


# Xe chemical shift temperature dependence in solution

n-pentane :



n-hexane :



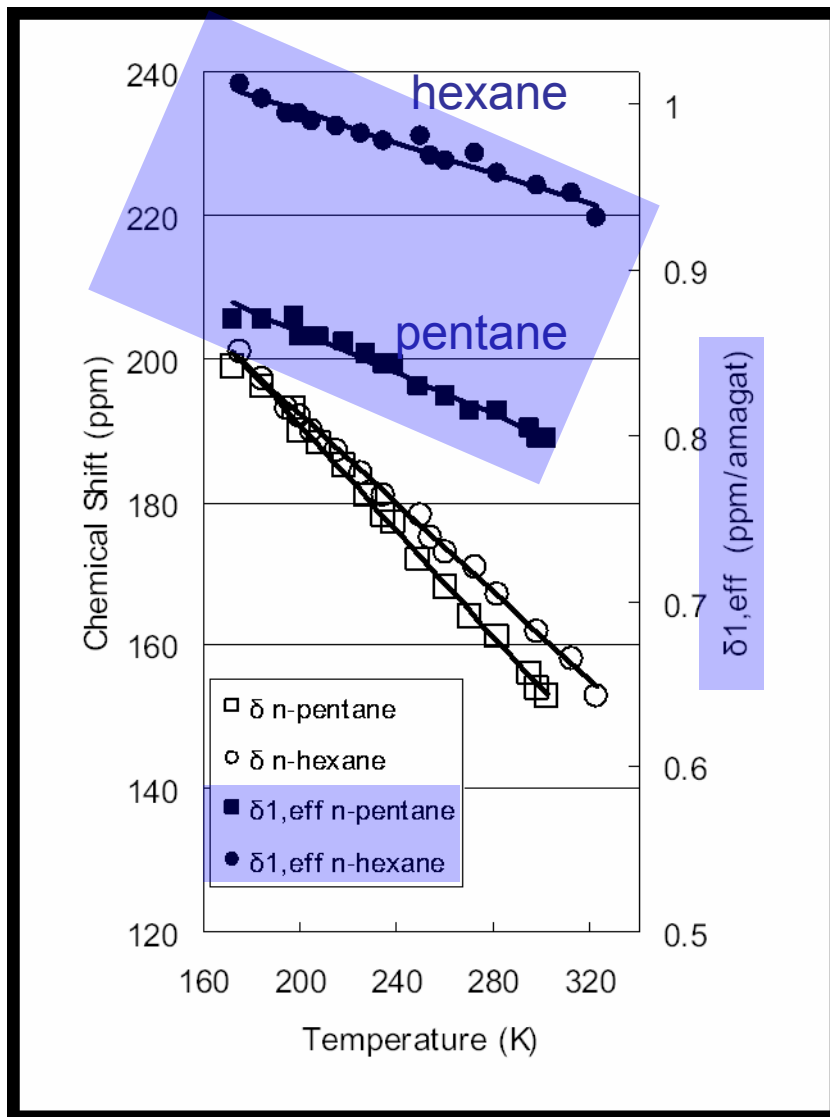
Molecular Dynamics simulations results

**J. Phys. Chem. C**, 111, 15771-15783 (2007).

# Contributions to the temperature dependence of Xe chemical shifts in solution

T dependence of the solvent density

is responsible for most of the observed steep T dependence of Xe chemical shifts in solution. The remainder is from T dependent Xe Interactions with alkane,  $\delta_1(T)$



divide out the density to get  $\delta_{1,eff}$  just as in pure liquids

# VI. intermolecular shifts in heterogeneous systems: one in a cage, $n$ in a cage

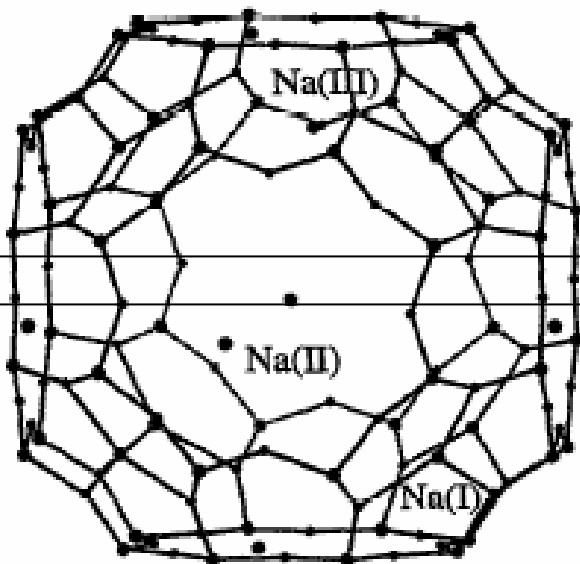
- one Xe in a cage: governed by probability distribution functions changing with temperature
- compare with one Xe in a flexible cage governed by (a) probability distribution functions changing with temperature, and (b) dynamics of cage atoms changing with temperature
- $n$  Xe in a cage governed by (a) one-body probability distribution functions changing with temperature, and (b) two-body distribution functions changing with temperature

# first consider one Xe in a cage, no Xe-Xe interactions

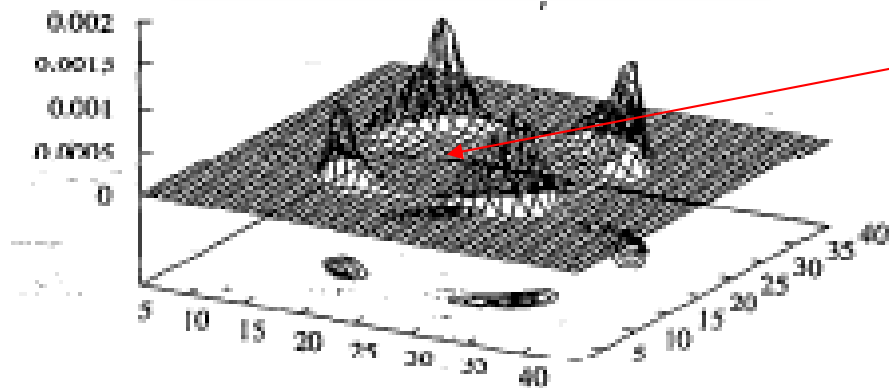
- What is the expected temperature dependence of the chemical shift?
- This depends on the size of the cage relative to the diameter of the Xe atom
- in a small cage, the potential energy surface for the Xe is lowest in the center
- in a larger cage, there are potential energy minima for the Xe at points  $\sim 4 \text{ \AA}$  to the wall, less favorable at the center

# Xe in a rigid cage NaA

Let us take a look at points on this plane



on this plane, where is Xe is likely to be found?

