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## Chemistry 342

First Exam

September 24, 1999

$1 \text{ J} = 1 \text{ kg m}^2 \text{ s}^{-2}$      $k_B = 1.38066 \times 10^{-23} \text{ J K}^{-1}$      $R = N_{\text{Avogadro}} k_B$   
 $R = 8.31441 \text{ J mol}^{-1} \text{ K}^{-1} = 1.98718 \text{ cal mol}^{-1} \text{ K}^{-1} = 0.082057 \text{ L atm mol}^{-1} \text{ K}^{-1}$   
 $p/p_0 = \exp[ -(M/RT)gz ]$     *barometric formula where  $g = 9.80665 \text{ m s}^{-2}$*   
 monatomic gas molar heat capacity:  $C_V = (3/2)R$   
*General relations for any equation of state:*  
 $(\partial U / \partial V)_T = T(\partial p / \partial T)_V - p$      $(\partial H / \partial p)_T = -T(\partial V / \partial T)_p + V$   
 $C_p - C_V = \{ p + (\partial U / \partial V)_T \} (\partial V / \partial T)_p$

1. A monatomic gas obeys the equation of state  $pV = nRT + nap$  where  $a = 0.02 \text{ L mol}^{-1}$ , such that  $(\partial U / \partial V)_T = 0$  for the gas. This gas is taken from state **A** (10. L, 1 atm,  $T = 304.7 \text{ K}$ ) to state **B** (? L, 20 atm,  $T = 304.7 \text{ K}$ ) by several possible paths.

Path I : A compression along the isotherm connecting initial and final states.

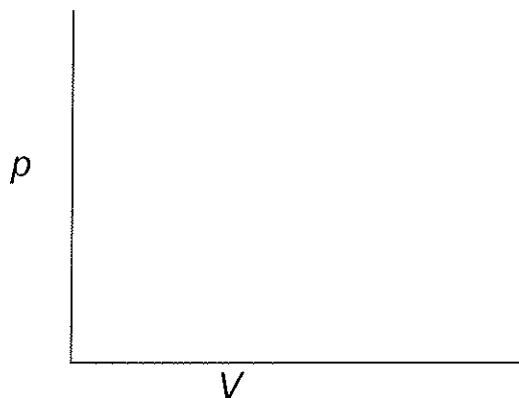
Path II: A constant volume process which takes the gas from the initial pressure to the final pressure, followed by a constant pressure (20 atm) process which takes the gas to the final state.

Path III: A constant pressure (1 atm) process which takes the gas from the initial volume to the final volume, followed by a constant volume process which takes the gas to the final state.

Consider each **A**→**B** path and **calculate**  $\Delta U$  and  $\Delta H$  in joules **for each path**.

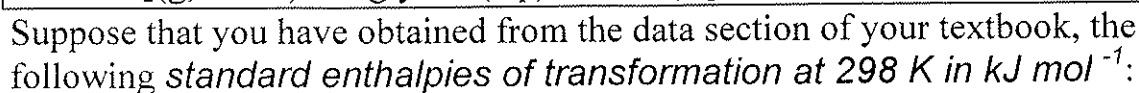
**For each path, calculate**  $q$  and  $W$  where possible (if not, say why not).

First, **draw** these three paths on the  $pV$  diagram of the gas:




| Path I     | Path II    | Path III   |
|------------|------------|------------|
| $W$        | $W$        | $W$        |
| $q$        | $q$        | $q$        |
| $\Delta U$ | $\Delta U$ | $\Delta U$ |
| $\Delta H$ | $\Delta H$ | $\Delta H$ |

Consider one of the large number of reactions that may occur:


$$\Delta H^\ominus \text{ of hydrolysis of 1 mol solid urea to CO}_2 \text{ and ammonia} = b$$
$$\Delta H^\ominus \text{ of dissolution of solid glycine} = c$$
$$\Delta H^\ominus \text{ of dissolution of solid urea} = d$$

In case you have forgotten: glycine  $\text{NH}_2\text{CH}_2\text{COOH}$     urea  $\text{H}_2\text{NCONH}_2$   
(aq.) means very dilute aqueous solutions

Suppose  $n$  moles of urea are produced via this reaction per day, how many  $\text{kJ day}^{-1}$  is the contribution of this reaction to the metabolic rate?



3. If two gases A and B of molecular weight  $x$  and  $y$  ( $\text{g mol}^{-1}$ ) respectively are found at equal abundance in the atmosphere at sea level, at what height should we expect to find gas A to be three times as abundant as gas B? You may assume that the atmosphere is isothermal at 298 K.

4. If a compound is burned under adiabatic conditions so that all the heat evolved is used in heating the product gases, the maximum temperature reached is called the adiabatic flame temperature. **Calculate this temperature** for the burning of acetylene (ethyne) in oxygen sufficient for complete combustion to  $\text{CO}_2$  and  $\text{H}_2\text{O}(\text{g})$ . **Predict:** Do you expect the flame temperature of an oxyacetylene torch to be higher or lower when excess oxygen is used?