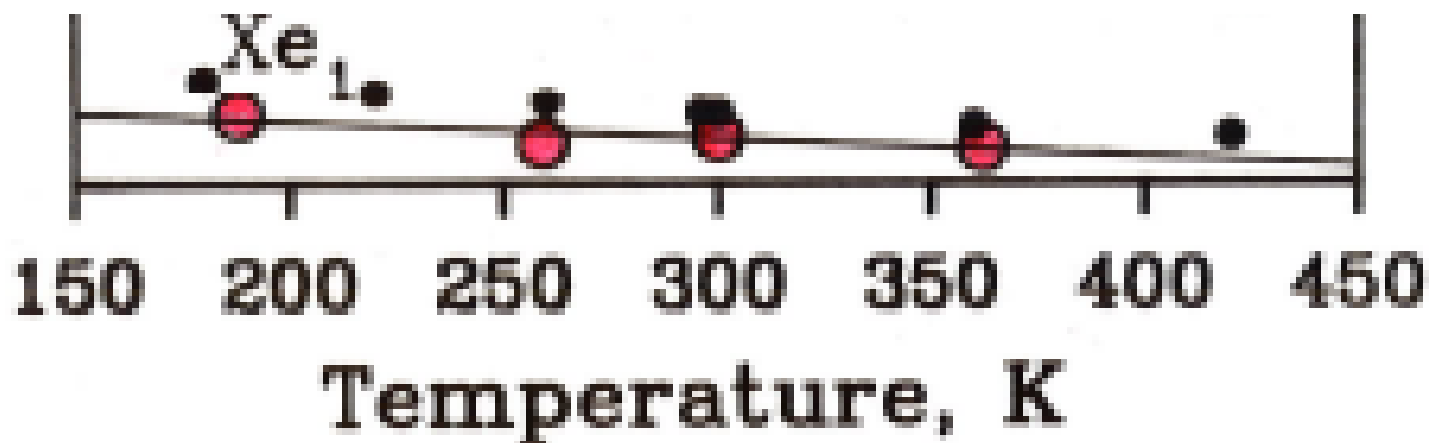


smaller probability  
near center of cage  
where chemical shift  
is lower

With increase in temperature, probability density spreads out, including more of central region where chemical shift is lower

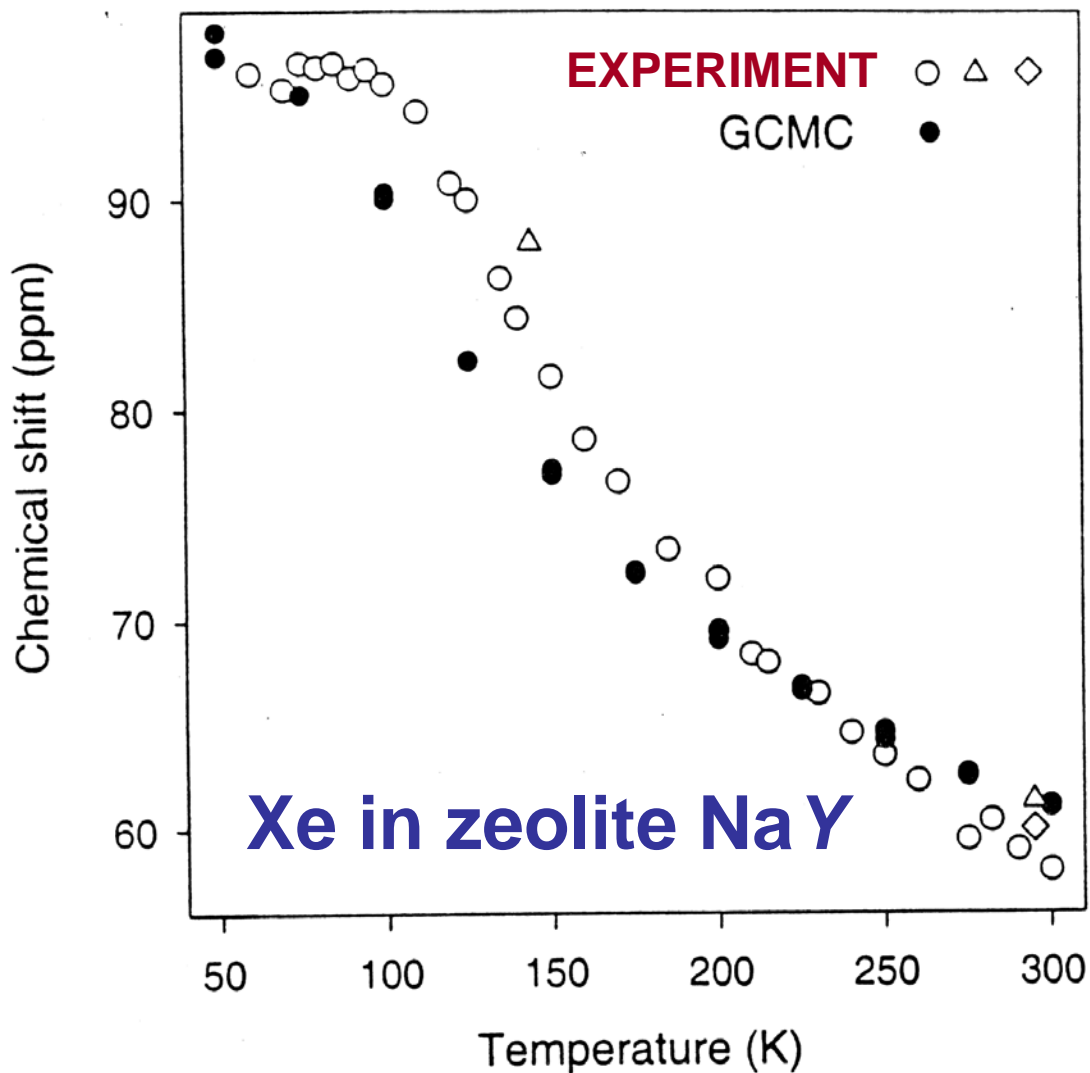


at higher T, Xe can explore regions of higher potential energy and smaller chemical shift

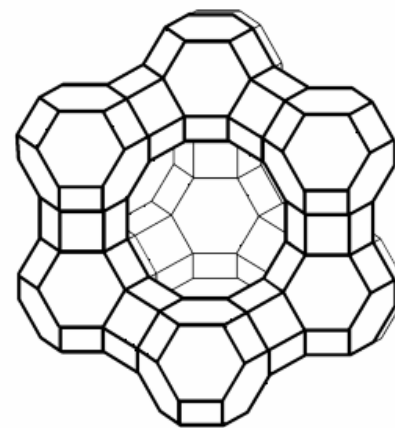


Xe-cage contribution only. This intermolecular chemical shift decreases with increasing temperature