For ease of calculations, assume independent of temperature the following data:

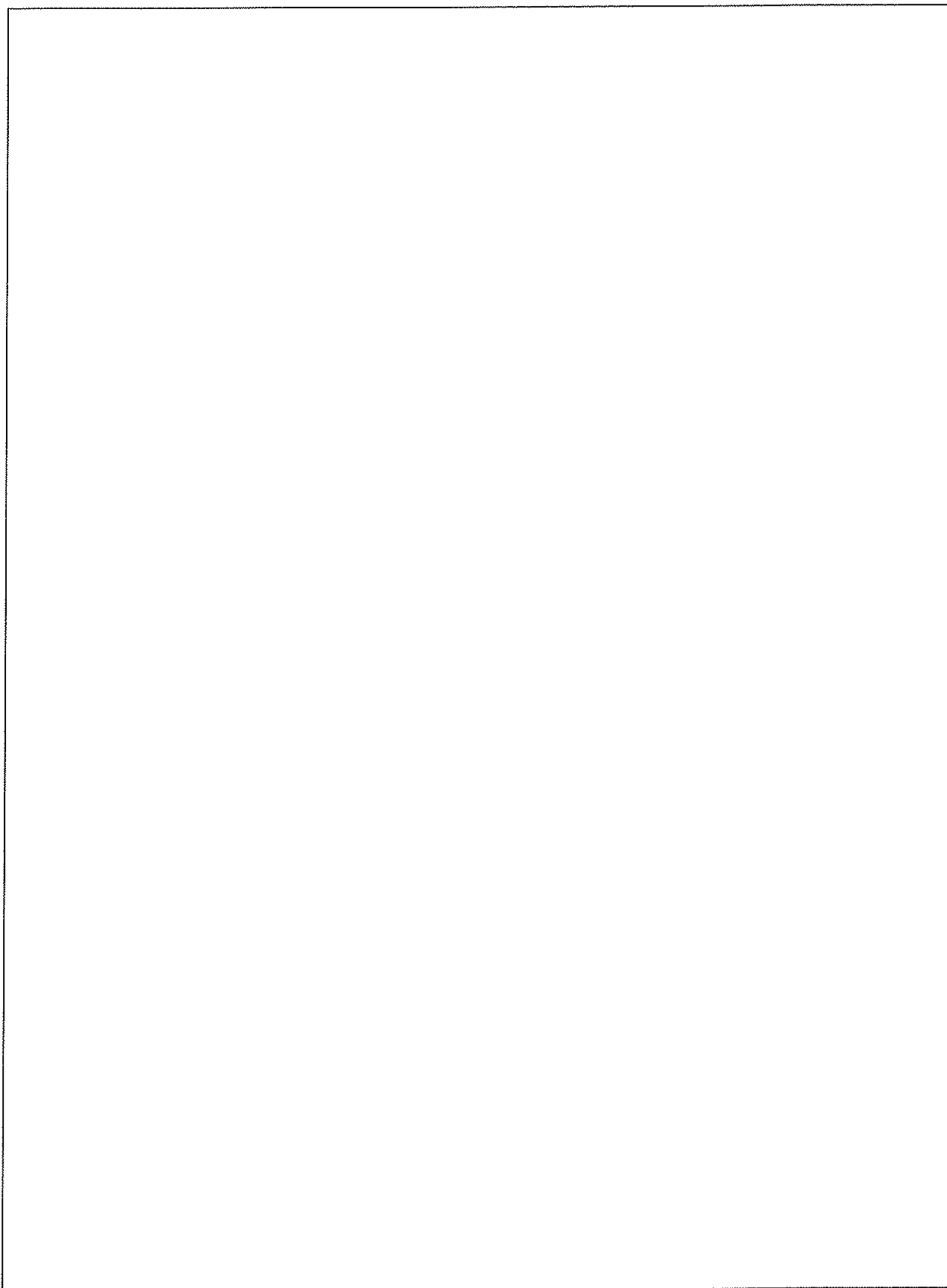
|                                | $C_p \text{ J mol}^{-1} \text{ K}^{-1}$ | $C_v \text{ J mol}^{-1} \text{ K}^{-1}$ |
|--------------------------------|---|---|
| $\text{H}_2(\text{g})$         | 28.824                                  | 20.5                                    |
| $\text{O}_2(\text{g})$         | 29.355                                  | 21.0                                    |
| $\text{H}_2\text{O}(\text{g})$ | 33.58                                   | 25.3                                    |
| $\text{H}_2\text{O}(\text{l})$ | 75.291                                  | 75.2                                    |
| $\text{CO}_2(\text{g})$        | 37.11                                   | 28.8                                    |
| $\text{HCCH}(\text{g})$        | 43.93                                   | 35.0                                    |

Also, you may use the following values at 298 K

| $\Delta_f \text{H}^\ominus$ for the formation of | $\Delta_f \text{H}^\ominus \text{ kJ mol}^{-1}$ |
|--|---|
| $\text{H}_2\text{O}(\text{g})$                   | -241.82   |
| $\text{H}_2\text{O}(\text{l})$                   | -285.83   |
| $\text{CO}_2(\text{g})$                          | -393.51   |
| $\text{HCCH}(\text{g})$                          | +226.73   |

and at 373 K

| $\Delta_{\text{vap}} \text{H}^\ominus$ for $\text{H}_2\text{O}$ $\text{kJ mol}^{-1}$ |
|--|
| 40.656   |



5

6. Ten moles of nitrogen at 300 K are held by a piston under 40 atm pressure. The pressure is suddenly released to 10 atm and then the gas expands adiabatically. If  $C_V$  for  $N_2$  is assumed to be constant and equal to  $20.8 \text{ J mol}^{-1} \text{ K}^{-1}$ , calculate the final temperature of the gas. Assume the gas is ideal. Calculate  $\Delta U$  and  $\Delta H$  for the change in the gas.

|            |            |
|------------|------------|
|            |            |
| $\Delta U$ | $\Delta H$ |