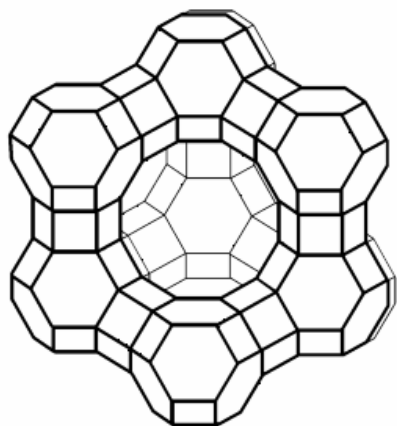
# Temperature dependence of $^{129}\text{Xe}$ chemical shift at near-zero loading



**GCMC simulations**  
Jameson and Kostikin,  
2001



- Expt., Pietraß et al. 1999  $\langle n \rangle_{\text{Xe}} = 0.25$  atoms/cage
- △ Expt., Cheung, 1988  $\langle n \rangle_{\text{Xe}} = 0.2$  atoms/cage
- ◇ Expt., S. B. Liu, 1994  $\langle n \rangle_{\text{Xe}} = 0.2$  atoms/cage
- GCMC calculations  $\langle n \rangle_{\text{Xe}} = 0.250(5)$  atoms/cage

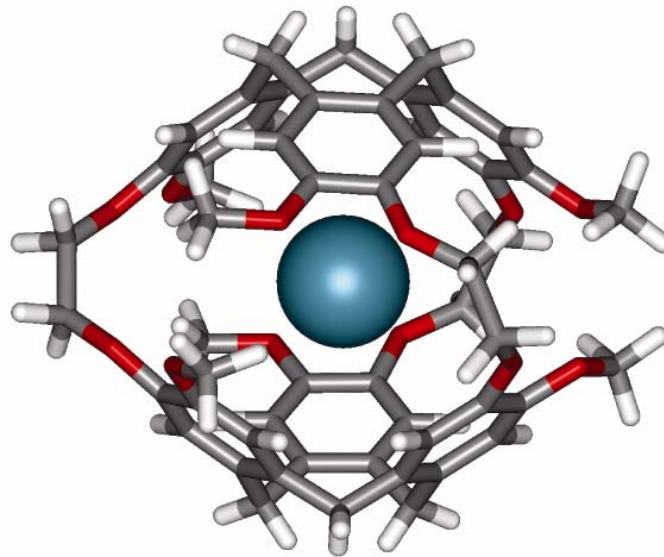


## Xe at near zero loading in NaY

At low temperatures, Xe spends most of its time in the low potential energy regions next to the walls of the large cages, which correspond to higher chemical shifts. As temperature increases, the Xe probability density spreads out over more regions farther away from the walls, which correspond to lower chemical shifts.

**This is the same trend as for one Xe in NaA cage**

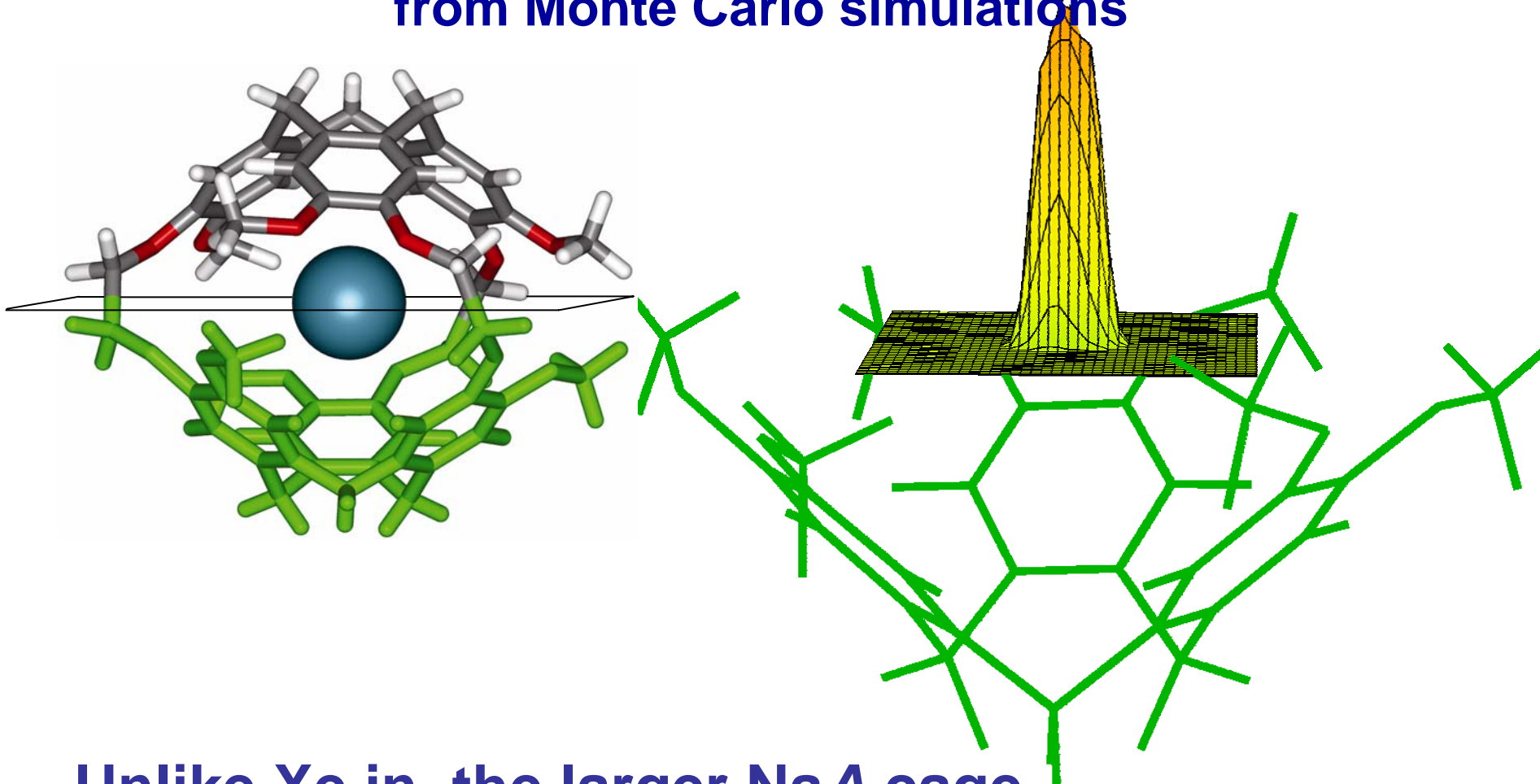
# Xe in a small flexible cage



**two contributions:**

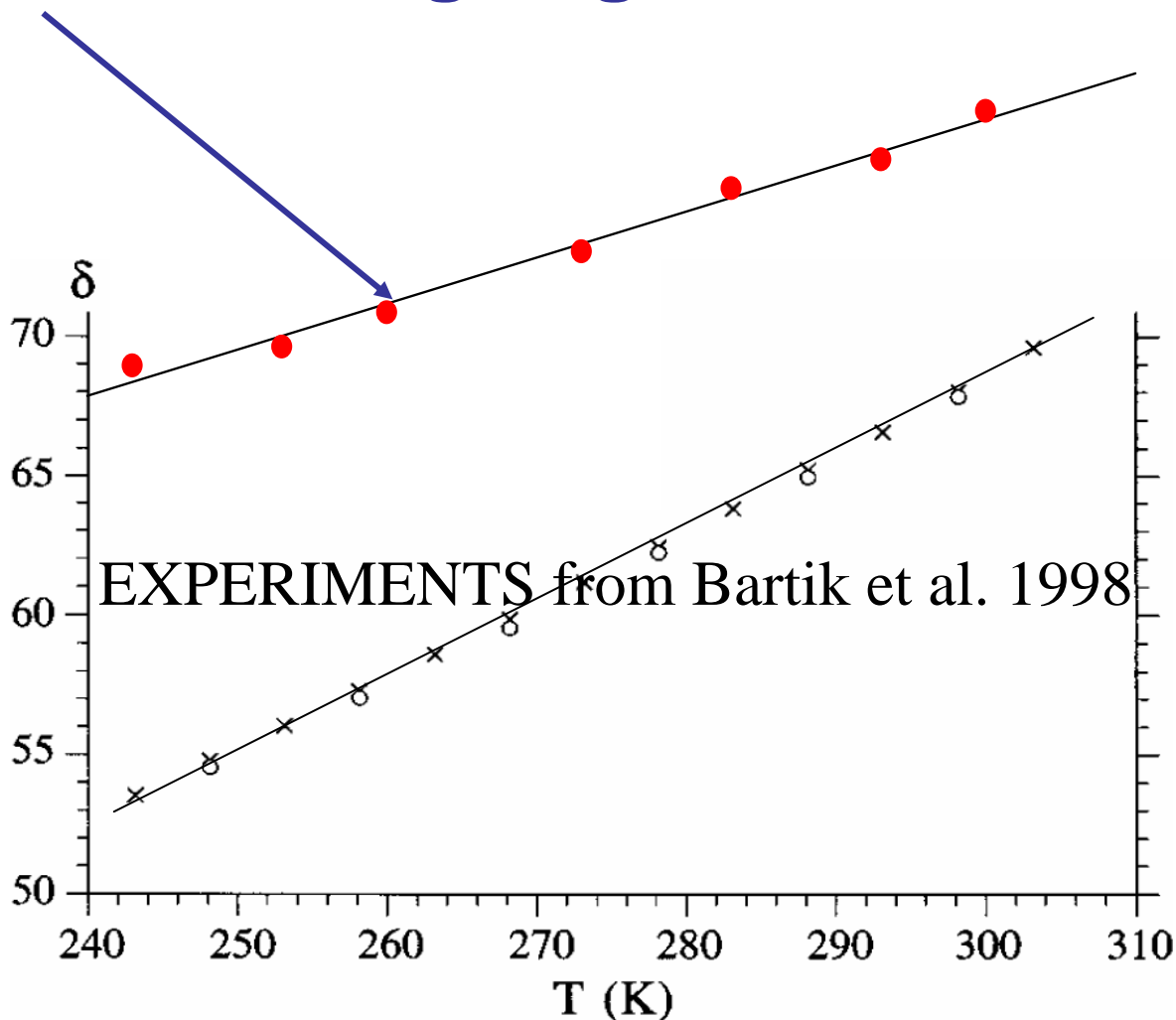
- Xe probability distribution within the cage changes with T
- cage deformation (away from nearly spherical) is more pronounced at higher T, leads to closer Xe interactions with wall atoms

# One-body distribution function for Xe@cryptoA from Monte Carlo simulations



Unlike Xe in the larger NaA cage,  
for Xe in this smaller cage, the probability  
is highest in the center, and lower near the walls.

# Temperature dependence of Xe@cryptoA not including cage deformation



● **Monte Carlo SIMULATIONS**

D. N. Sears and C. J. Jameson, 2003

Our Monte Carlo  
SIMULATIONS

T, K       $\delta$ , ppm

300	78.77
293	76.35
283	75.31
273	73.04
260	70.73
253	69.62
243	68.94

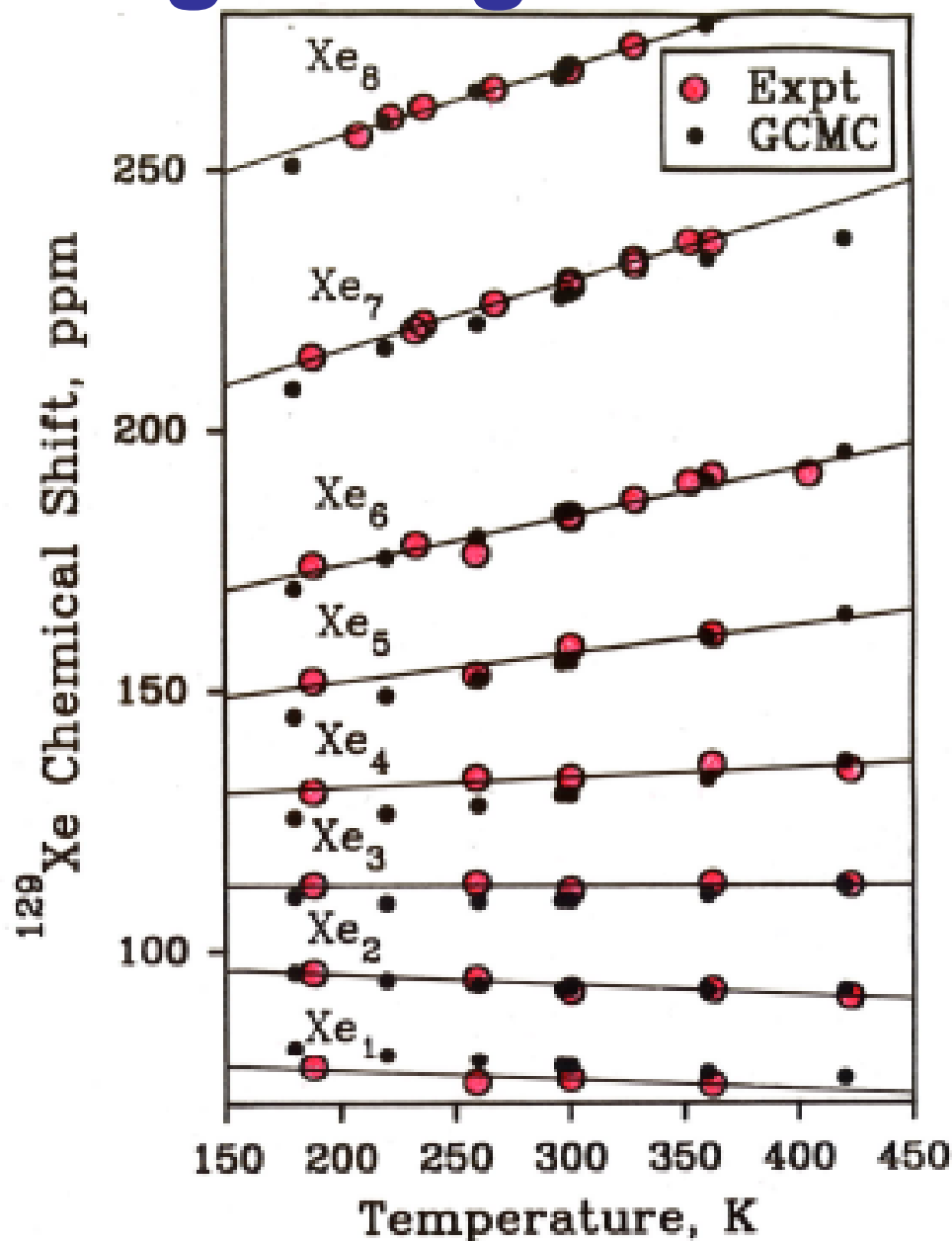
# Xe-Xe chemical shift contributions

- with increasing number of Xe atoms in the same cage, Xe-Xe contributions increase, leading to higher chemical shifts
- for a fixed number of Xe atoms in the cage, temperature dependence is a combination of Xe-Xe contributions changing with T and Xe- wall contributions changing with T

# $n$ Xe atoms in a rigid cage

Xe-Xe contributions dominate over Xe-cage contributions at  $n$  large enough.

Xe-Xe interactions explore regions higher up on repulsive Xe-Xe potential wall at higher T, these correspond to larger chemical shifts.

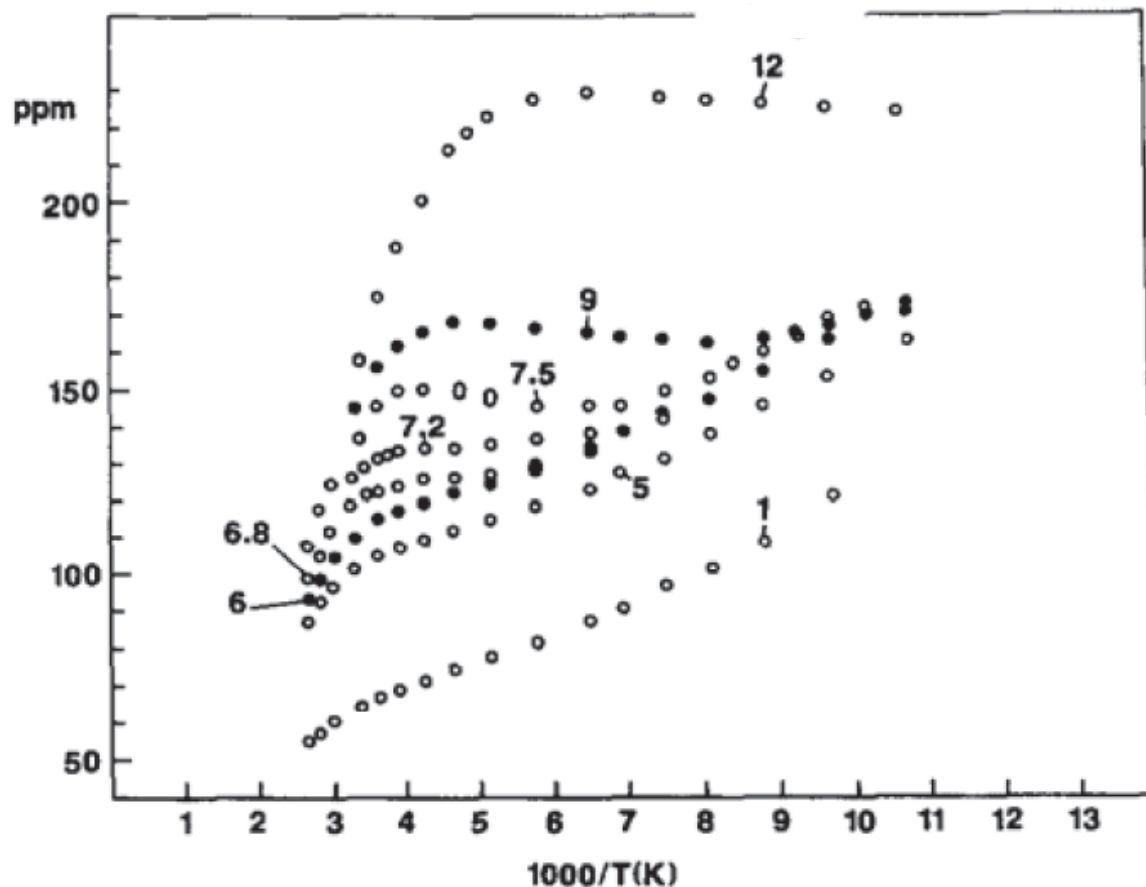




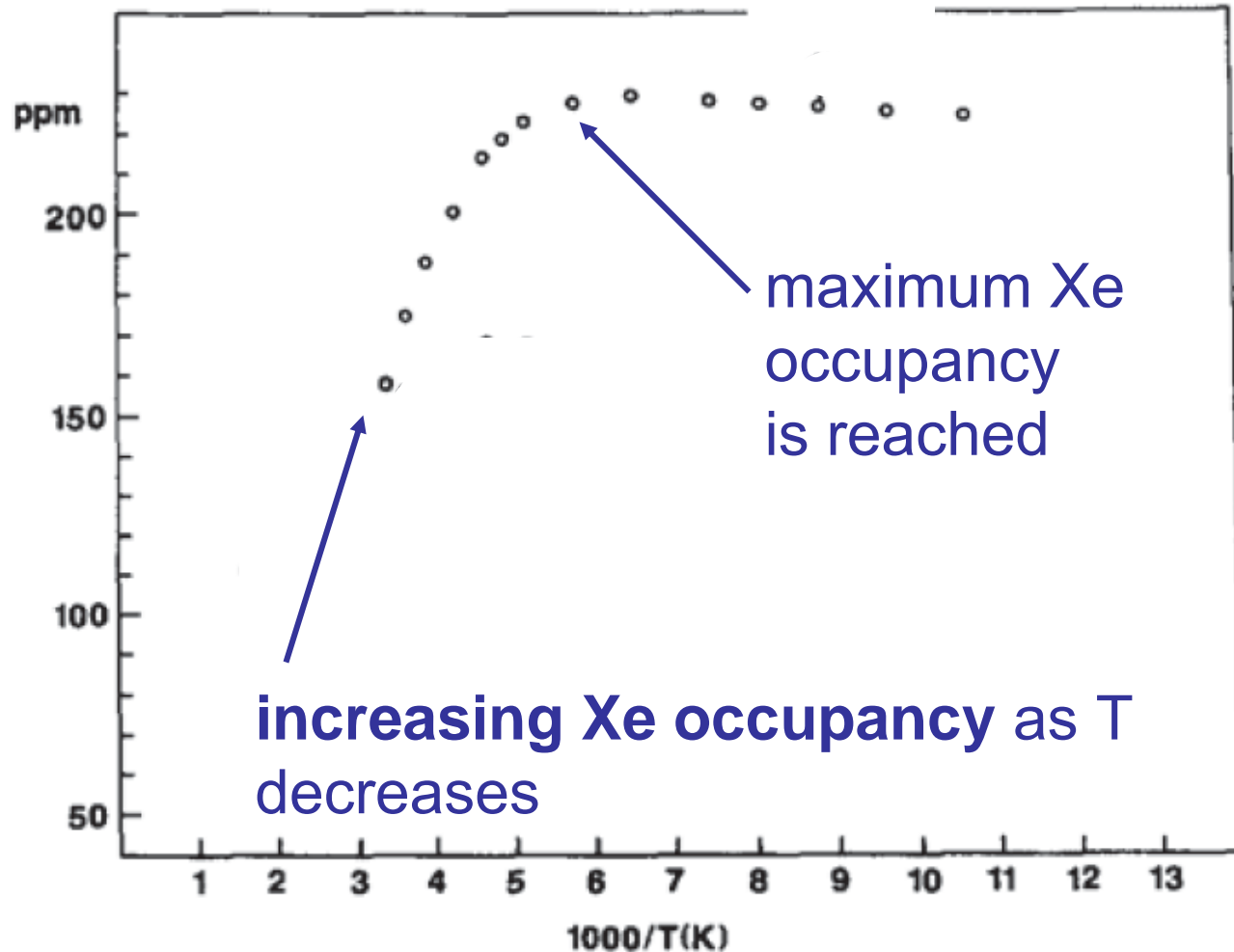
# VII. heterogeneous systems: changing occupancy in a channel

dominated by changes in adsorption isotherm with increasing temperature, that is, **Xe occupancy changes markedly with temperature**

J.A. Ripmeester,  
C. I. Ratcliffe  
Anal. chim. Acta  
283, 1103 (1993)

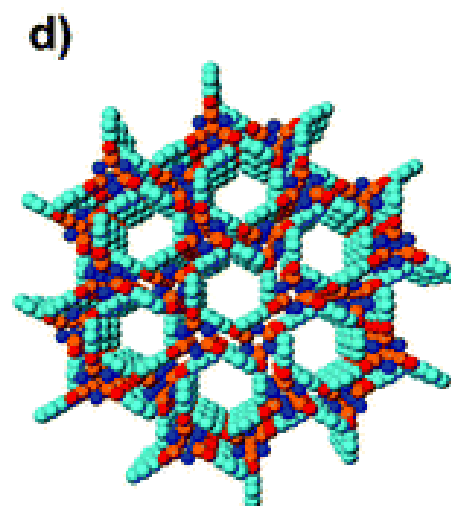
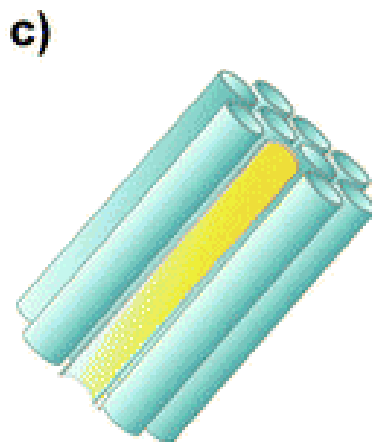
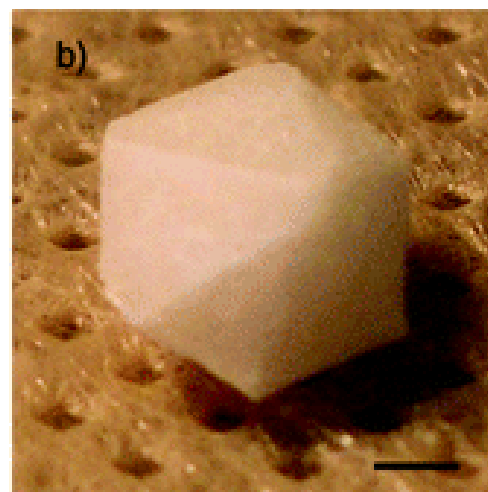
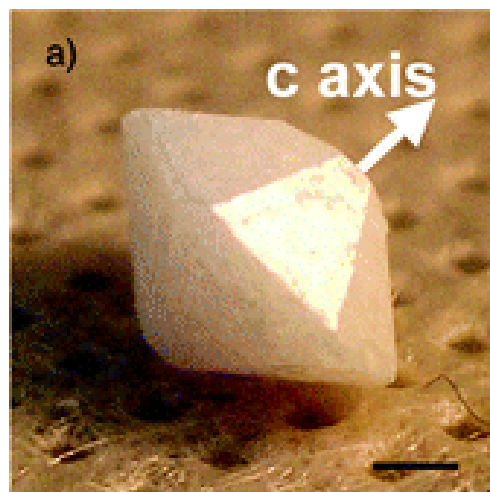


For a sealed sample of Xe in NaY, steep increase in Xe chemical shift from **increasing Xe-Xe contributions**



# single crystal experiments

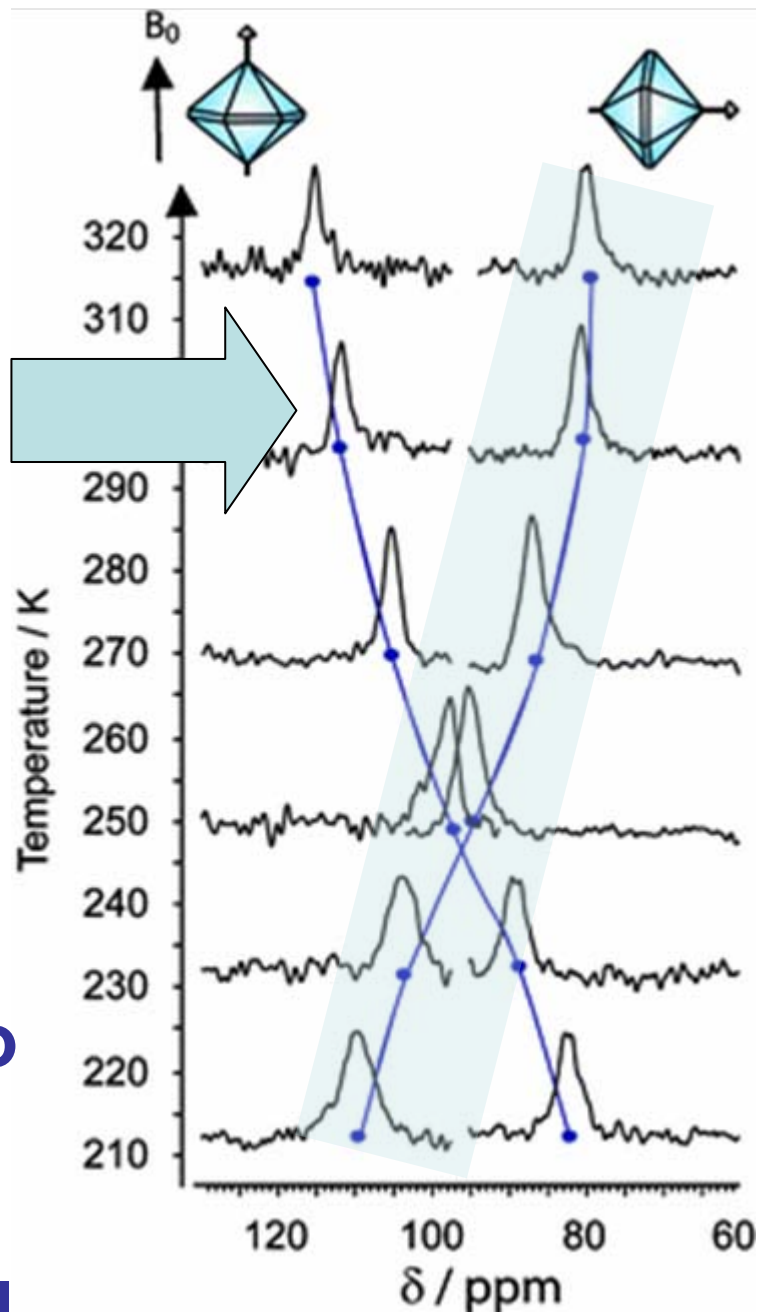
A. Comotti, S. Bracco, L. Ferretti, M. Mauri, R. Simonutti and P. Sozzani Chem Commun 2007, 350-352



continuous flow  
**HP  $^{129}\text{Xe}$   
NMR**

$\delta_{\parallel}$  not  
dependent  
on Xe loading

increases  
with  
increasing T.  
This has to do  
with the  
constrictions  
in the channel



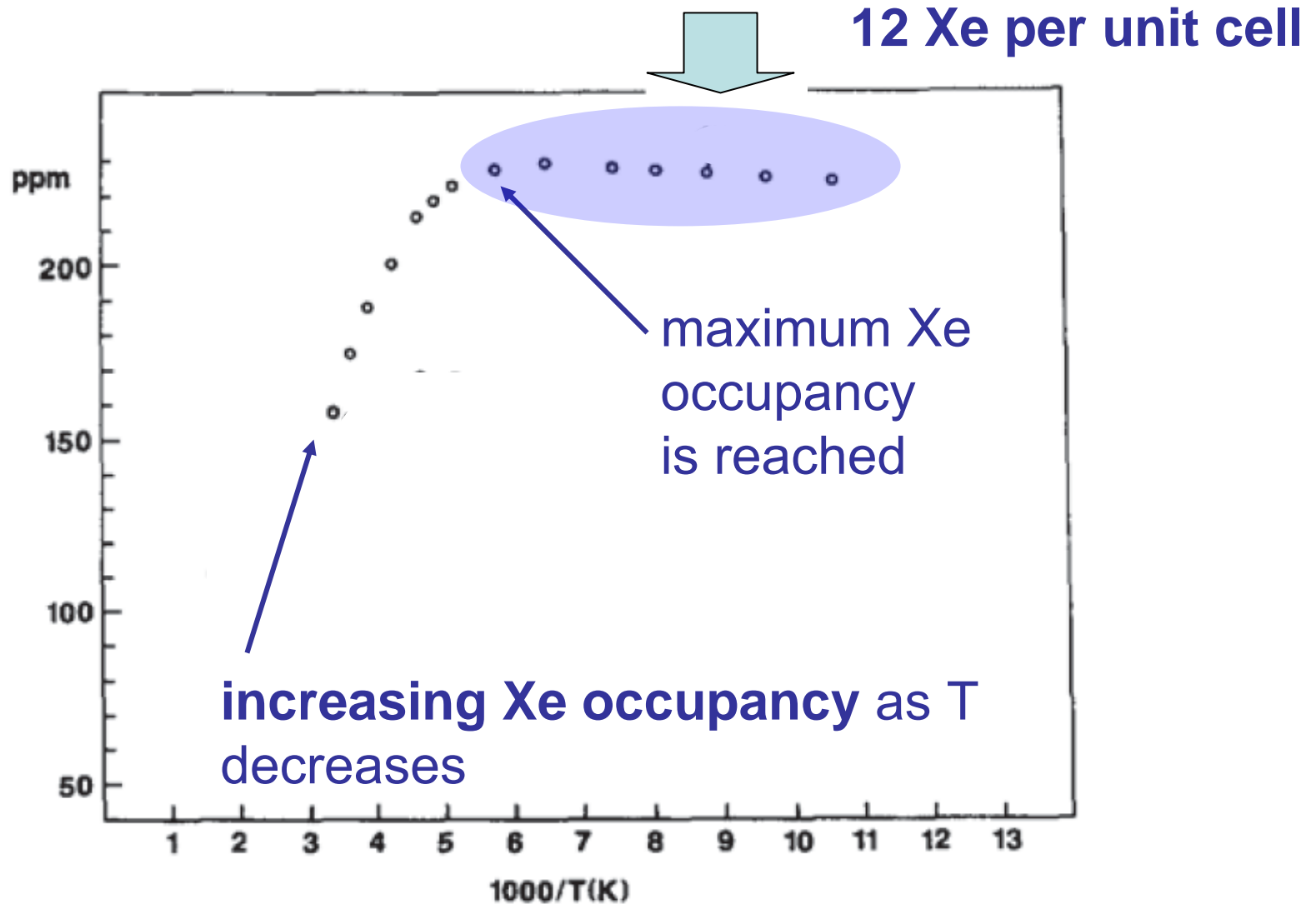
$\delta_{\perp}$  increases  
**Xe-Xe**  
contributions  
increase with  
increasing Xe  
occupancy  
as T  
decreases

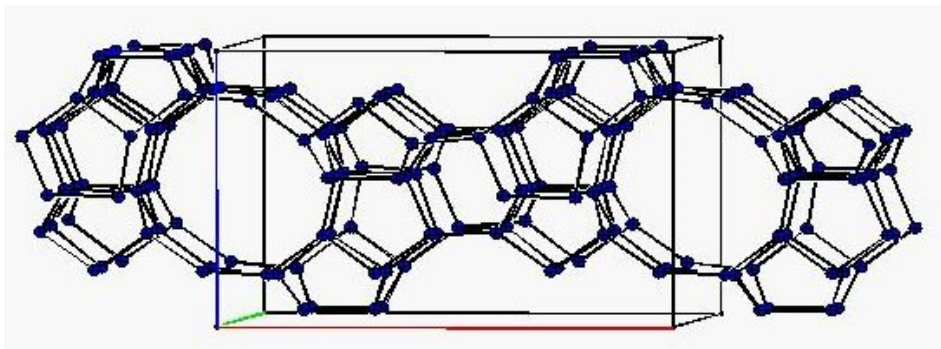
A. Comotti, S. Bracco,  
L. Ferretti, M. Mauri,  
R. Simonutti and  
P. Sozzani  
Chem. Commun.  
2007, 350-352

# observe temperature dependence at fixed Xe occupancy

- Xe in NaY at full occupancy
- Xe in silicalite at full occupancy

# Xe in NaY at full occupancy

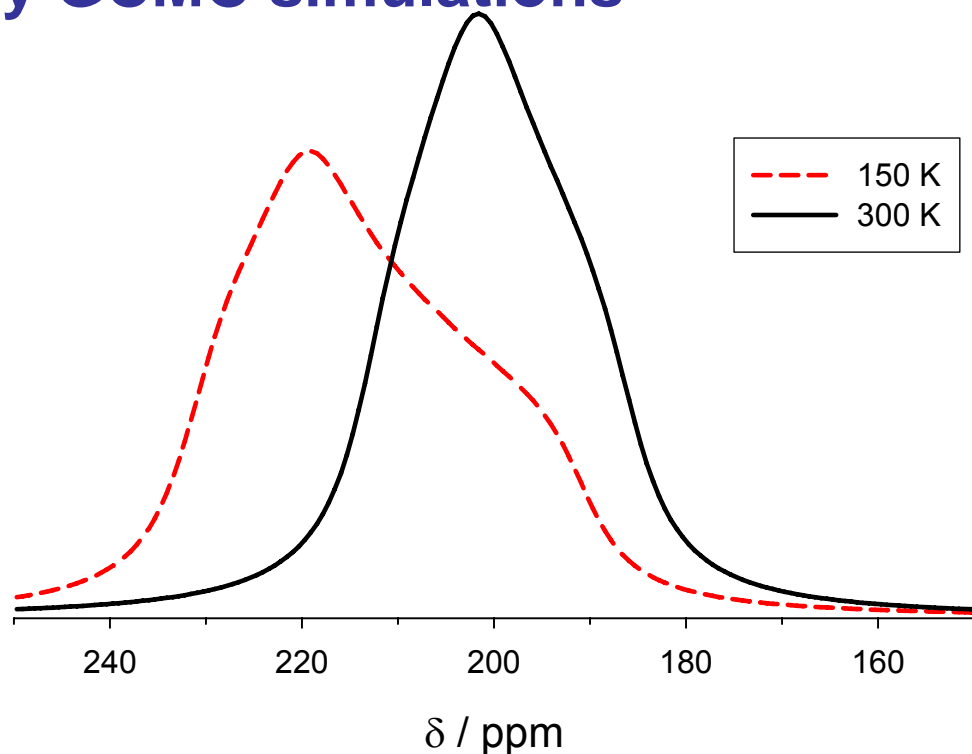




**Xe at full loading**  
(16 Xe per unit cell)  
in silicalite

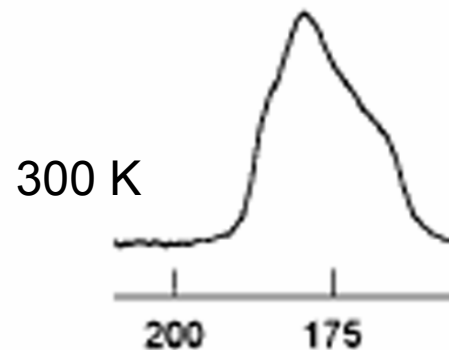
The **anisotropic** environment of silicalite gives rise to **3 unique tensor components** primarily arising from **Xe-Xe contributions**. Two of the components change dramatically with temperature, while the smallest component hardly changes. The changes in the Xe-Xe pair distribution function with temperature predicted by the Monte Carlo calculations reproduce the observed changes in line shape.

# Xe line shapes at full occupancy are well reproduced by GCMC simulations

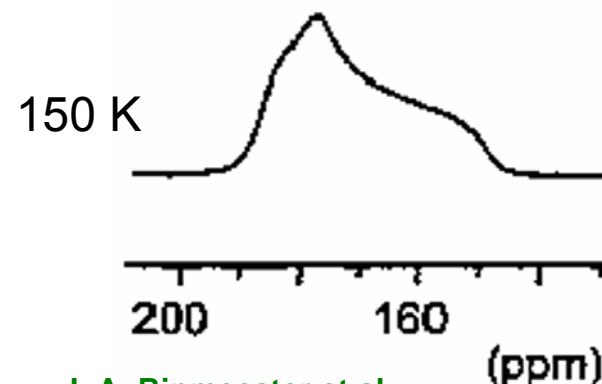


**CALCULATIONS**  
Jameson 2003

# Temperature dependence with no change in $\langle N \rangle_{\text{Xe}}$



Jameson et al.  
*J. Phys. Chem. B* **1997**, 101, 8418



J. A. Ripmeester et al.  
*J. Am. Chem. Soc.* **2001**, 123, 10399

**EXPERIMENTS**  
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Rex E. Gerald II  
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Devin N. Sears  
Lela Vukovic

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